Lecture 20-21: Introduction to Reinforcement Learning

CS109B Data Science 2 Pavlos Protopapas, Mark Glickman, and Chris Tanner





https://www.theopennotebook.com/20 20/04/13/now-peep-this-announcing-th e-winners-of-peepyourscience-2020/

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Outline

- What is Reinforcement Learning?
- RL Formalism:
 - 1. Reward
 - 2. The agent
 - 3. The environment
 - 4. Actions
 - 5. Observations
- Markov Decision Process:
 - 1. Markov Process
 - 2. Markov Reward Process
 - 3. Markov Decision process

- Learning Optimal Policies
 - 1. Model Based (knowing the transition matrix):
 - i. Value Iteration
 - ii. Policy Iteration
 - 2. Model Free (not knowing the transition matrix):
 - I. Q-Learning
 - II. SARSA



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The setting

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		4
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Lapan, Maxim. Deep Reinforcement Learning Hands-On



- A maze with walls, food and electricity
- Mouse can move left, right, up and down
- Mouse wants the cheese but not electric shocks
- Mouse can observe the environment



The setting

	4	1
		5
-		

- Mouse => Agent
- A maze with walls, food and electricity => Environment
- Mouse can move left, right, up and down => Actions
- Mouse wants the cheese but not electric shocks => Rewards
- Mouse can observe the environment
 => Observations



Learn to make sequential decisions in an environment to maximize some notion of overall **rewards** acquired along the way.



In simple terms:

The mouse is trying to find as much food as possible while avoiding an electric shock whenever possible.

The mouse could be brave and get an electric shock to get to the place with plenty of food—this is a better result than just standing still and gaining nothing.



What is Reinforcement Learning?

- Learn to make sequential decisions in an environment to maximize some notion of overall **rewards** acquired along the way.
- Simple Machine Learning problems have a hidden time dimension, which is often overlooked, but it is crucial to production systems.
- **Reinforcement Learning** incorporates time (or an extra dimension) into learning, which puts it much close to the human perception or artificial intelligence.



What don't we want the mouse to do?

- We do **not** want to have the best actions to take in every specific situation. Too much and not flexible.
- Find a magic set of methods that will allow our mouse to learn how to avoid electricity and gather as much food as possible.

Reinforcement Learning is precisely this magic toolbox.



Challenges of RL

- Observations depend on the agent's actions. If the agent decides to do stupid things, then the observations will tell nothing about improving the outcome (only negative feedback).
- Agents need to not only **exploit** the policy they have learned but to actively **explore** the environment. In other words, maybe by doing things differently, we can significantly improve the outcome. This **exploration/exploitation** dilemma is among the open fundamental questions in RL (and in my life).
- Reward can be delayed from actions. Ex: In cases of chess, it can be one single strong move in the middle of the game that has shifted the balance.



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RL formalisms and relations



- Agent
- Environment

Communication channels:

- Actions,
- Reward, and
- Observations:

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- A scalar value obtained from the environment
- It can be positive or negative, large or small
- The purpose of the reward is to tell our agent how well they have behaved

reinforcement = reward or **reinforced** the behavior

Examples:

- Cheese or electric shock
- Grades: Grades are a reward system to give you feedback about you are paying attention to me.



All goals can be described by the maximization of some expected cumulative reward.







An agent is somebody or something who/which interacts with the environment by executing certain actions, taking observations, and receiving eventual rewards for this.

In most practical RL scenarios, it's our piece of software that is supposed to solve some problems in a more-or-less efficient way.

Example:

You



Everything outside of the agent.

The universe!

The environment is external to an agent, and communications to and from the agent are limited to rewards, observations and actions.





Things the agent can do in the environment. Can be:

- moves allowed by the rules of play (if it's some game),
- doing homework (in the case of school).

They can be simple such as move pawn one space forward, or complicated such as fill the tax form.

Could be discrete or continuous



Second information channel for an agent, with the first being a reward.

Why? Convenience



RL within the ML Spectrum



What makes RL different from other ML paradigms ?

- No supervision, just a reward signal from the environment.
- Feedback is sometimes delayed (Example: Time taken for drugs to take effect).
- Time matters sequential data
- Feedback Agent's action affects the subsequent data it receives (not i.i.d.).



Many Faces of Reinforcement Learning



- Defeat a World Champion in Chess, Go, BackGammon
- Manage an investment portfolio
- Control a power station
- Control the dynamics of a humanoid robot locomotion
- Treat patients in the ICU
- Automatic fly stunt manoeuvres in helicopters



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More terminology we need to learn before proceeding:

- state
- episode
- history
- value
- policy



Example:

System: Weather in Boston.

States: We can observe the current day as **sunny**, **rainy** or **windy**. **History**: A sequence of observations over time forms a **chain** of **states**, such as:

[sunny, sunny, rainy, sunny, ...],



- For a given system we observe states.
- The system changes between states according to some dynamics.
- We do not influence the system just observe.
- There are only finite number of states (could be very large).
- Observe a sequence of states or a chain => Markov chain.

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A system is a **Markov Process**, if it fulfils the **Markov property**.

The future system dynamics from any state have to depend on this state only.

- Every observable state is self-contained to describe the future of the system.
- Only one state is required to model the future dynamics of the system, not the whole history or, say, the last N states.



Weather example:

The probability of sunny day followed by rainy day is independent of the amount of sunny days we've seen in the past.

Notes:

This example is really naïve, but it's important to understand the limitations.

We can for example extend the state space to include other factors.



Markov Process (cont)

Transition probabilities is expressed as a **transition matrix**, which is a square matrix of the size N×N, where N is the number of states in our model.

	sunny	rainy
sunny	0.8	0.2
rainy	0.1	0.9





In practice, we rarely know the exact transition matrix. A more realistic scenario is when we have only observations of our systems' states, which we call **episodes**:

Episodes:

- rainy, cloudy, cloudy, sunny
- cloudy, cloudy, sunny



Extend Markov process to include rewards.

Add another square matrix which tells us the reward for going from state *i* to state *j*.

Often (but not always the case) the reward only depends on the landing state so we only need a number, R_t .

Note: Reward is just a number, positive, negative, small, large



For every time point, we define **return** as a sum of **subsequent** rewards:

$$G_t = R_{t+1} + R_{t+2} + \dots$$

Distance and all at a set was seen as a set of a



The **return** quantity is not very useful in practice, as it was defined for every specific chain. But since there are probabilities to reach other states this can vary a lot depending which path we take.



How to extend our Markov Return Process (MRP) to include **actions**?

We must add a set of actions (A), which has to be finite. This is our agent's action space.

Condition our transition matrix with action, which means the transition matrix needs an extra action dimension => turns it into a cube.





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By choosing an action, the agent can affect the probabilities of target states, which is GREAT to have.

Finally, to turn our MRP into an MDP, we need to add actions to our reward matrix in the same way we did with the transition matrix: our reward matrix will depend not only on state but also on action.

In other words, it means that the reward the agent obtains now depends not only on the state it ends up in but also on the action that leads to this state. It's similar as when putting effort into something, you're usually gaining skills and knowledge, even if the result of your efforts wasn't too successful.



More terminology we need to learn

- state 🗸
- episode ✓
- history \checkmark
- value \checkmark
- policy



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We are finally ready to introduce the most important central thing for MDPs and Reinforcement Learning:

policy

The intuitive definition of policy is that it is some set of rules that controls the agent's behavior.



Even for fairly simple environments, we can have a variety of policies.

- Always move forward
- Try to go around obstacles by checking whether that previous forward action failed
- Funnily spin around to entertain
- Choose an action randomly



Remember: The main objective of the agent in RL is to gather as much return (which was defined as discounted cumulative reward) as possible.

Different policies can give us different return, which makes it important to find a good policy. This is why the notion of policy is important, and it's the central thing we're looking for.



Formally, policy is defined as the probability distribution over actions for every possible state:

$$\pi(a|s) = P(A_t = a|S_t = s)$$

An optimal policy π^* is one that maximizes the expected value function :

$$\pi^*$$
 = argmax $_{\pi}V_{\pi}(s)$



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Learning Optimal Policies

Dynamic Programming Methods (Value and Policy Iteration)

We introduced the concept of value state without a policy in mind. Now we should introduce a value that depends on the policy. The **value function** of a state *s* under a policy π , denoted $v_{\pi}(s)$, is the expected return when starting in *s* and following π thereafter:



$$v_{\pi}(s) = \mathbb{E}_{\pi} \left[G_t | S_t = s \right] = \mathbb{E}_{\pi} \left[\sum_{k=0} \gamma^k R_{t+k+1} | s \right]$$



Consider discount factor $\gamma = 0.5$

Policy: always go left

$$v(S_0) = -1 + 0.5(-1) + (0.5)^2(-1) + \dots = -2$$

$$v(S_1) = -1 + 0.5(-1) + (0.5)^2(-1) + \dots = -2$$

$$v(S_1) = -1 + 0.5(-1) + (0.5)^2(-1) + \dots = -2$$



For any policy π and any state s, the following consistency condition holds between the value of s and the value of its possible successor states:



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Dynamic Programming - Value function

Revisit MDP. What is p(s', r|s, a)? p(s', r|s, a) = p(s'|s, a)p(r|s, a)





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We define action-value function for policy π to be the value of taking action a in state s under a policy π , denoted $q_{\pi}(s, a)$:

$$q_{\pi}(s,a) = \mathbb{E}[G_t|s,a] = \mathbb{E}[\sum_{k=0}^{\infty} \gamma^k R_{t+k+1} | S_t = s, A_t = a]$$
$$q_{\pi}(s,a) = \mathbb{E}[R_{t+1} + \gamma \nu_{\pi}(S_{t+1}) | S_t = a, A_t = a]$$

$$= \sum p(s', r|s, a)[r + \gamma v_{\pi}(s')]$$







Consider discount factor $\gamma = 0.5$ Policy: **always go left**

$$q(S_0, left) = -1 + 0.5(-1) + (0.5)^2(-1) + \dots = -2$$





Lets start with state S_0 , and take the action a_j , then the value will be

$$V_0(a=a_i)=R_i+\gamma V_i$$

So, to choose the best possible action, the agent needs to calculate the resulting values for every action and choose the maximum possible outcome. (not totally greedy)

$$V_0 = \max_{a \in 1 \dots N} (R_a + \gamma V_a)$$



Bellman equation (stochastic)



Bellman optimality equation for the general case:

$$V_0 = \max_{a \in A} \sum_{s \in S} p_{a,0 \to s} (R_{s,a} + \gamma V_s)$$



Model Based:

Knowing the transition matrix.

Model Free:

Not knowing the transition matrix.



Model-Based Methods

Policy Iteration

- 1. Set π , the policy to evaluate
- 2. Set a small threshold θ determining accuracy of estimation
- 3. Initialize V(s), for all s, arbitrarily except that V(terminal) = 0
- 4. Loop:



Using iterative policy evaluation for estimating $\pi\approx\pi^{\star}$

1. Initialization:

 $\pi(s)$ and V(s)arbitrarily

- 2. Policy Evaluation: (as before) but actions are given from policy π
- 3. Policy Improvement:
 - policy_stable = true
 - For each state, s:
 - $old_action = \pi(s)$
 - $\pi(s) = \operatorname{argmax}_{a} \sum_{s',r} p(s',r|s,a)[r + \gamma V(s')]$
 - If $old_action \neq \pi(s)$ then $policy_stable = false$

policy_stable = *true*, then stop and return $\pi \approx \pi^*$ else got to 2



References:

Sutton and Barto, Reinforcement Learning (<u>http://incompleteideas.net/book/RLbook2018.pdf</u>)

Maxim Lapam, Deep Reinforcement Learning Hands-On: Apply Modern RL Methods, with Deep Q-networks, Value Iteration, Policy Gradients, TRPO, AlphaGo Zero and More

Model Free Methods

SARSA and Q-learning Friday at a-sec by Javier Zazo





I am Pavlos Protopapas Thank you!

