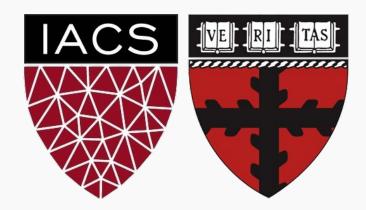




Lecture 13: Recurrent Neural Networks

CS109B Data Science 2 Pavlos Protopapas, Mark Glickman, and Chris Tanner

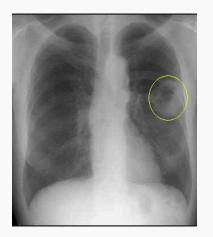


Outline

Why Recurrent Neural Networks (RNNs) Main Concept of RNNs More Details of RNNs RNN training Gated RNN



Many classification and regression tasks involve data that is assumed to be independent and identically distributed (i.i.d.). For example:



Detecting lung cancer



Face recognition



Risk of heart attack



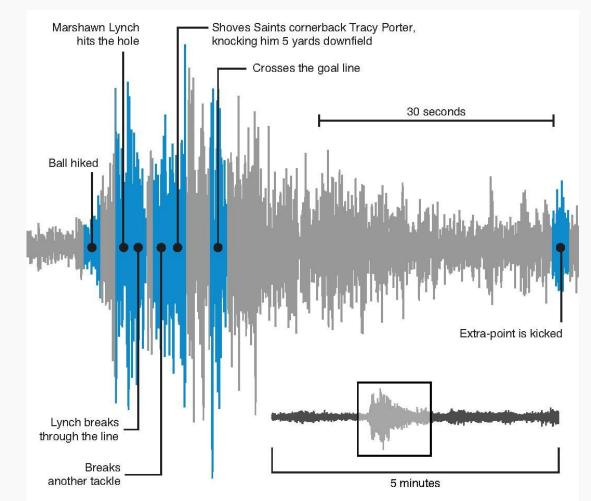
Much of our data is inherently sequential

scale	examples
WORLD	Natural disasters (e.g., earthquakes) Climate change
HUMANITY	Stock market Flu outbreaks
INDIVIDUAL PEOPLE	Speech recognition Machine Translation (e.g., English -> French) ^{CS109B, PROTOPAPAS, GLICKMAN, TANNER}

Background

Much of our data is inherently sequential

PREDICTING EARTHQUAKES





Background

Much of our data is inherently sequential





Background

Much of our data is inherently sequential

SPEECH RECOGNITION

"What is the weather today?"

"What is the weather two day?"

"What is the whether too day?"

"What is, the Wrether to Dae?"





Sequence Modeling: Handwritten Text

Winter is here. Go to the store and buy some snow shovels. Winter is here. Go to the store and buy some snow shovels.

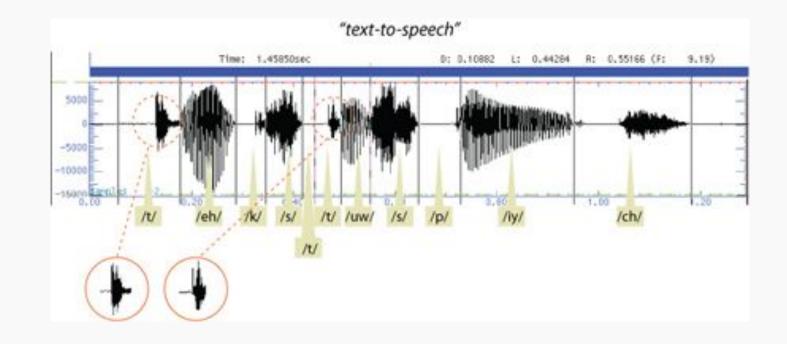
- Input : Image
- Output: Text

https://towardsdatascience.com/build-a-handwritten-text-recognition-system-using-tensorflow-2326a3487c



<u>d5</u>

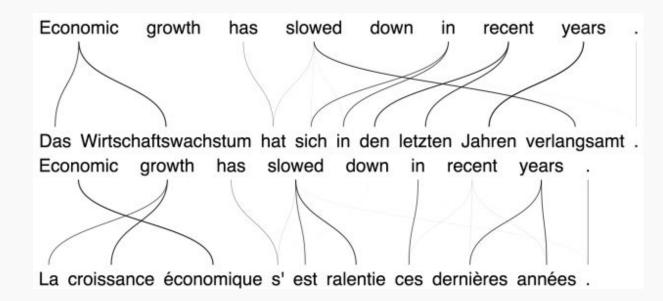
Sequence Modeling: Text-to-Speech



- Input : Audio
- Output: Text



Sequence Modeling: Machine Translation



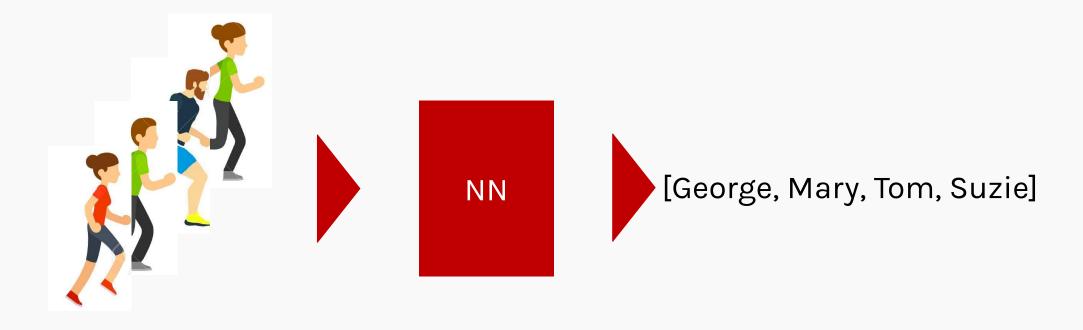
- Input : Text
- Output: Translated
 Text



Why RNNs **Main Concept of RNNs (part 1)** More Details of RNNs RNN training Gated RNN



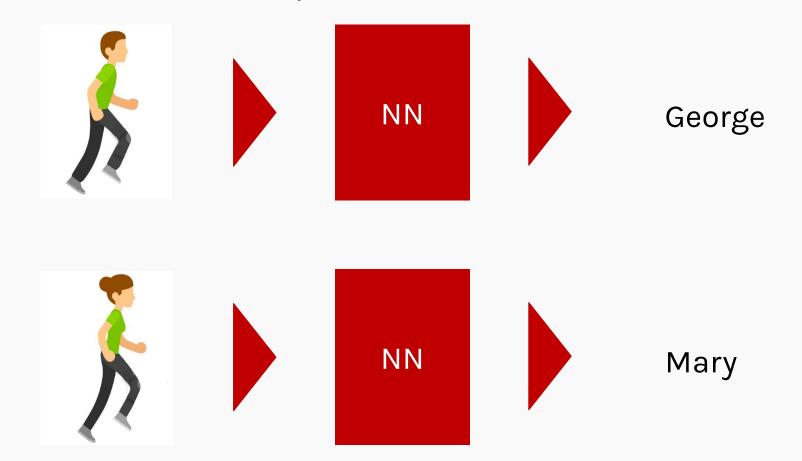
Training: Present to the NN examples and learn from them.





What can my NN do?

Prediction: Given an example



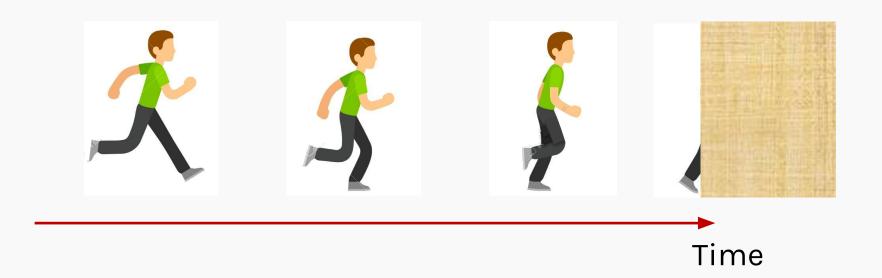


What my NN can NOT do?



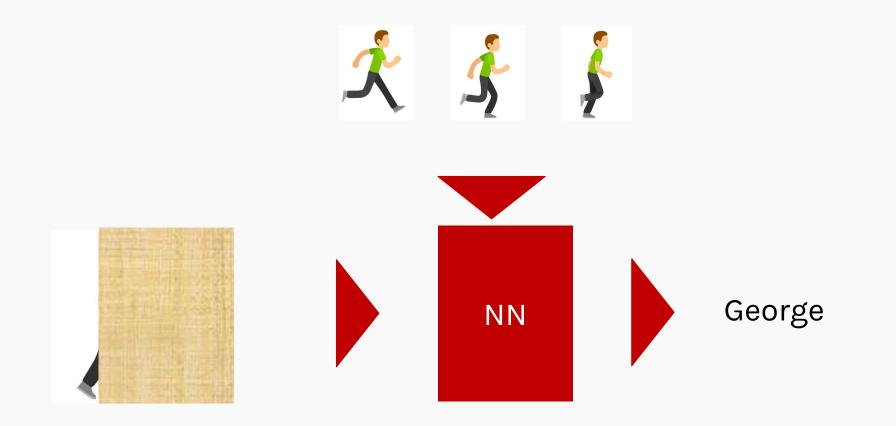


Learn from previous examples

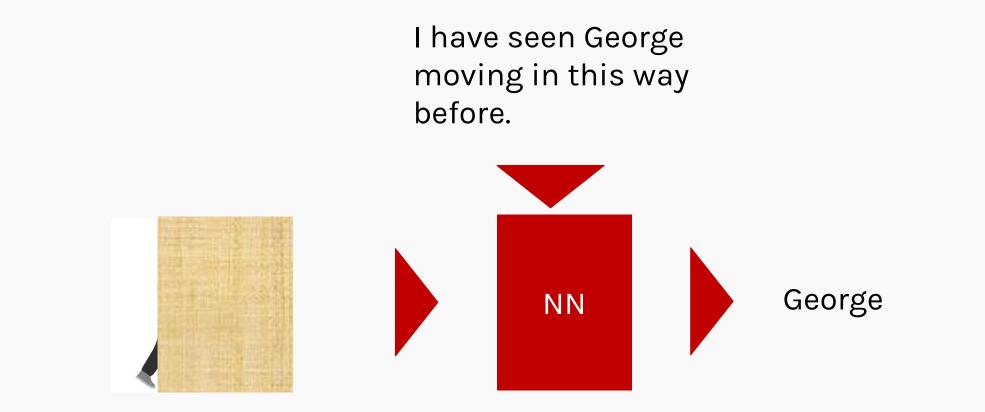




Recurrent Neural Network (RNN)







RNNs recognize the data's sequential characteristics and use patterns to predict the next likely scenario.



Recurrent Neural Network (RNN)



Our model requires context - or contextual information - to understand the subject (he) and the direct object (it) in the sentence.



Hellen: Nice sweater Joe.
Joe: Thanks, Hellen. It used to belong to my brother and he told me I could have it.

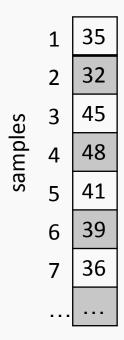


After providing sequential information, the model understood the subject (Joe's brother) and the direct object (sweater) in the sentence.



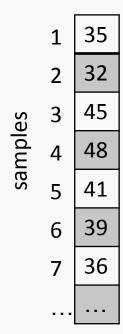
- We want a machine learning model to understand sequences, not isolated samples.
- Can MLP do this?
- Assume we have a sequence of temperature measurements and we want to take 3 sequential measurements and predict the next one

features

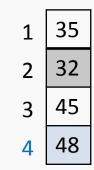




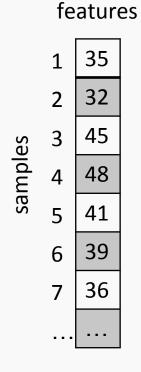
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features



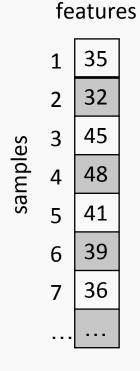
- We want a machine learning model to understand sequences, not isolated samples.
- Can MLP do this?
- Assume we have a sequence of temperature measurements and we want to take 3 sequential measurements and predict the next one



1	35	2	32
2	32	3	45
3	45	4	48
4	48	5	41



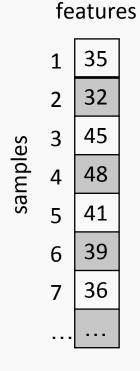
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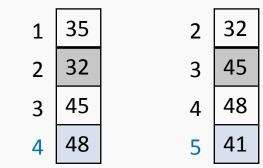


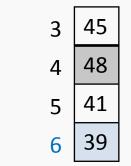
1	3
2	3
3	4
4	48

5	2	32
2	3	45
.5	4	48
.8	5	41

- We want a machine learning model to understand sequences, not isolated samples.
- Can MLP do this?
- Assume we have a sequence of temperature measurements and we want to take 3 sequential measurements and predict the next one



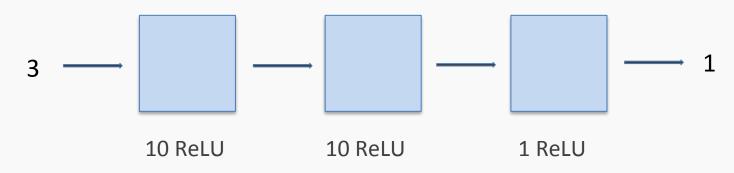




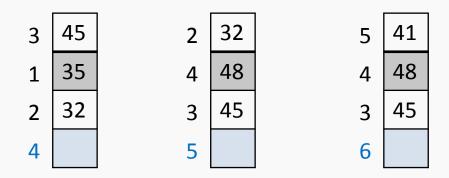


This is called **overlapping windowed** dataset, since we're windowing observations to create new.

We can easily do using a MLS:



But re-arranging the order of the inputs like:





will produce the same results

- 1. MLPs/CNNs require fixed input and output size
- 2. MLPs/CNNs can't classify inputs in multiple places



What follows after: 'I got in the car and'?

drove away

What follows after: 'In car the and I'?

Not obvious it should be 'drove away'

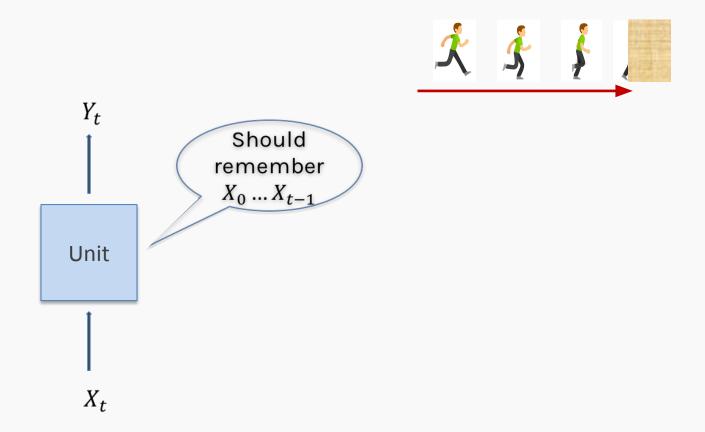
The order of words matters. This is true for most sequential data. A fully connected network will not distinguish the order and therefore missing some information.



Why RNNs **Main Concept of RNNs** More Details of RNNs RNN training Gated RNN

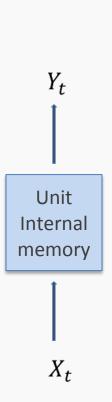


Somehow the computational unit should remember what it has seen before.





Somehow the computational unit should remember what it has seen before.





Somehow the computational unit should remember what it has seen before. We'll call the information the unit's **state**.







Memory

In neural networks, once training is over, the weights do not change. This means that the network is done learning and done changing.

Then, we feed in values, and it simply applies the operations that make up the network, using the values it has learned.

But the RNN units can remember new information after training has completed.

That is, they're able to keep changing after training is over.



Question: How can we do this? How can build a unit that remembers the past?

The memory or **state** can be written to a file but in RNNs, we keep it inside the recurrent unit.

In an array or in a vector!

Work with an example:

Anna Sofia said her shoes are too ugly. Her here means Anna Sofia.

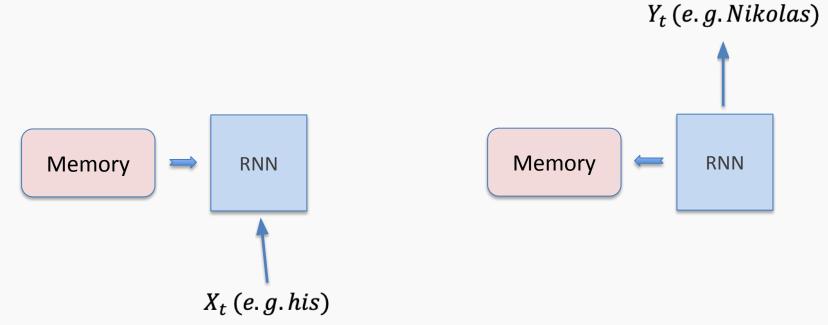
Nikolas put his keys on the table. His here means Nikolas



Question: How can we do this? How can build a unit that remembers the past?

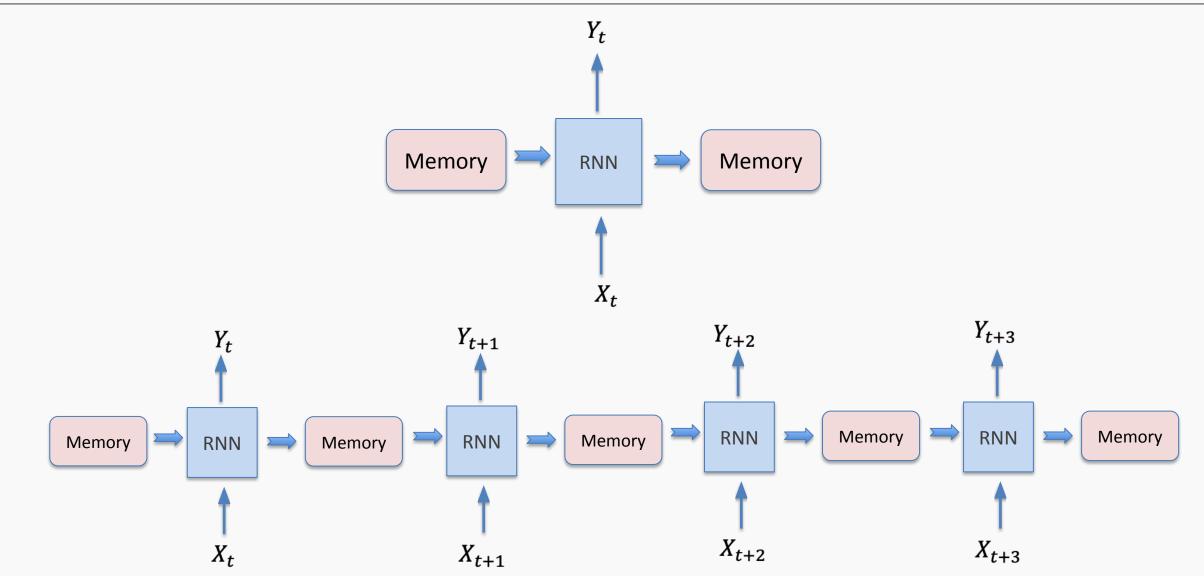
The memory or **state** can be written to a file but in RNNs, we keep it inside the recurrent unit.

In an array or in a vector!





Building an RNN

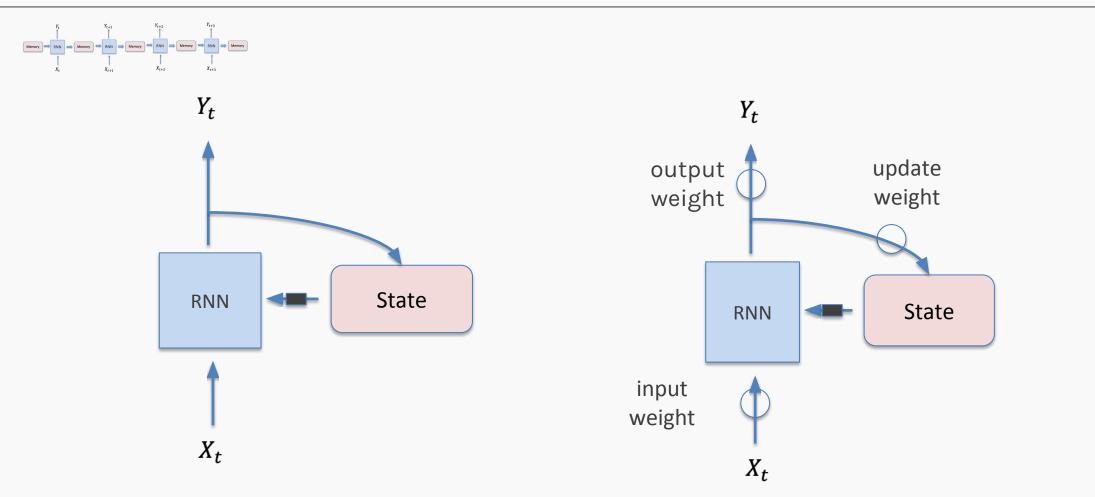




Why RNNs Main Concept of RNNs **More Details of RNNs** RNN training Gated RNN

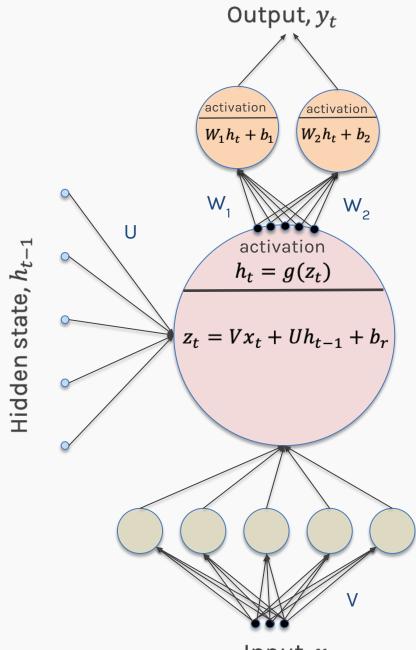


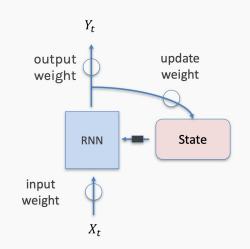
Structure of an RNN cell





Anatomy of an RNN unit





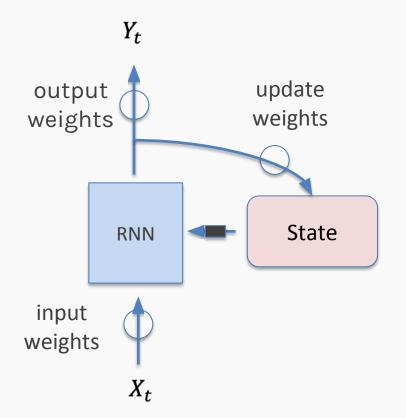


Input, *x*_{*t*} CS109B, Protopapas, Glickman, Tanner Why RNNs Main Concept of RNNs More Details of RNNs **RNN training** Gated RNN

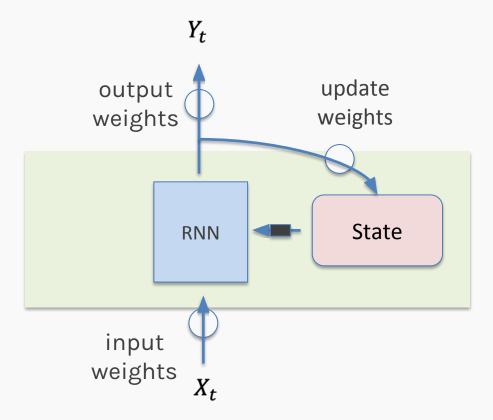


- For each input, unfold network for the sequence length T
- Back-propagation: apply forward and backward pass on unfolded network
- Memory cost: O(T)

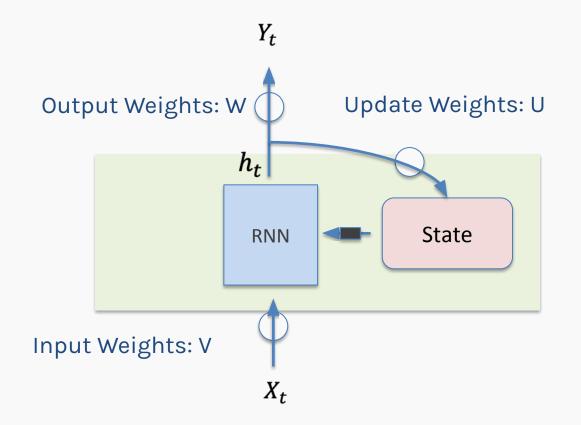




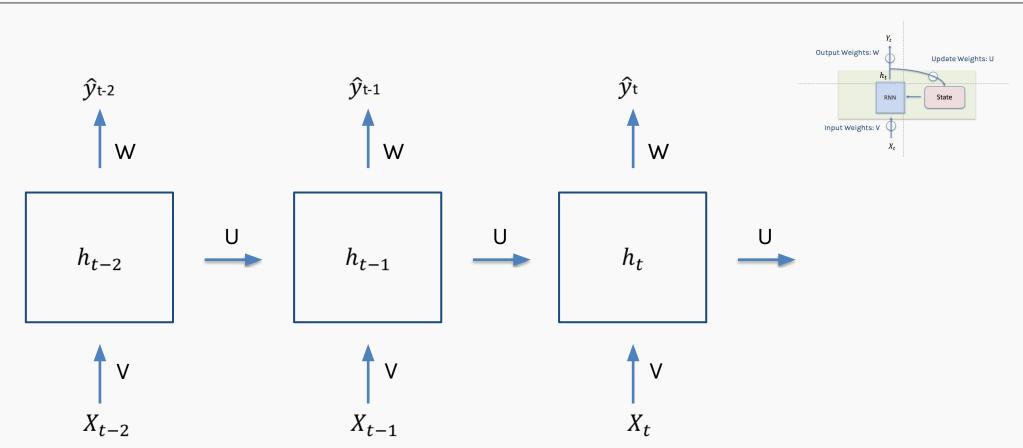








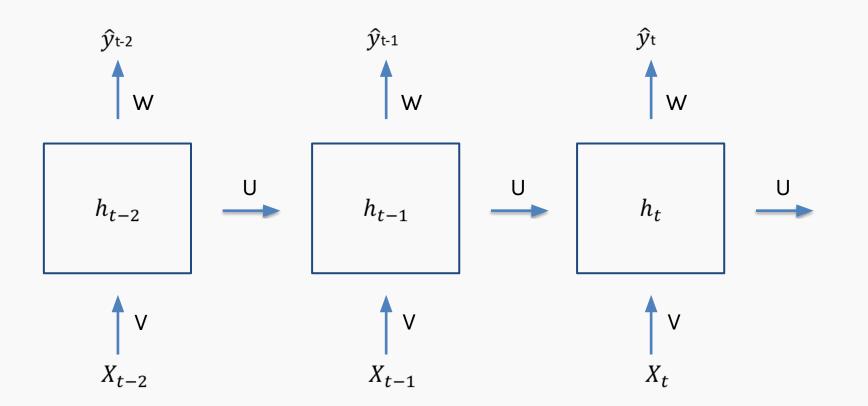




You have two activation functions g_h which serves as the activation for the hidden state and g_y which is the activation of the output. In the example shown before g_y was the identity.



CS109B, Protopapas, Glickman, Tanner



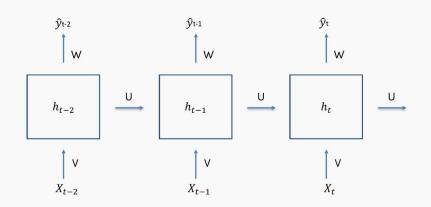


$$\hat{y}_t = g_y(Wh_t + b)$$

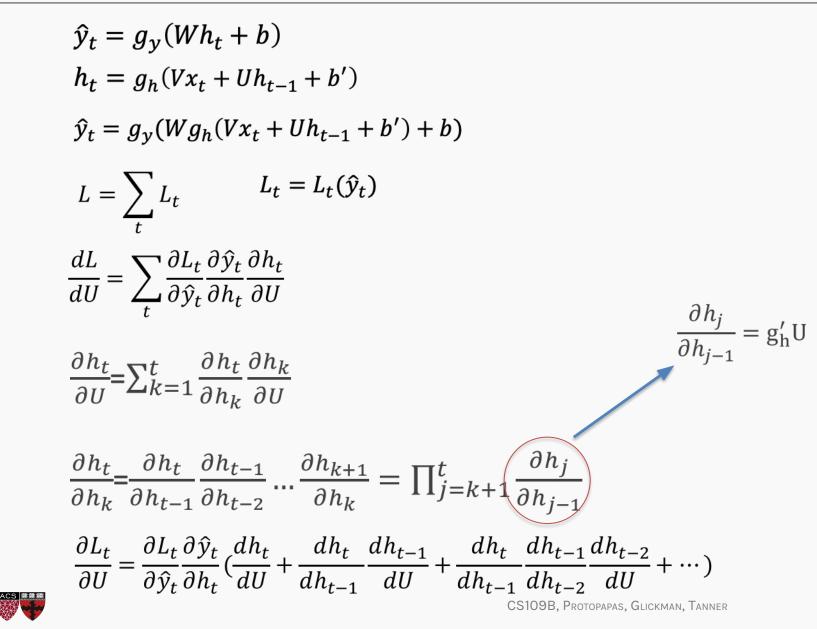
$$L = \sum_{t} L_t \qquad \qquad L_t = L_t(\hat{y}_t)$$

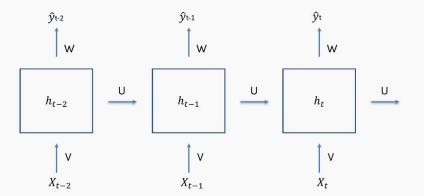
$$\frac{dL}{dW} = \sum_{t} \frac{dL_t}{dW} = \sum_{t} \frac{\partial L_t}{\partial \hat{y}_t} \frac{\partial \hat{y}_t}{\partial W}$$

$$\frac{\partial \hat{y}_t}{\partial W} = g_y' h_t$$



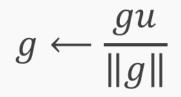






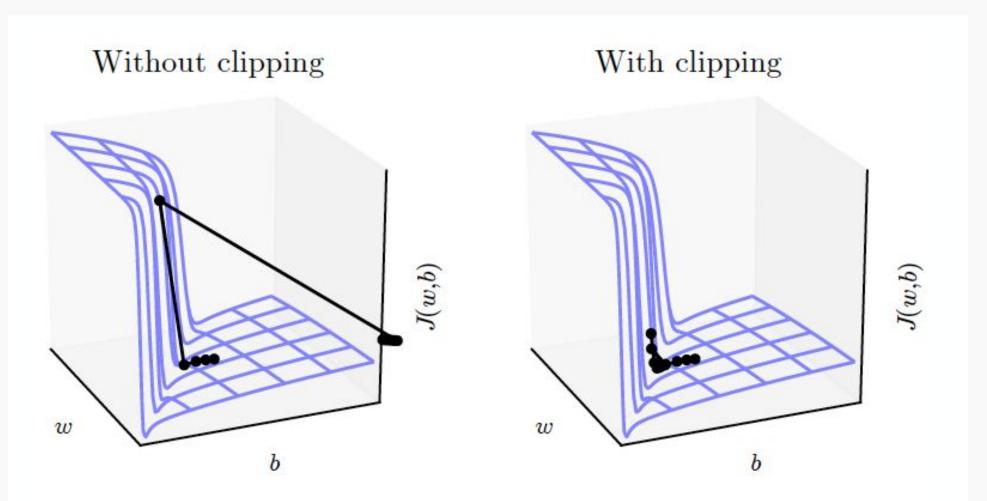
Prevents exploding gradients Clip the norm of gradient before update. For some derivative *g*, and some threshold *u*

 $\text{if } \|g\| > u$





Gradient Clipping





Why RNNs Main Concept of RNNs More Details of RNNs RNN training Gated RNN



Unfolded networks can be very deep

Long-term interactions are given exponentially smaller weights than small-term interactions

Gradients tend to either vanish or explode

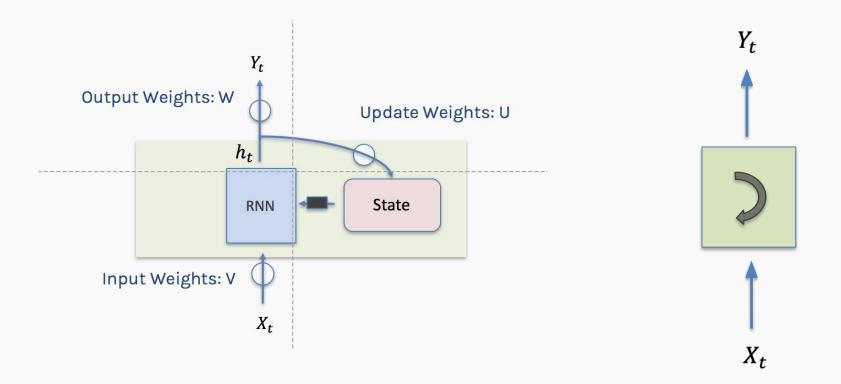


Handles long-term dependencies

- Leaky units where weight on self-loop α is context-dependent
- Allow network to decide whether to accumulate or forget past info

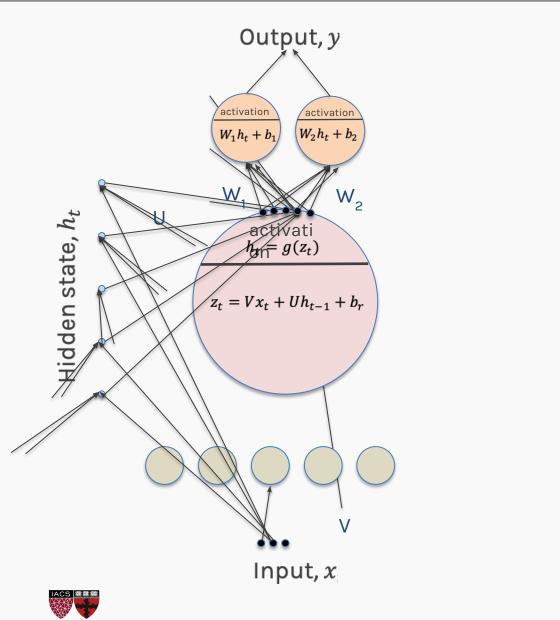


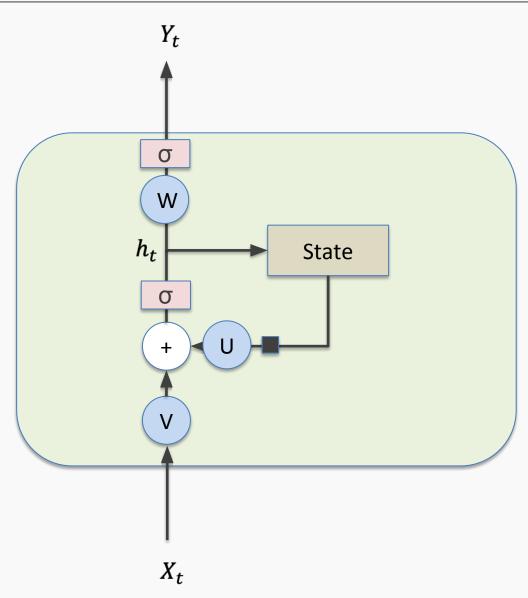
Using conventional and convenient notation





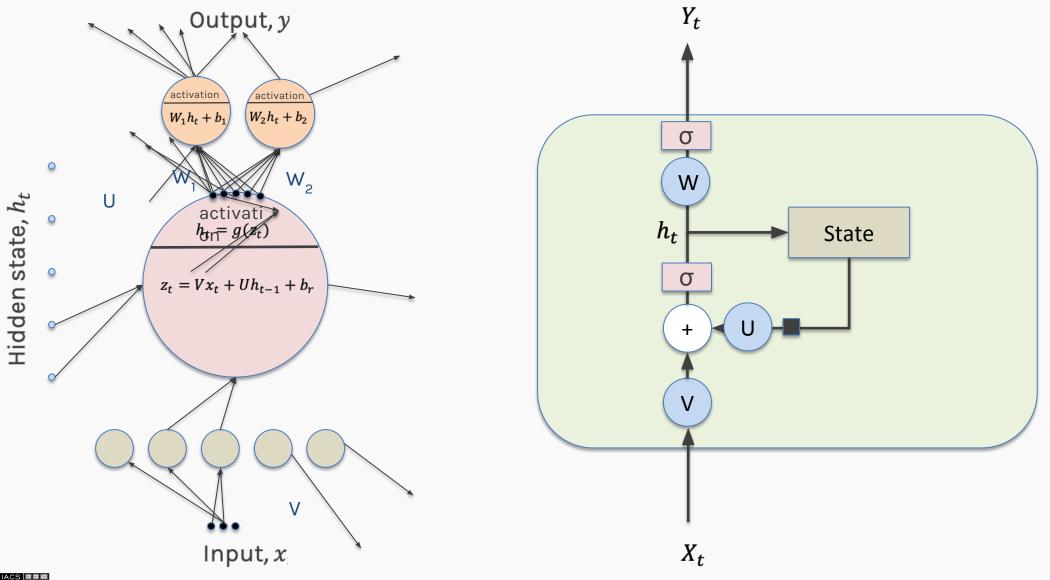
Simple RNN again





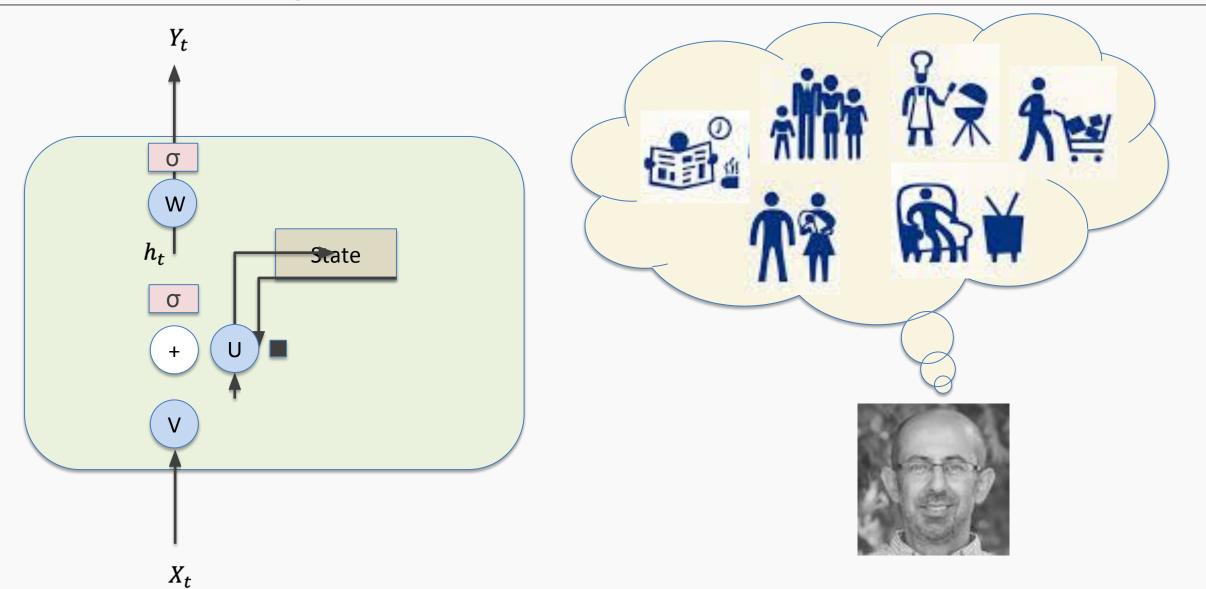
55

Simple RNN again





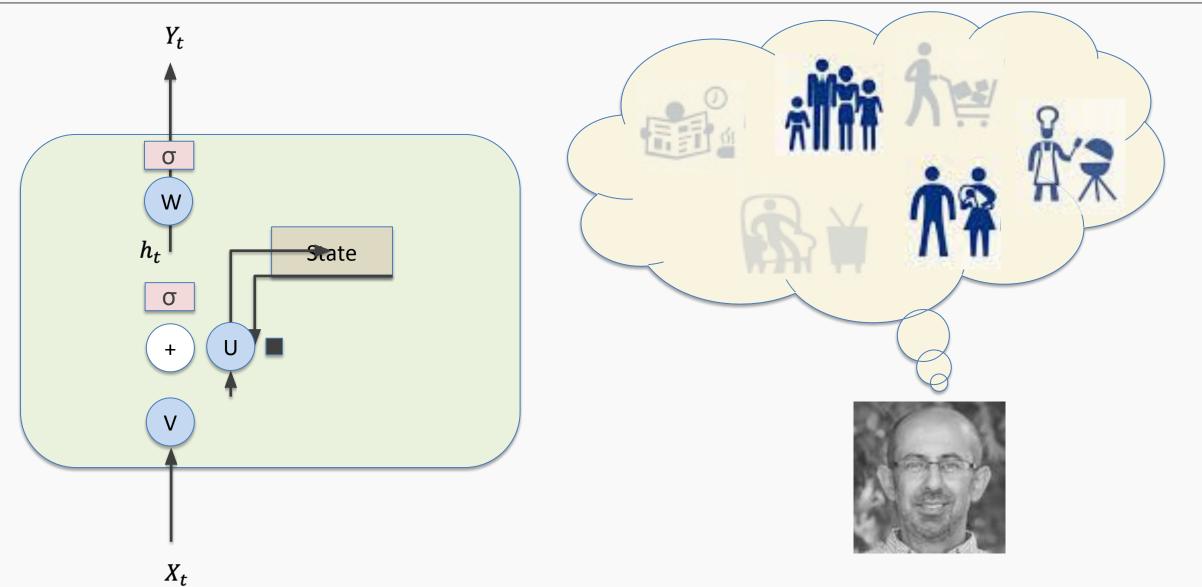
Simple RNN again: Memories





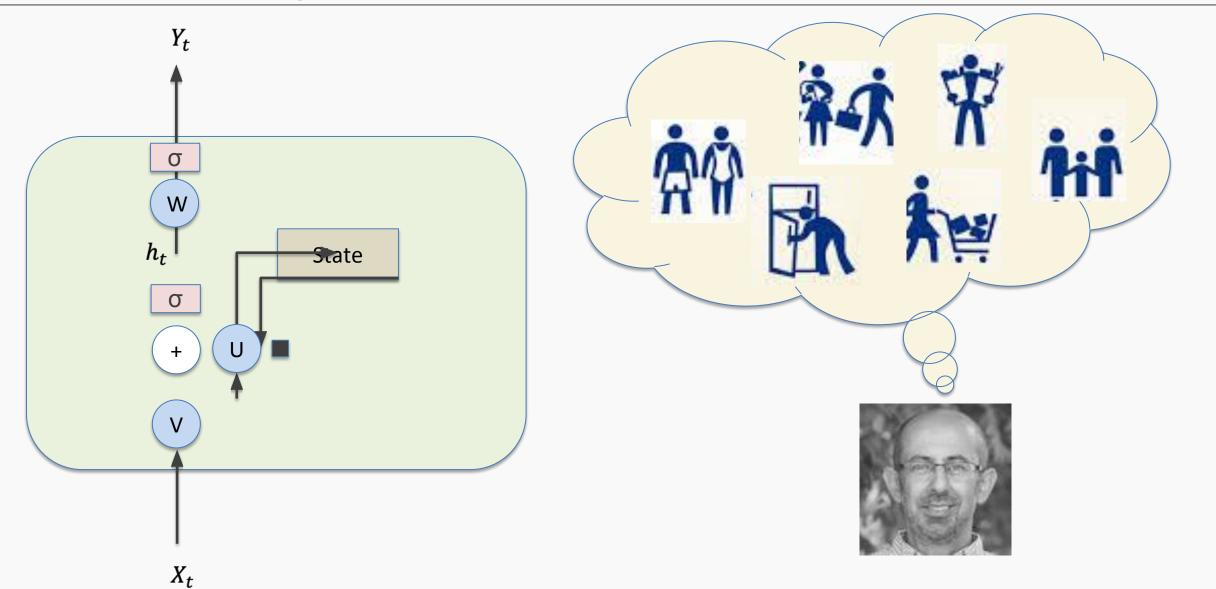
CS109B, Protopapas, Glickman, Tanner

Simple RNN again: Memories - Forgetting





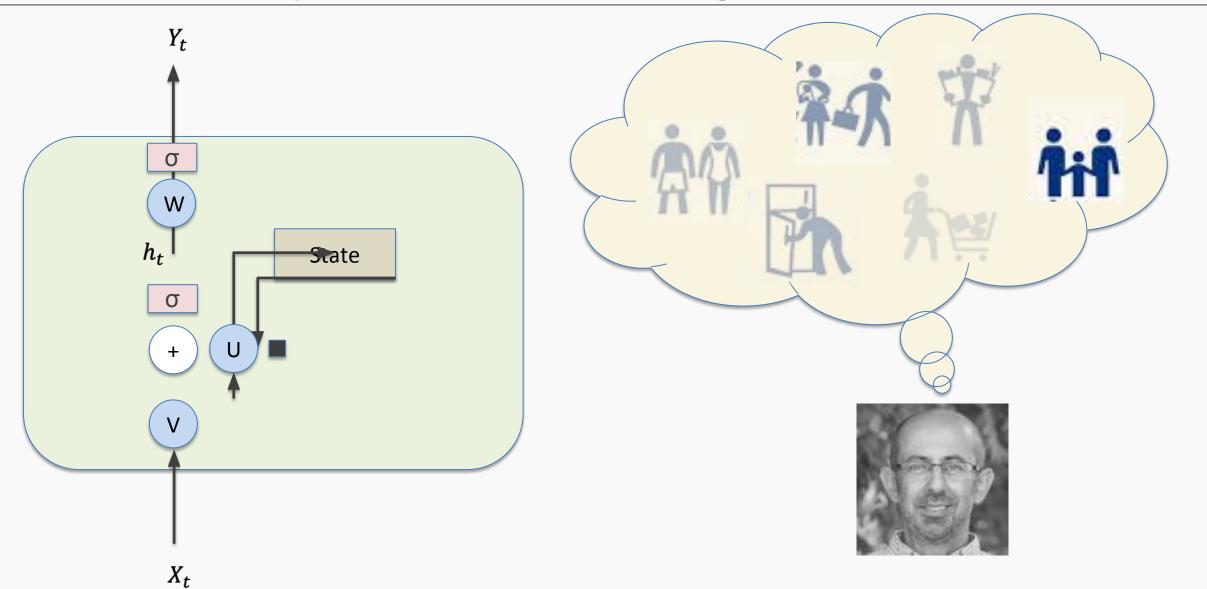
Simple RNN again: New Events





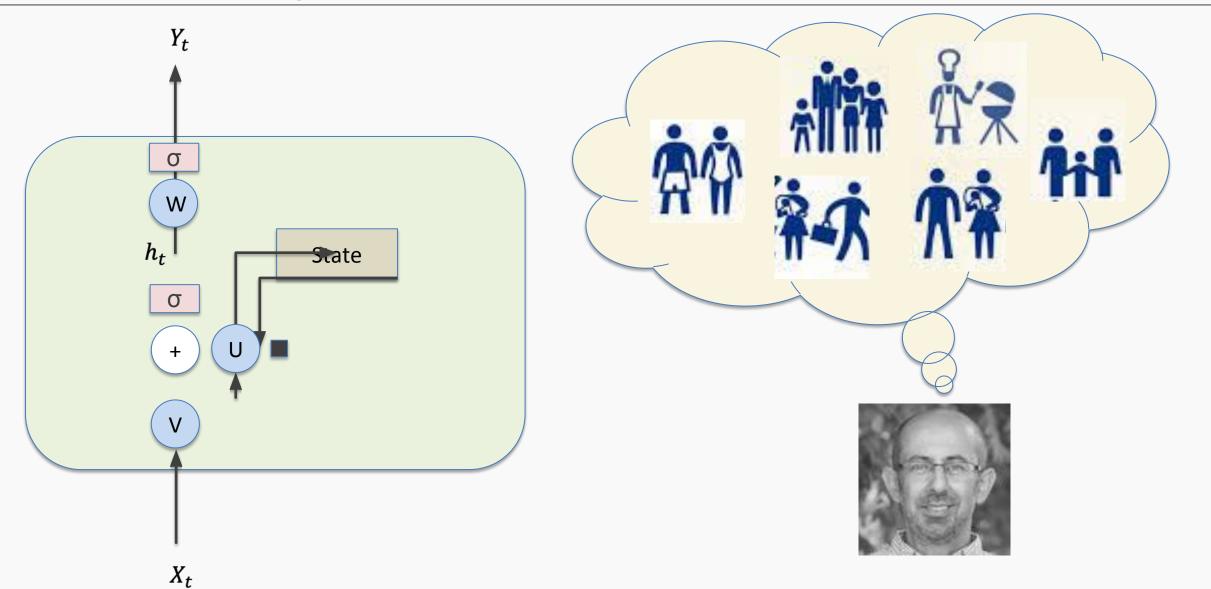
CS109B, Protopapas, Glickman, Tanner

Simple RNN again: New Events Weighted





Simple RNN again: Updated memories





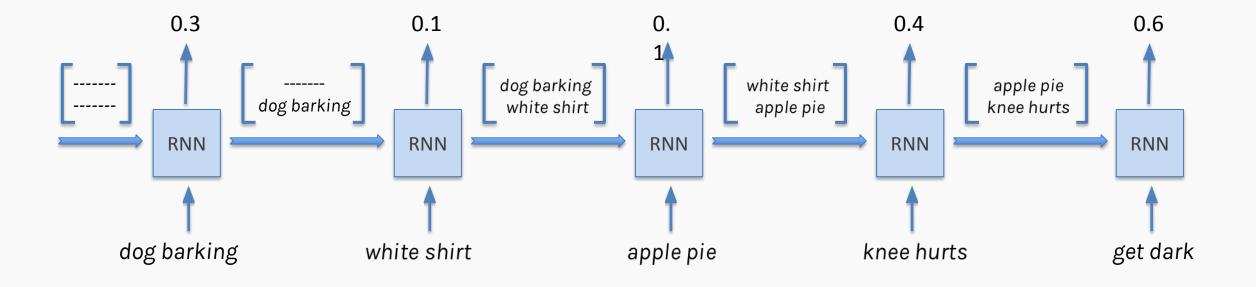
- [Chen17b] Qiming Chen, Ren Wu, "CNN Is All You Need", arXiv 1712.09662, 2017. <u>https://arxiv.org/abs/1712.09662</u>
- [Chu17] Hang Chu, Raquel Urtasun, Sanja Fidler, "Song From PI: A Musically Plausible Network for Pop Music Generation", arXiv preprint, 2017. <u>https://arxiv.org/abs/1611.03477</u>
- [Johnson17] Daniel Johnson, "Composing Music with Recurrent Neural Networks", Heahedria, 2017. <u>http://www.hexahedria.com/2015/08/03/</u> <u>composing-music-with-recurrent-neural-networks/</u>
- [Deutsch16b] Max Deutsch, "Silicon Valley: A New Episode Written by Al", Deep Writing blog post, 2017. <u>https://medium.com/deep-writing/</u> <u>silicon-valley-a-new-episode-written-by-ai-a8f832645bc2</u>
- [Fan16] Bo Fan, Lijuan Wang, Frank K. Soong, Lei Xie "Photo-Real Talking Head with Deep Bidirectional LSTM", Multimedia Tools and Applications, 75(9), 2016. <u>https://www.microsoft.com/en-us/research/wp-content/uploads/2015/04/icassp20</u> <u>15_fanbo_1009.pdf</u>



Continue on Wednesday

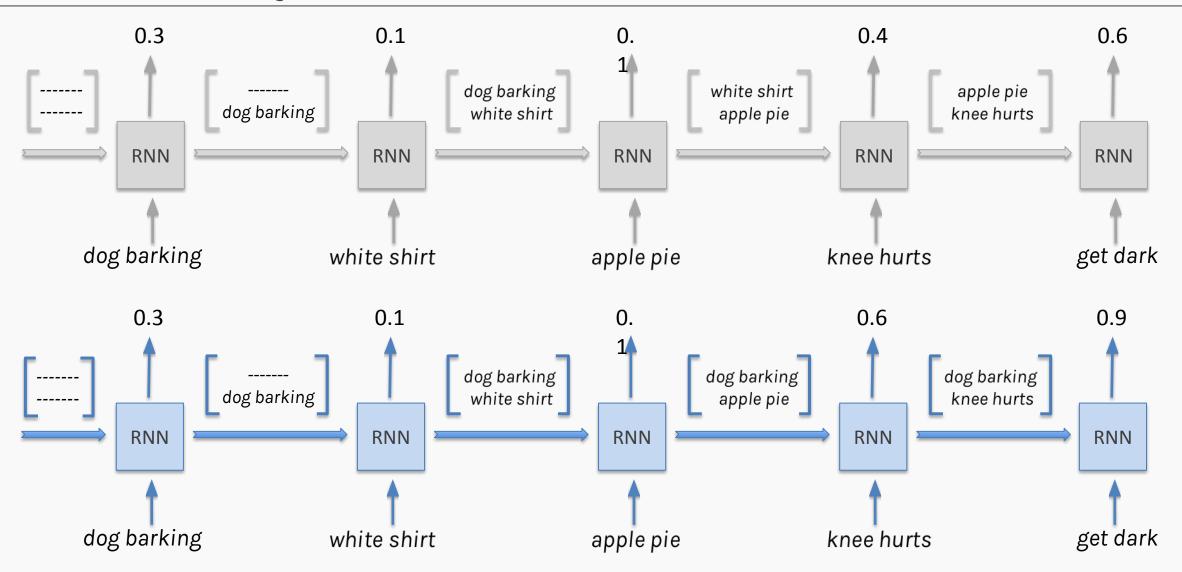


Is it raining? We build an RNN to the probability if it is raining:



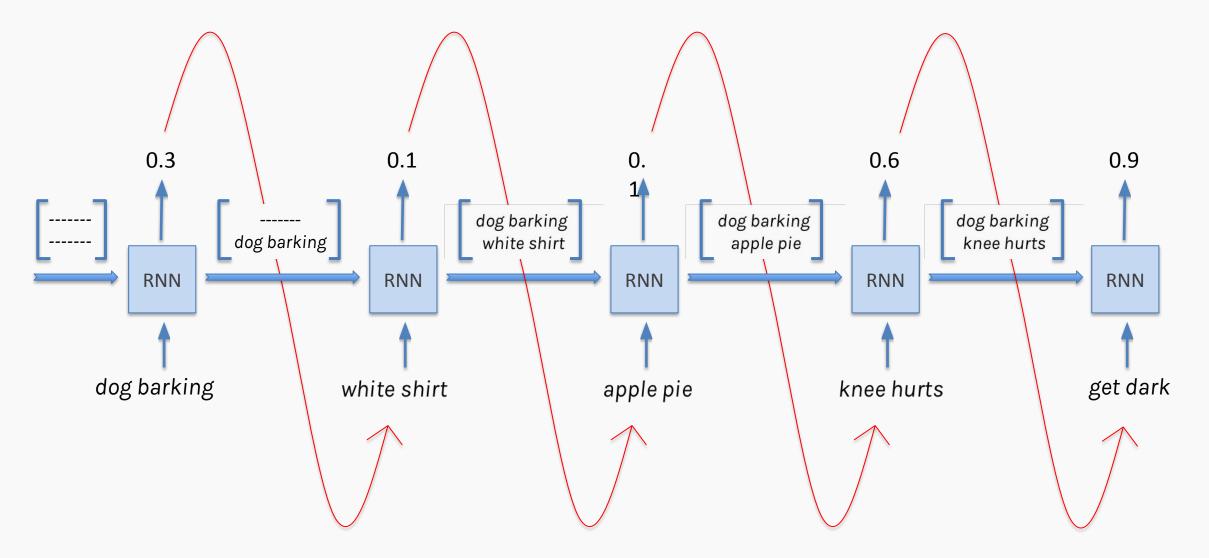


RNN + Memory



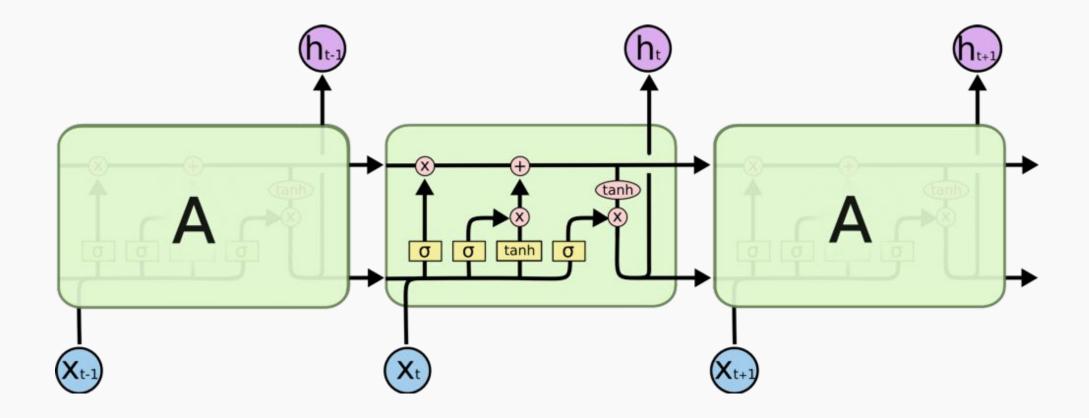


RNN + Memory + Output



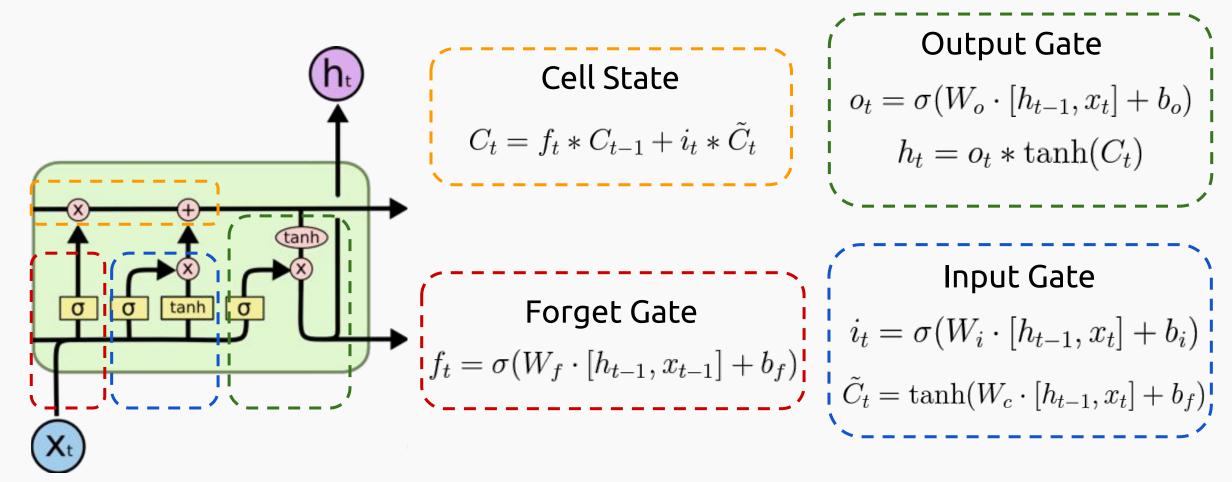


LSTM: Long short term memory



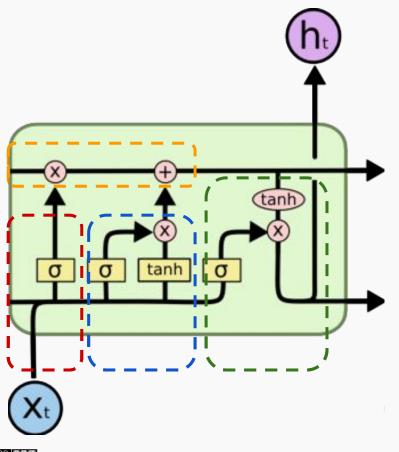


Before to really understand LSTM lets see the big picture ...





Before to really understand LSTM lets see the big picture ...



- LSTM are recurrent neural network with a cell and a hidden state, boths of these are updated in each step and can be thought as memories.
- Cell states work as a long term memory and the updates depends on the relation between the hidden state in t -1 and the input.
- 3. The hidden state of the next step is a transformation of the cell state and the output (which is the section that is in general used to calculate our loss, ie information that we want in a short memory).



Let's think about my cell state

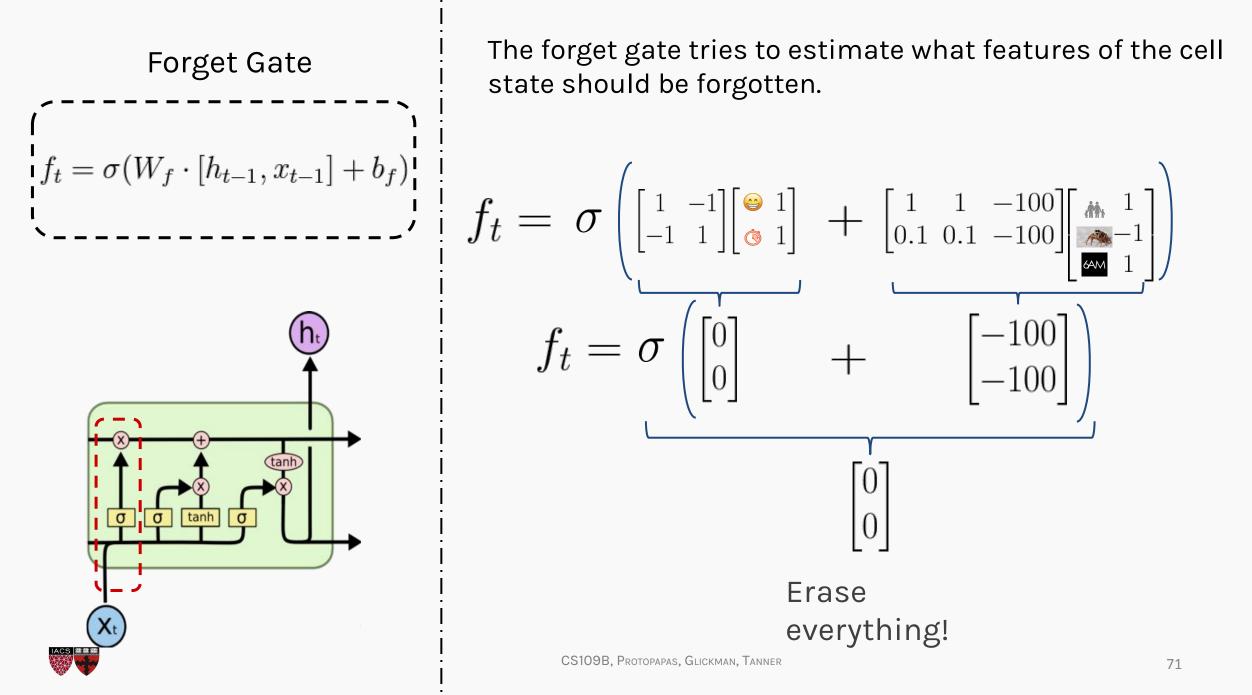
 x_t =

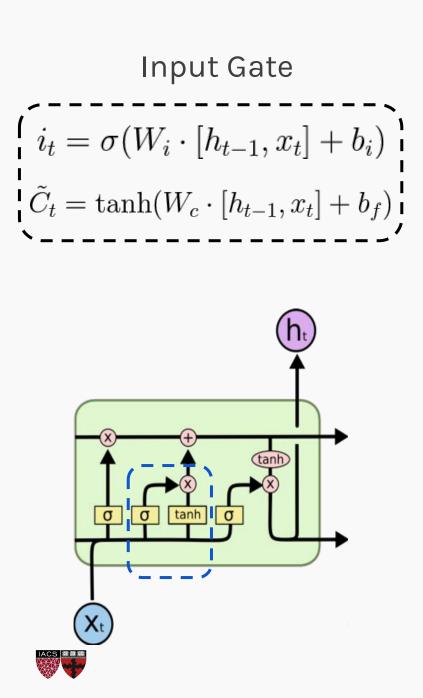
Let's predict if i will help you in the homework in time t



CS109B, Protopapas, Glickman, Tanner

 $\begin{array}{c|c} & & 1 \\ \hline & & \\ \hline & & \\ \hline & & \\ \hline & & \\ 1 \end{array} \end{array} \begin{array}{c} h_{t-1} = \begin{bmatrix} & 1 \\ & 1 \end{bmatrix} \\ h_{t-1} = \begin{bmatrix} & 1 \\ & 1 \end{bmatrix} \\ \hline & & \\ \hline \end{array}$



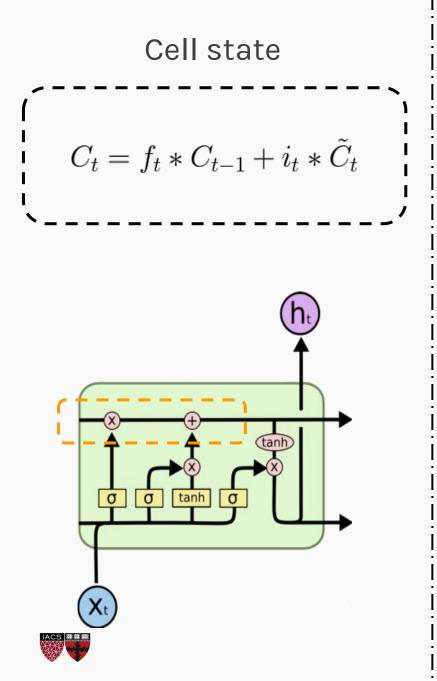


The input gate layer works in a similar way that the forget layer, the input gate layer estimate the degree of confidence of \tilde{C}_t and \tilde{C}_t is a new estimation of the cell state.

Let's say that my input gate estimation is:

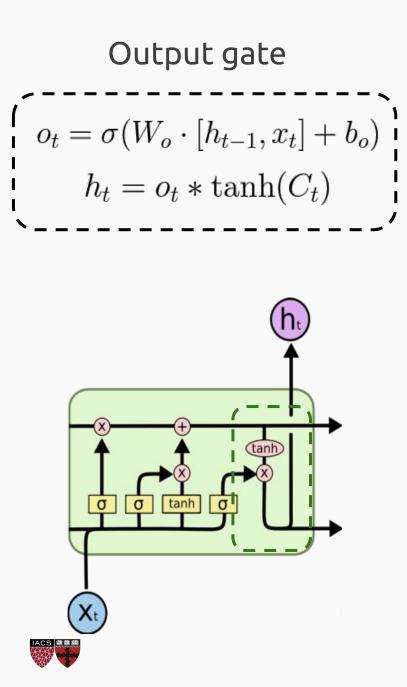
$$i_t = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\tilde{C}_{t} = \tanh\left(\begin{bmatrix}1 & 0\\0 & 1\end{bmatrix}\begin{bmatrix} @ & 1\\0 & 1\end{bmatrix} + \begin{bmatrix}10 & 1 & -1\\-1 & 1 & 10\end{bmatrix}\begin{bmatrix} & 1\\0 & -1\\0 & 1\end{bmatrix}\right)$$
$$\tilde{C}_{t} = \tanh\left(\begin{bmatrix}1\\1\end{bmatrix} + \begin{bmatrix}10\\10\end{bmatrix}\right)$$



After the calculation of forget gate and input gate we can update our cell state.

$$C_{t} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} * \begin{bmatrix} \Theta & 0.7 \\ 0 & 0.3 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} * \begin{bmatrix} \Theta & 1 \\ 0 & 1 \end{bmatrix}$$
$$C_{t} = \begin{bmatrix} \Theta & 1 \\ 0 & 1 \end{bmatrix}$$

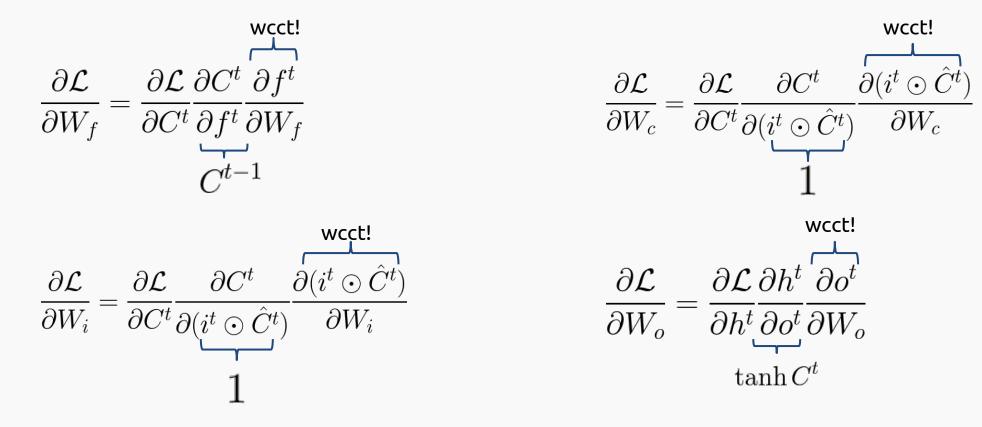


- The output gate layer is calculated using the information of the input x in time t and hidden state of the last step.
 - It is important to notice that hidden state used in the next step is obtained using the output gate layer which is usually the function that we optimize.

$$o_{t} = \sigma \left(\begin{bmatrix} 1 & 1 \end{bmatrix} \begin{bmatrix} \bullet & 1 \\ \bullet & 1 \end{bmatrix} + \begin{bmatrix} 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} \bullet & 1 \\ \bullet & -1 \end{bmatrix} \right)$$
$$o_{t} \approx 0.9$$
$$h_{t} \approx 0.9 * \begin{bmatrix} \bullet & 1 \\ \bullet & 1 \end{bmatrix} = \begin{bmatrix} \bullet & 0.9 \\ \bullet & 0.9 \end{bmatrix}$$

To optimize my parameters i basically need to do: Let's calculate all the derivatives in some time t!

$$W = W - \eta \frac{\partial \mathcal{L}}{\partial W}$$



So... every derivative is wrt the cell state or the hidden state

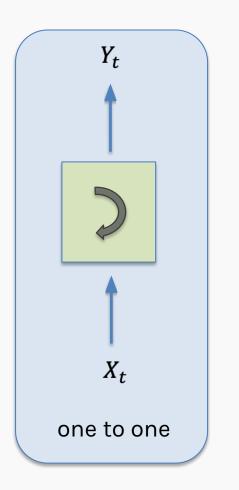
Let's calculate the cell state and the hidden state

$$\frac{\partial \mathcal{L}}{\partial h^{t-1}} = \frac{\partial \mathcal{L}}{\partial C^t} \left(\frac{\partial C^t}{\partial f^t} \frac{\partial f^t}{\partial h^t} + \frac{\partial C^t}{\partial (i^t \odot \hat{C}^t)} \frac{\partial (i^t \odot \hat{C}^t)}{\partial h^t} \right) + \frac{\partial \mathcal{L}}{\partial h^t} \frac{\partial h^t}{\partial o^t} \frac{\partial o^t}{\partial h^{t-1}}$$

$$\begin{split} \frac{\partial \mathcal{L}}{\partial C^{t}} &= \frac{\partial \mathcal{L}}{\frac{\partial (f^{t+1} \odot C^{t} + i^{t+1} \odot \hat{C}^{t})}{Q(f^{t+1} \odot C^{t} + i^{t+1} \odot \hat{C}^{t})}} \underbrace{\frac{\partial (f^{t+1} \odot C^{t} + i^{t+1} \odot \hat{C}^{t})}{QC^{t}}}_{\left(\frac{\partial \mathcal{L}}{\partial C^{t+1}} + \frac{\partial \mathcal{L}}{\partial h^{t+1}} \frac{\partial h^{t+1}}{QC^{t+1}}\right) \odot f^{t+1}} \end{split}$$

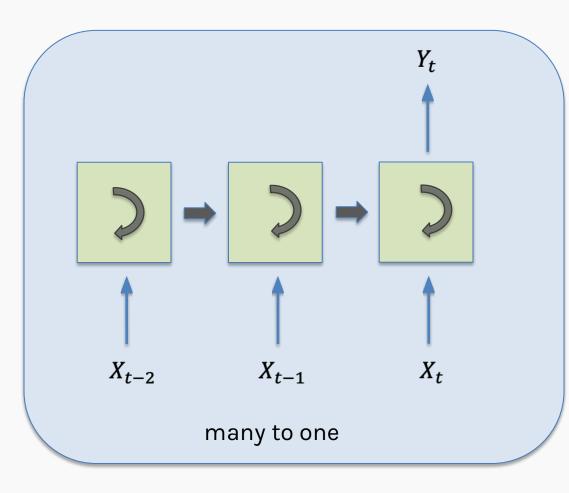


RNN Structures



- The one to one structure is useless.
- It takes a single input and it produces a single output.
- Not useful because the RNN cell is making little use of its unique ability to remember things about its input sequence

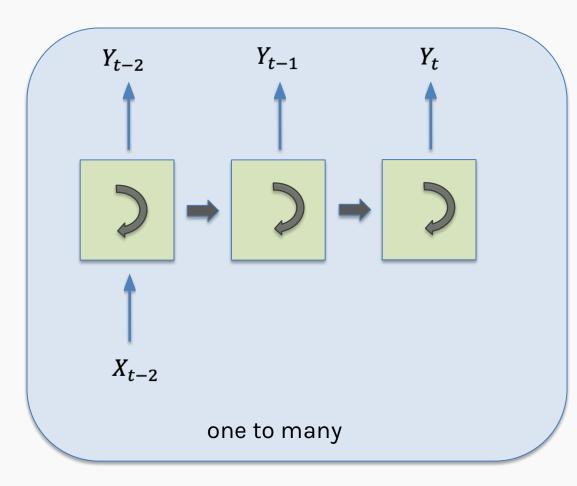




The many to one structure reads in a sequence and gives us back a single value. Example: Sentiment analysis, where the network is given a piece of text and then reports on some quality inherent in the writing. A common example is to look at a movie review and determine if it was positive or negative.



RNN Structures (cont)

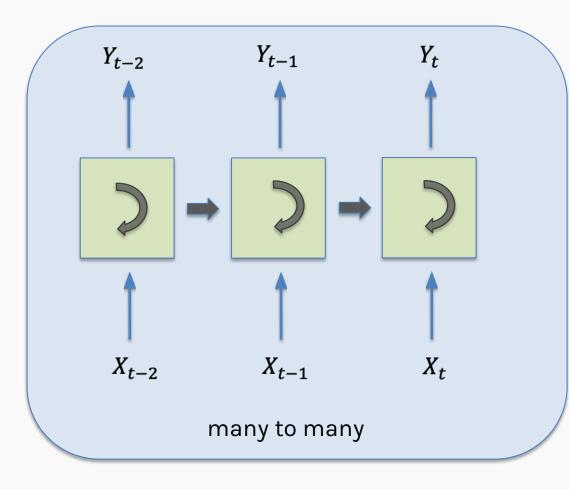


The **one to many** takes in a single piece of data and produces a sequence.

For example we give it the starting note for a song, and the network produces the rest of the melody for us.

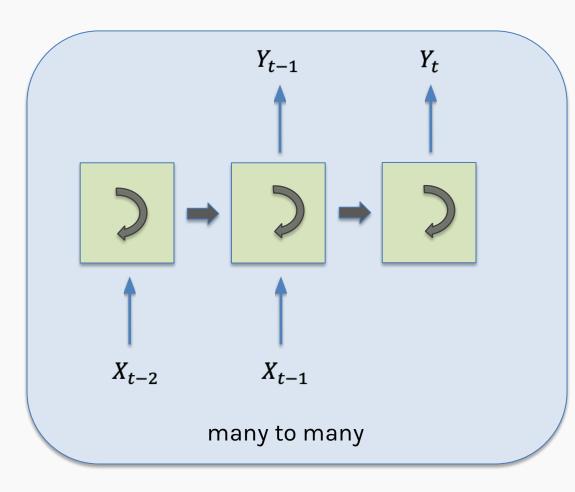


RNN Structures (cont)



The **many to many** structures are in some ways the most interesting. used for machine translation. Example: Predict if it will rain given some inputs.





This form of **many to many** can be used for machine translation.

For example, the English sentence: **"The black dog jumped over the cat"** In Italian as: "Il cane nero saltò sopra il gatto" In the Italia, the adjective "nero" (black) follows the noun "cane" (dog), so we need to have some kind of buffer so we can produce the words in their proper English.



LSTM and RNN are designed to analyze sequence of values.

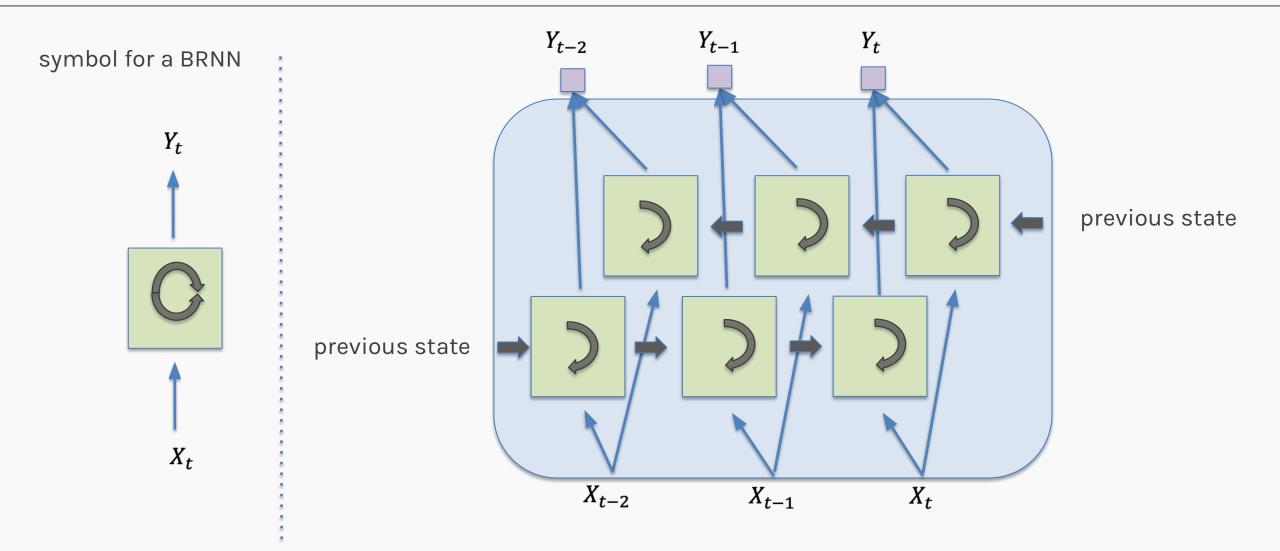
For example: Patrick said he needs a vacation. he here means Patrick and we know this because Patrick was before the word he.

However consider the following sentence: He needs to work more, Pavlos said about Patrick.

Bidirectional RNN or BRNN or bidirectional LSTM or BLSTM when using LSTM units.



Bidirectional (cond)



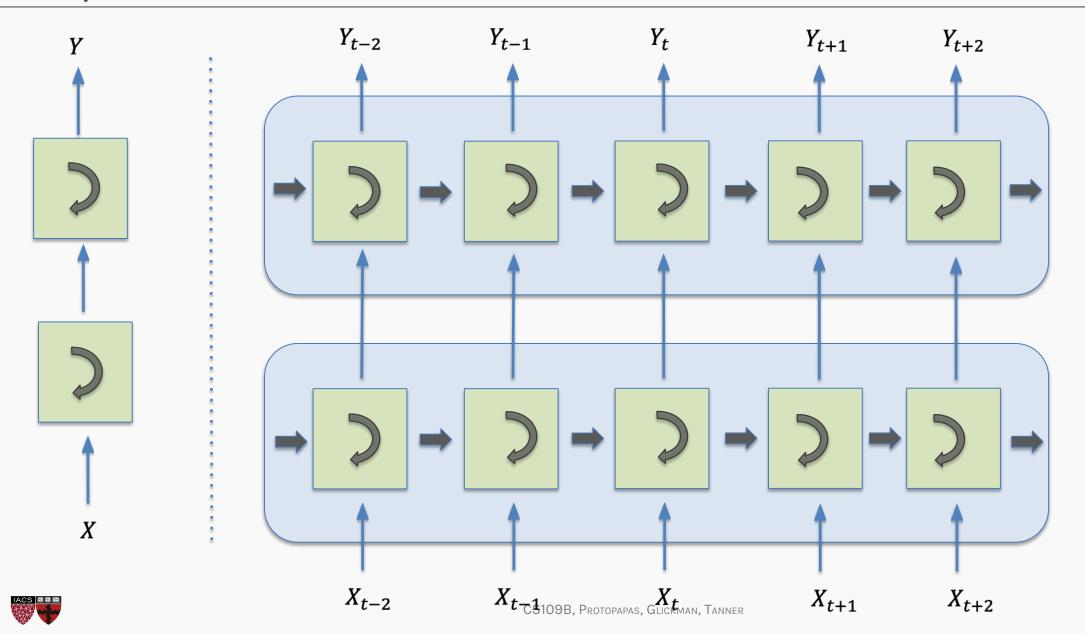


LSTM units can be arranged in layers, so that each the output of each unit is the input to the other units. This is called **a deep RNN**, where the adjective "deep" refers to these multiple layers.

- Each layer feeds the LSTM on the next layer
- First time step of a feature is fed to the first LSTM, which processes that data and produces an output (and a new state for itself).
- That output is fed to the next LSTM, which does the same thing, and the next, and so on.
- Then the second time step arrives at the first LSTM, and the process repeats.

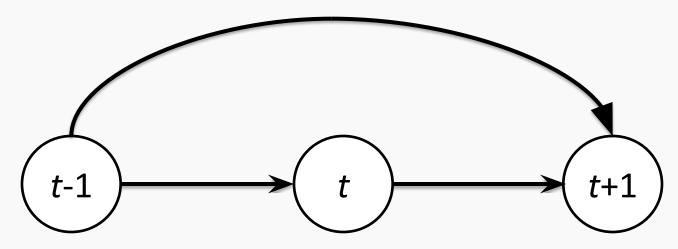


Deep RNN



85

Add additional connections between units *d* time steps apart Creating paths through time where gradients neither vanish or explode





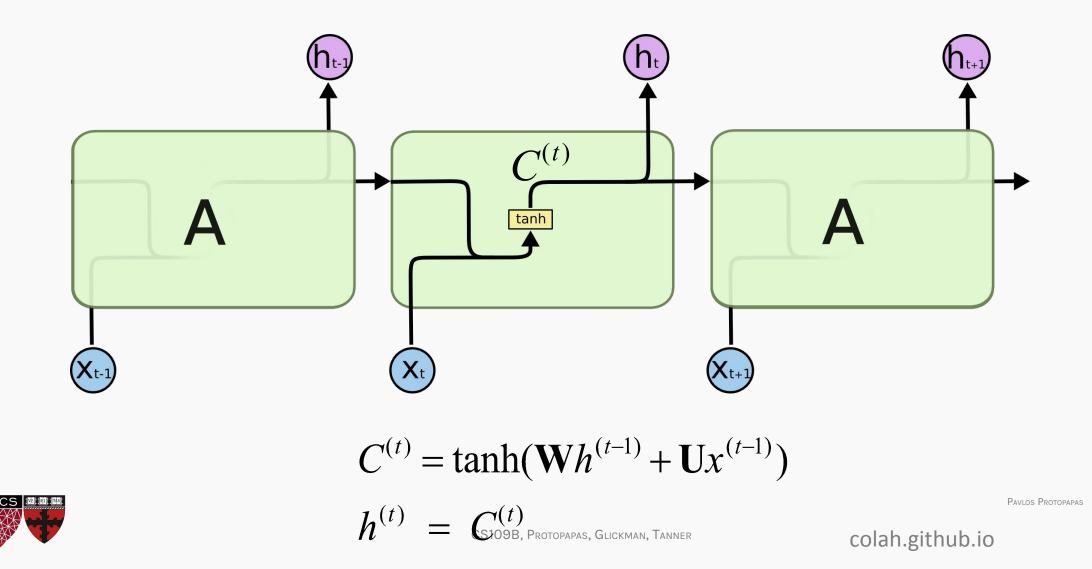
CS109B, PROTOPAPAS, GLICKMAN, TANNER

Linear self-connections

Maintain cell state: running average of past hidden activations



Standard RNN



Leaky Unit

