

# The Roadmap:

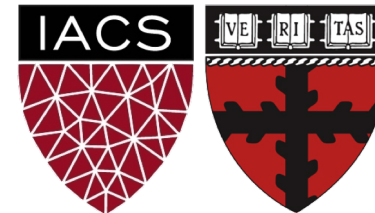
a recap of where we've been, where we're heading, and how it's all related

---







**Harvard IACS**

CS109B

Chris Tanner, Pavlos Protopapas, Mark Glickman



# Learning Objectives

-  Recap models from **CS109A** and **CS109B**
-  Understand the different categories of models
-  Discern similarities/differences between models
-  Feel comfortable choosing which model to use
-  Understand the limitations of our models thus far
-  Feel prepared tackling the remaining course content

# Data Science World

- ▶▶ 1 player
- 2 players
- ▶▶ 226 players

## Your Data $X$

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column

<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68



## Your Data $X$

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column

<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

## Your Data $X$

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column

<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

## Your Data $X$

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column

<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

## Your Data X

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column (e.g. **Temp**)

Age	Play	Rainy	Temp
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column (e.g. **Temp**)
- Let's divide our data and learn how data **X** is related to data **Y**
- Assert that:  $Y = f(X) + \varepsilon$

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column (e.g. **Temp**)
- Let's divide our data and learn how data **X** is related to data **Y**
- Assert that:  $Y = f(X) + \epsilon$
- Want a model  $f$  that is:
  - Supervised

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column (e.g. **Temp**)
- Let's divide our data and learn how data **X** is related to data **Y**
- Assert that:  $Y = f(X) + \epsilon$
- Want a model  $f$  that is:
  - Supervised

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

**Def:**

**Supervised** models use target data, **Y**, to provide feedback so that your model can learn the relationship between **X** and **Y**.

$$Y = f(X)$$

- Supervised

	<b>X</b>		<b>Y</b>
	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
	N	Y	91
	Y	N	89
	N	N	56
	Y	N	71
	N	Y	72
	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68



- Given some data such that each row corresponds to a distinct i.i.d. observation
- You may be interested in a particular column (e.g. **Temp**)
- Let's divide our data and learn how data **X** is related to data **Y**
- Assert that:  $Y = f(X) + \epsilon$
- Want a model  $f$  that is:
  - **Supervised**
  - Predicts real numbers (**regression** model)

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

X

Y

**Def:**

**Regression** models are **supervised**

models, whereby **Y** are *continuous* values.

- Predicts real numbers  
(**regression model**)

**Rainy**

**Temp**

Y

91

N

89

N

56

N

71

Y

72

N

83

Y

97

N

64

21

N

N

68

30

Y

Given some data such that each

**Def:**

**Regression** models are **supervised**

models, whereby **Y** are *continuous* values.

**Classification** models are **supervised**

models, whereby **Y** are *categorical* values.

Predicts real numbers  
(**regression model**)

**X**

**Y**

**Rainy**

**Temp**

Y

91

N

89

N

56

N

71

Y

72

N

83

Y

97

N

64

N

68

21

N

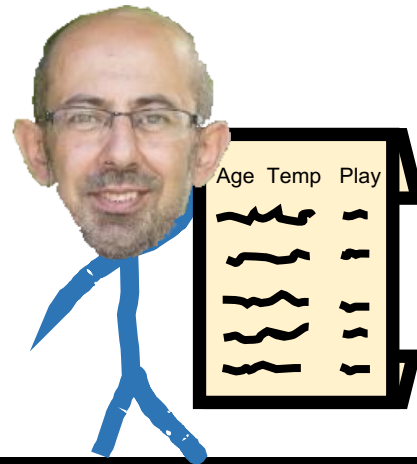
30

Y

- Let's say this is our data
- Want a model that is:
  - **Supervised**
  - Predicts real numbers  
(**regression model**)
- **Q:** What model could we use?

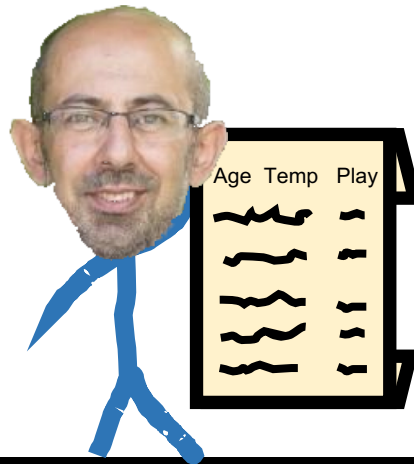
X			Y
Age	Play	Rainy	Temp
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

# Playground of Models



# Playground of Models

Linear  
Regression



Age	Temp	Play
~	~	~
~	~	~
~	~	~
~	~	~
~	~	~



# Linear Regression

**Y**



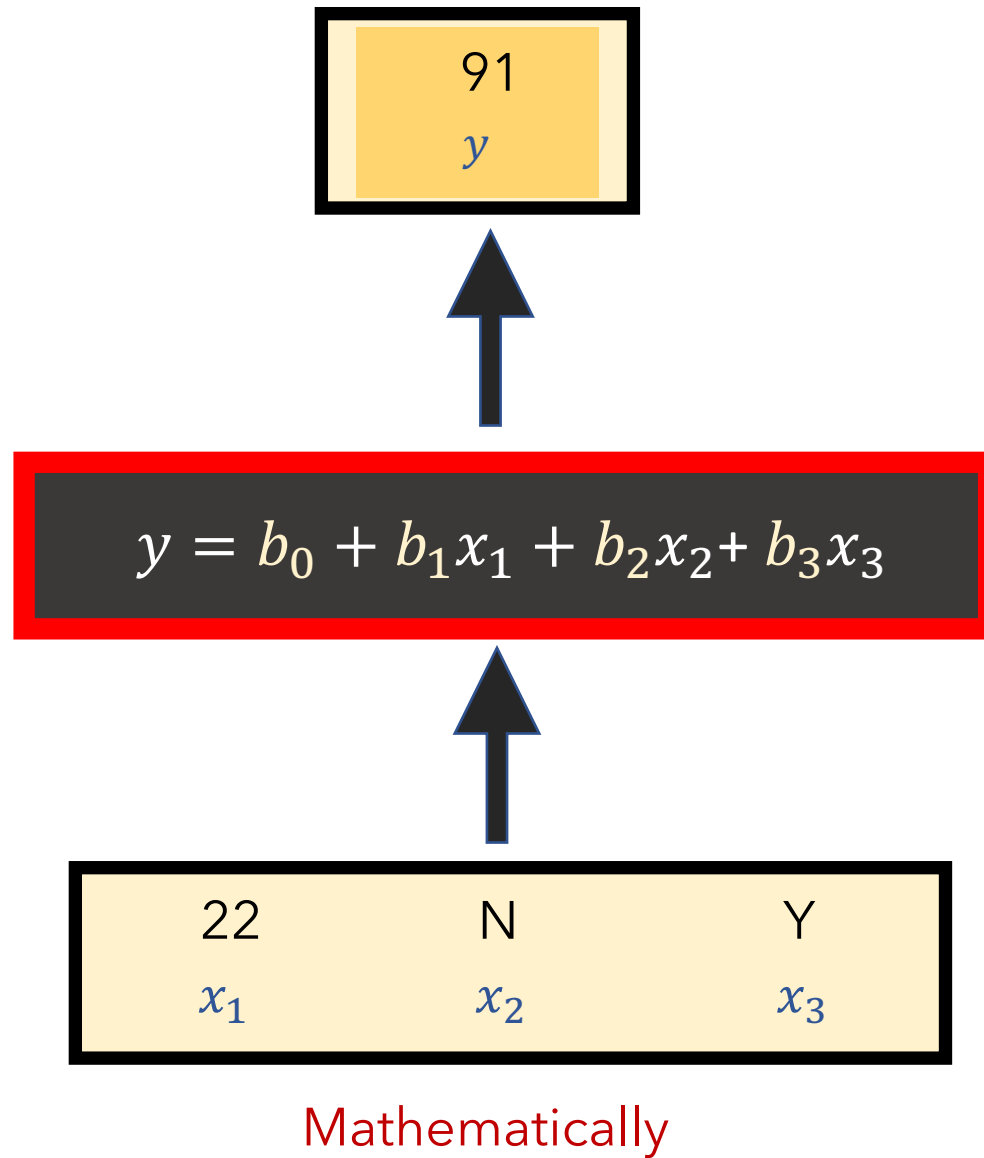
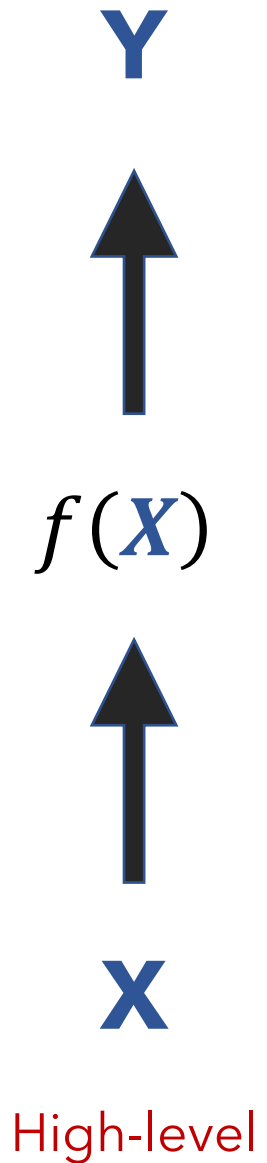
$f(X)$



**X**

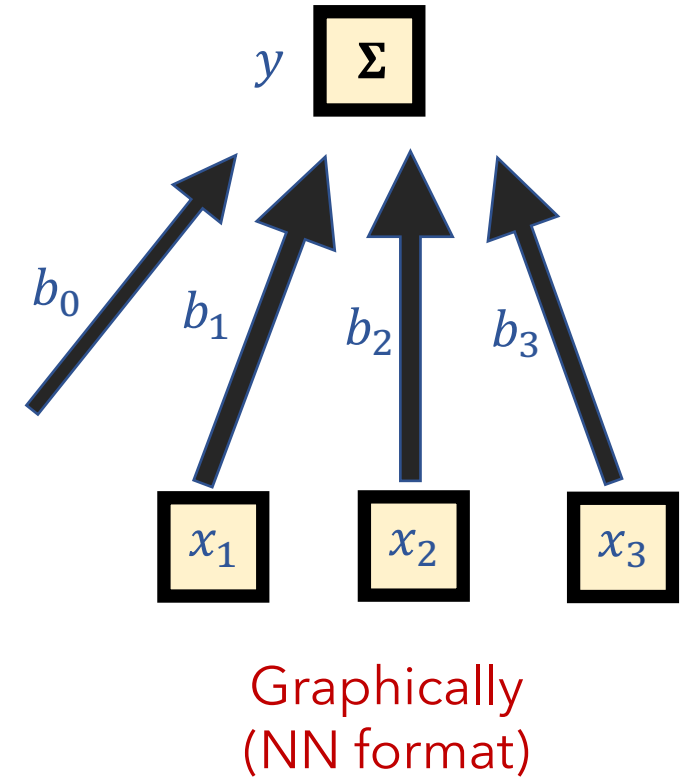
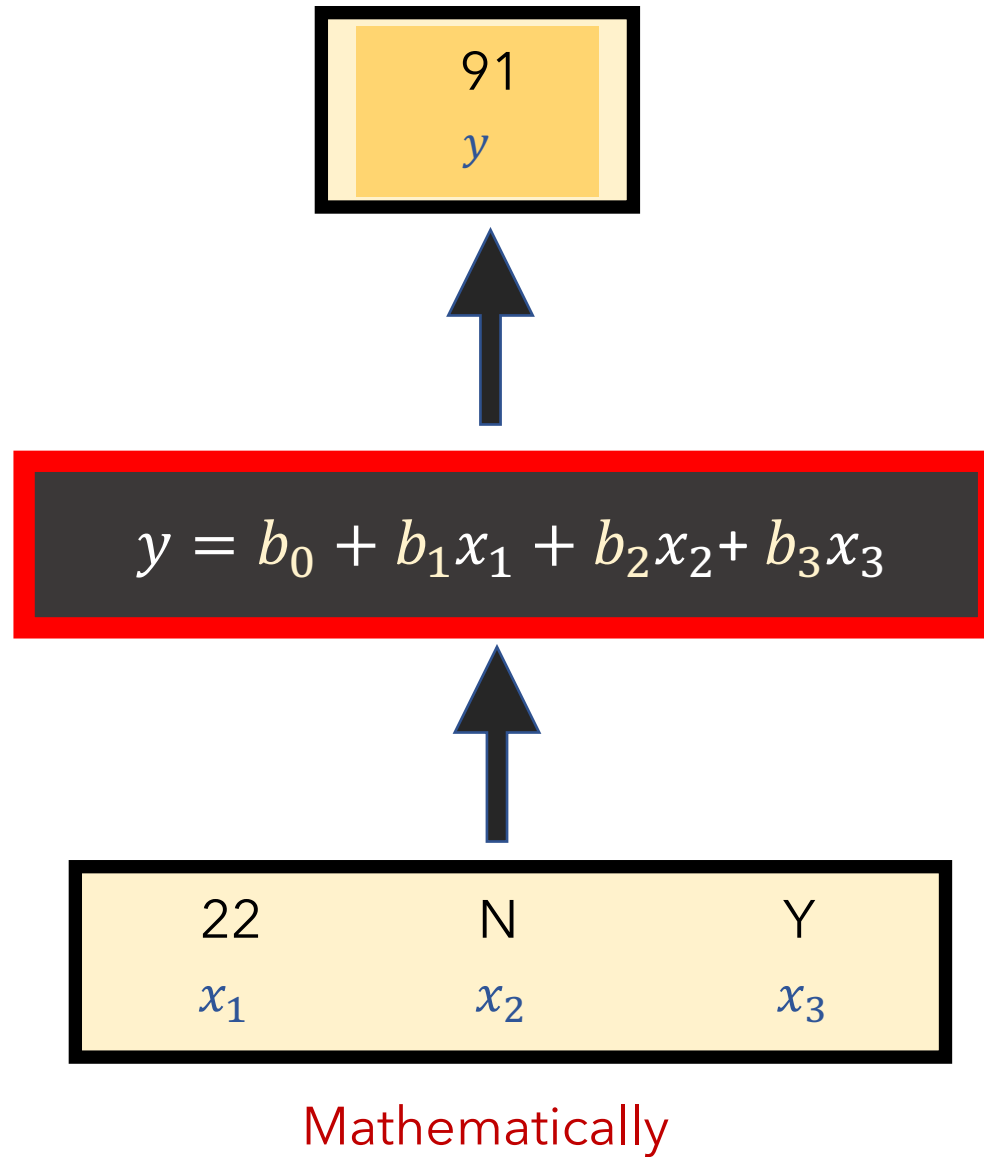
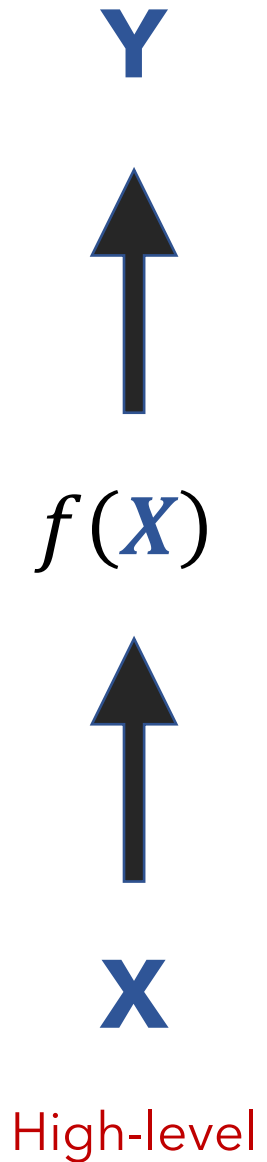
High-level

# Linear Regression





# Linear Regression



# Linear Regression

Y



$f(X)$



X

High-level

## NOTE:

For convenience, in machine learning we tend to let  $\theta$  represent all of our model's parameters (e.g.,  $\theta = \{b_0, b_1, b_2, b_3\}$  )

$x_1$

$x_2$

$x_3$

Mathematically

$x_1$

$x_2$

$x_3$

Graphically  
(NN format)

3

## IMPORTANT

When **training** any supervised model,  
be mindful of what you select for:

---

1. Our **loss function** (aka cost function)

Measures how bad our current  
parameters  $\theta$  are

2. Our **optimization** algorithm?

Determines how we update our parameters  $\theta$   
so that our model better fits our training data

## IMPORTANT

When **training** any supervised model, be mindful of what you select for:

1. Our **loss function** (aka cost function)

Measures how bad our current parameters  $\theta$  are

2. Our **optimization** algorithm?

Determines how we update our parameters  $\theta$  so that our model better fits our training data

When **testing** our model's predictions, be mindful of what you select for:

3. Our **evaluation metric**

Determines our model's performance (e.g., Mean Squared Error (MSE),  $R^2$ ,  $F1$  score, etc.)

# Linear Regression

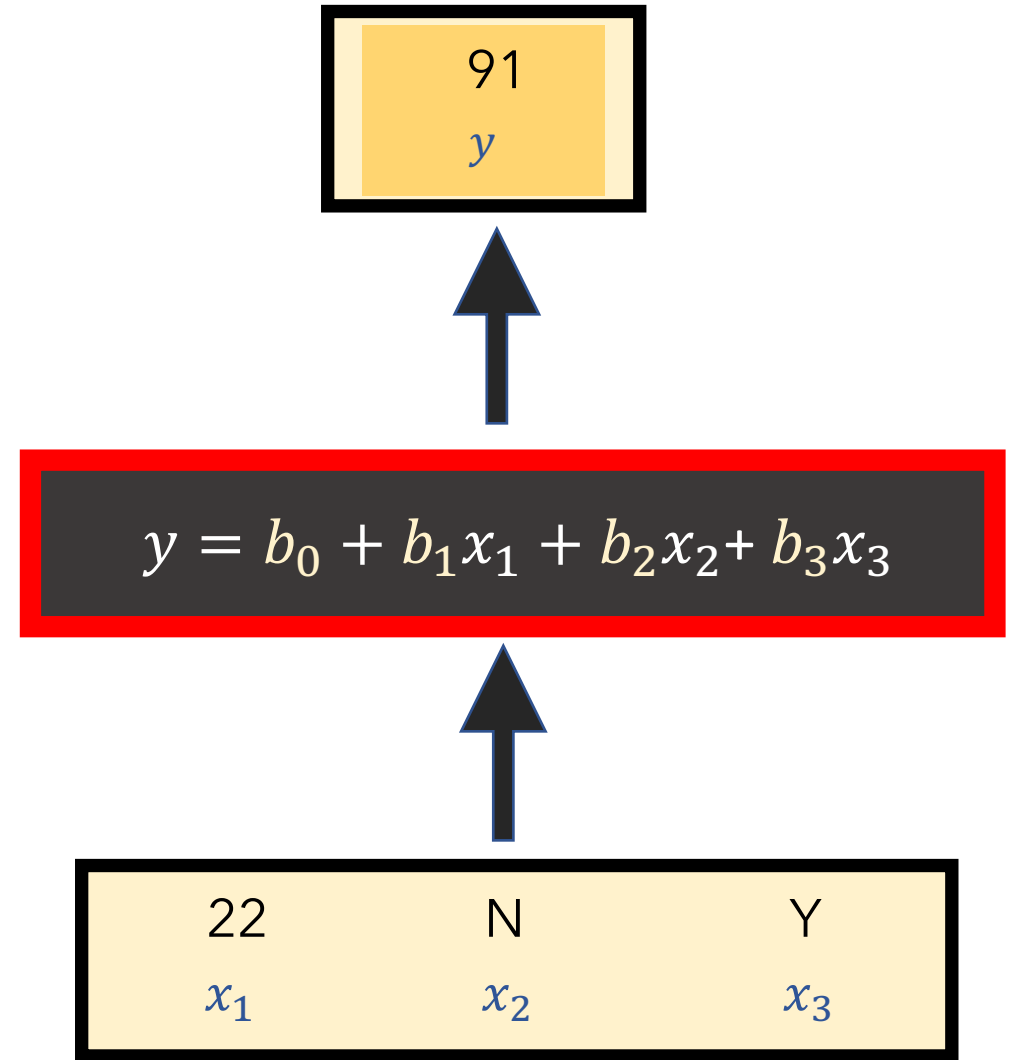
**Q1**

When training our model, how do we measure its  $m$  predictions  $\hat{y}$  ?

**A1**

Cost function  $J(\theta) = \frac{1}{2} \sum_{i=1}^m (\hat{y} - y)^2$

"Least Squares"



Mathematically

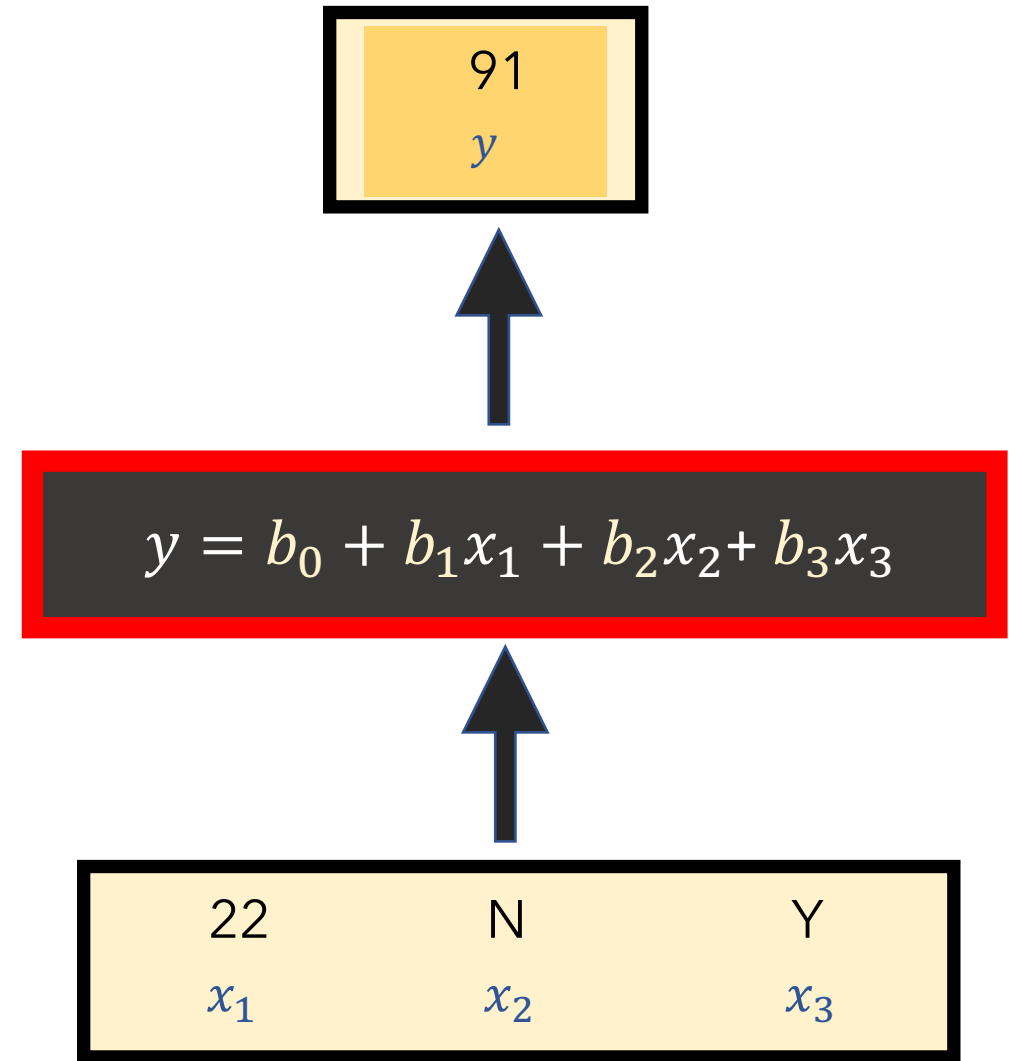
# Linear Regression

**Q1** When training our model, how do we measure its  $m$  predictions  $\hat{y}$  ?

**A1** Cost function  $J(\theta) = \frac{1}{2} \sum_{i=1}^m (\hat{y} - y)^2$

"Least Squares"

**Q2** How do we find the optimal  $\theta$  so that we yield the best predictions?



Mathematically

# Linear Regression

**Q1** When training our model, how do we measure its  $m$  predictions  $\hat{y}$  ?

**A1** Cost function  $J(\theta) = \frac{1}{2} \sum_{i=1}^m (\hat{y} - y)^2$

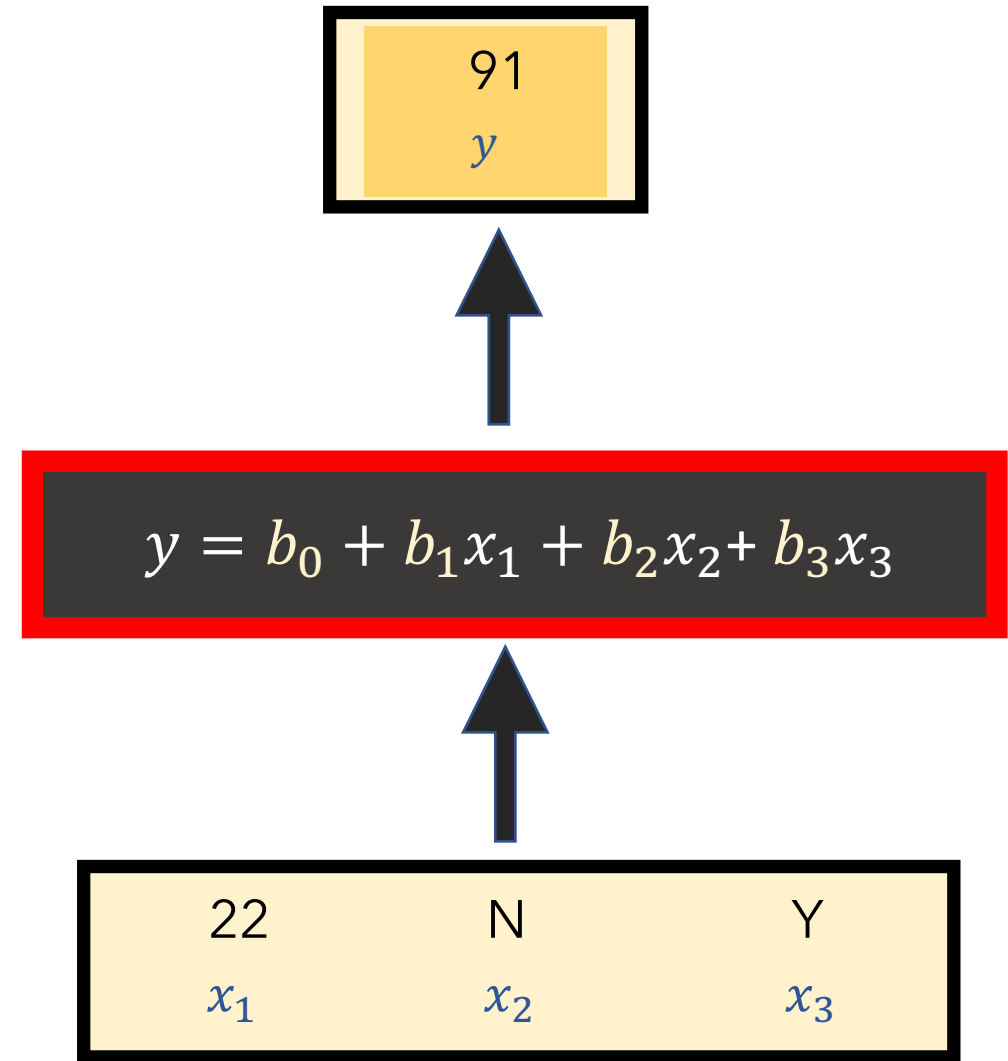
"Least Squares"

**Q2** How do we find the optimal  $\theta$  so that we yield the best predictions?

**A2** Two optimization algorithm options:

- Gradient Descent (iteratively search)
- Directly (closed-form solution)

$$\theta = (X^T X)^{-1} X^T Y$$

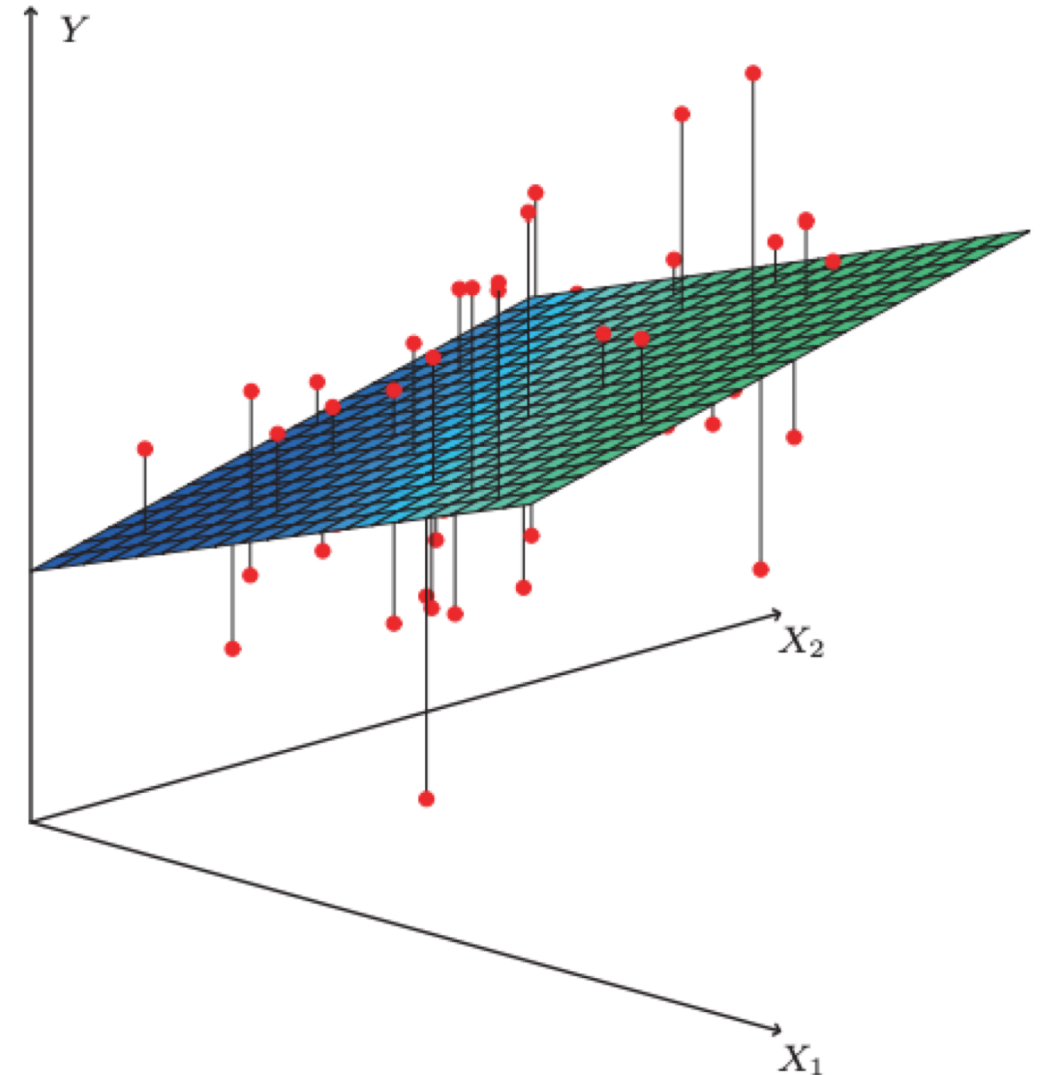


Mathematically

# Linear Regression

## Fitted model example

The plane is chosen to minimize the sum of the squared vertical distances (per our loss function, least squares) between each observation (red dots) and the plane.





# Linear Regression

## PROS

- **Simple** and **fast** approach to model linear relationships
- Interpretable results via  $\theta$  ( $\beta$  coefficients)

## CONS

- Can't model **non-linear** relationships
- Vulnerable to **outliers**
- Vulnerable to **collinearity**
- Assumes error terms are **uncorrelated\***

\* otherwise, we have false feedback during training

**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

Linear Regression

**Supervised**

**Regression**

- Returning to our data, let's model **Play** instead of **Temp**
- Again, we divide our data and learn how data **X** is related to data **Y**
- Again, assert:  $Y = f(X) + \epsilon$

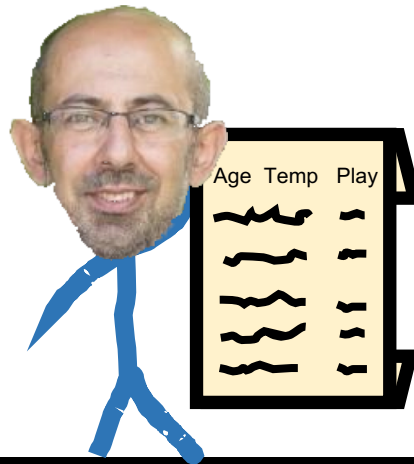
<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Temp</b>	<b>Rainy</b>	<b>Play</b>
22	91	Y	N
29	89	N	Y
31	56	N	N
23	71	N	Y
37	72	Y	N
41	83	N	Y
29	97	Y	Y
21	64	N	N
30	68	N	Y

- Returning to our data, let's model **Play** instead of **Temp**
- Again, we divide our data and learn how data **X** is related to data **Y**
- Again, assert:  $Y = f(X) + \epsilon$
- Want a model that is:
  - **Supervised**
  - Predicts categories/classes (**classification model**)
- **Q:** What model could we use?

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Temp</b>	<b>Rainy</b>	<b>Play</b>
22	91	Y	N
29	89	N	Y
31	56	N	N
23	71	N	Y
37	72	Y	N
41	83	N	Y
29	97	Y	Y
21	64	N	N
30	68	N	Y

# Playground of Models

Linear  
Regression



Age Temp Play

Age	Temp	Play
~	~	~
~	~	~
~	~	~
~	~	~
~	~	~

# Playground of Models

Logistic  
Regression

Linear  
Regression



Age	Temp	Play
~	~	~
~	~	~
~	~	~
~	~	~
~	~	~



# Logistic Regression

**Y**



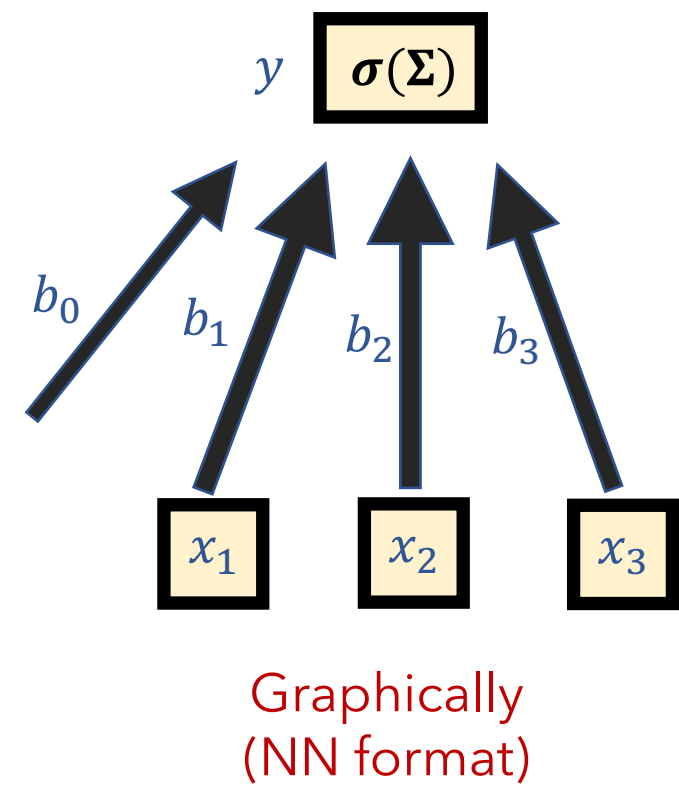
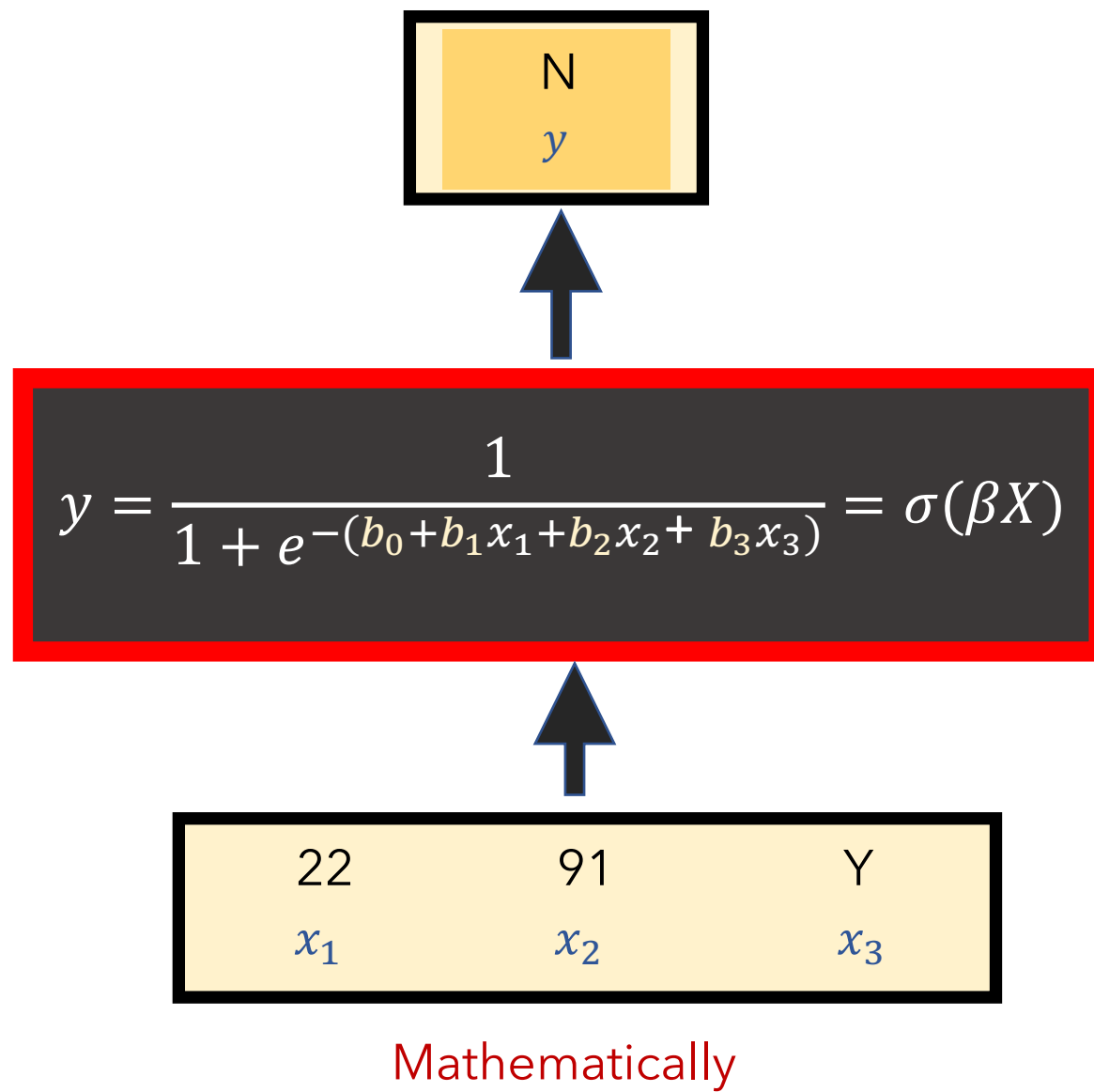
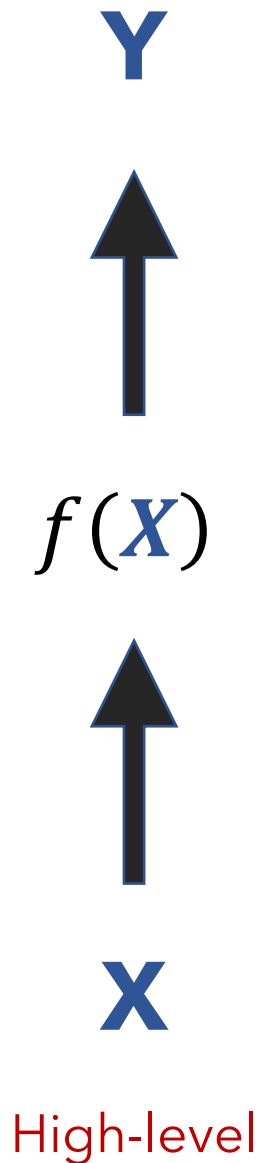
$f(X)$



**X**

High-level

# Logistic Regression





# Logistic Regression

This is a **non-linear activation function**, called a **sigmoid**.

Yet, our overall model is still considered **linear** w.r.t. the  $\beta$  coefficients.

It's a **generalized linear model**.

$$y = \frac{1}{1 + e^{-(b_0 + b_1x_1 + b_2x_2 + b_3x_3)}} = \sigma(\beta X)$$

$f(X)$



$X$

High-level



22	91	Y
$x_1$	$x_2$	$x_3$

Mathematically

# Logistic Regression

**Q1**

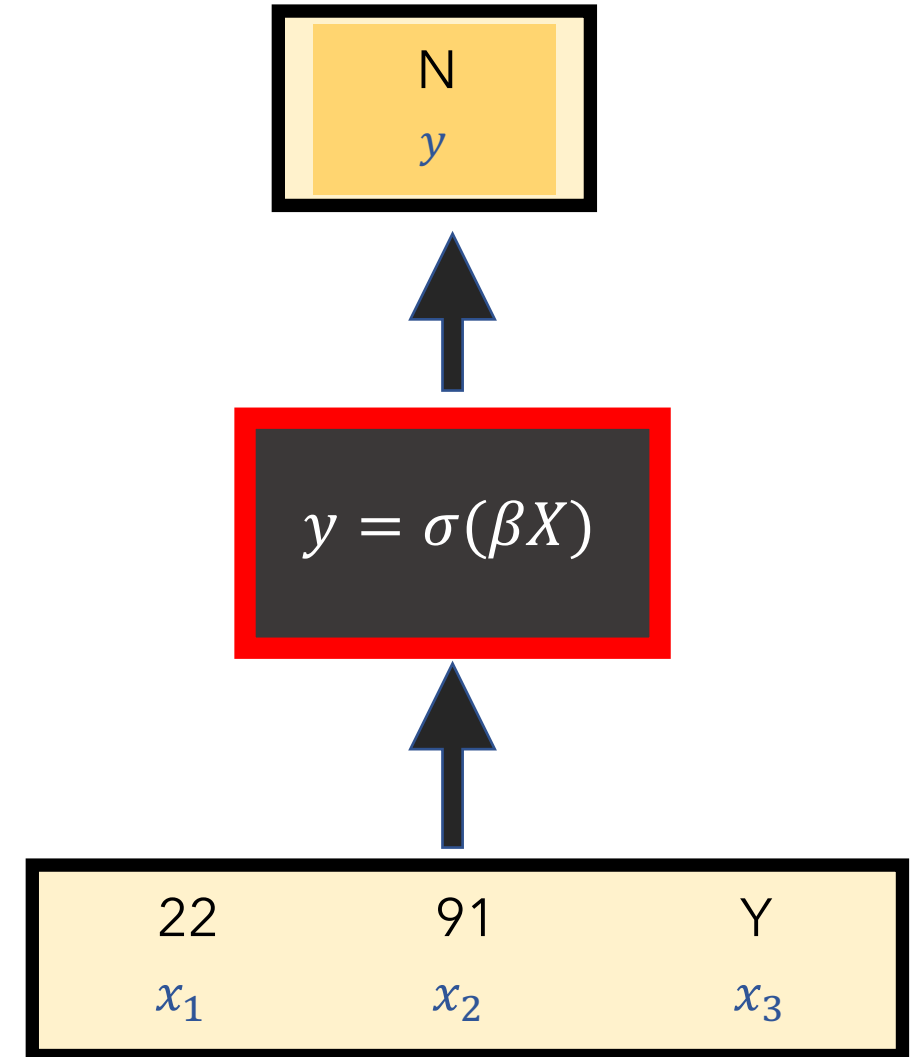
When training our model, how do we measure its  $m$  predictions  $\hat{y}$  ?

**A1**

Cost function

$$J(\theta) = -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]$$

"Cross-Entropy" aka "Log loss"



Mathematically

# Logistic Regression

**Q1** When training our model, how do we measure its  $m$  predictions  $\hat{y}$  ?

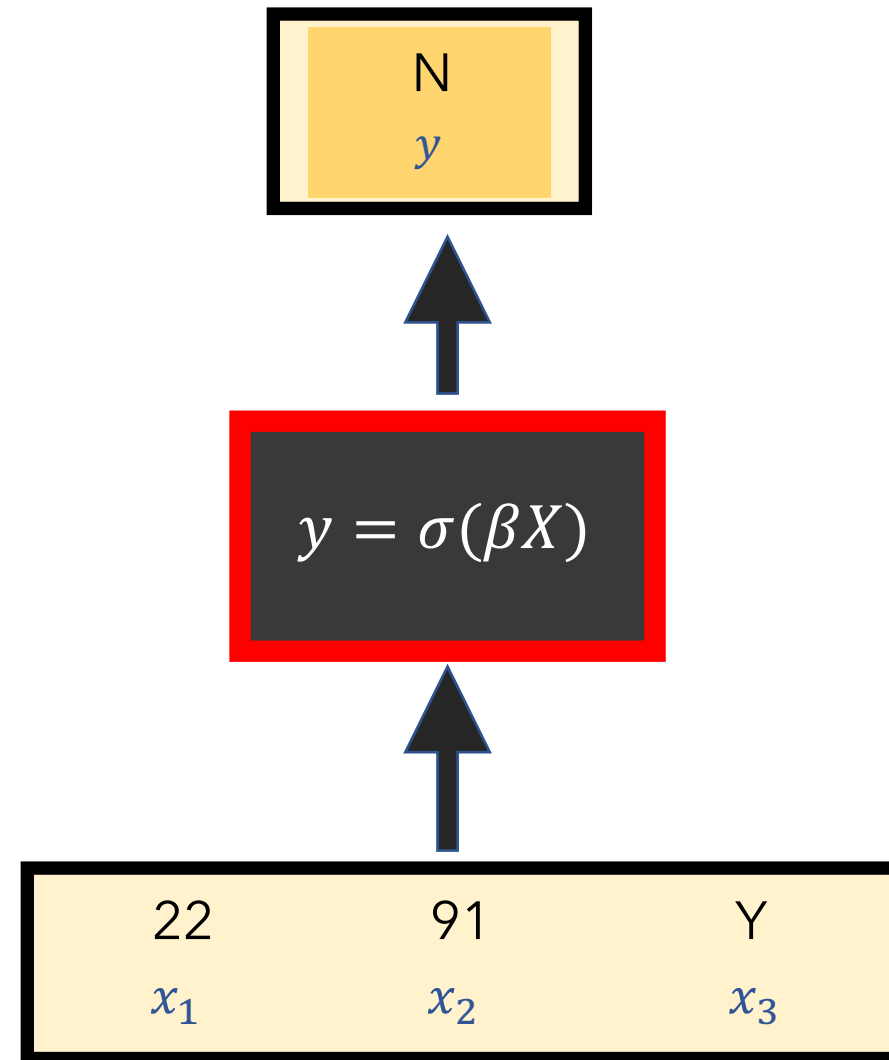
**A1** Cost function

$$J(\theta) = -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]$$

"Cross-Entropy" aka "Log loss"

**Q2** How do we find the optimal  $\theta$  so that we yield the best predictions?

**A2** [Scikits](#) has many optimization solvers: (e.g., liblinear, newton-cg, saga, etc)

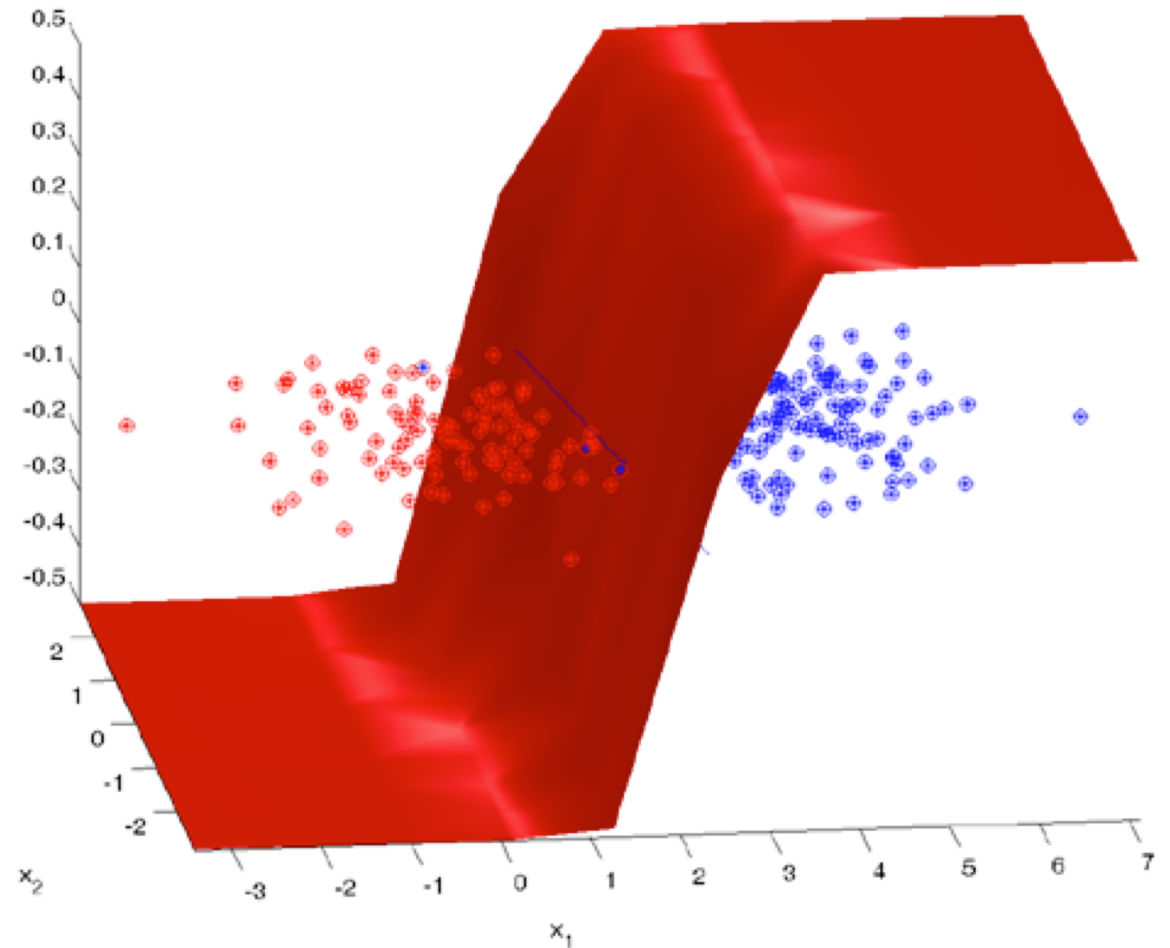


Mathematically

# Logistic Regression

## Fitted model example

The plane is chosen to minimize the error of our class probabilities (per our loss function, **cross-entropy**) and the true labels (mapped to **0** or **1**)



# Parametric Models

- So far, we've assumed our data  $\mathbf{X}$  and  $\mathbf{Y}$  can be represented by an underlying model  $f$  (i.e.,  $\mathbf{Y} = f(\mathbf{X}) + \varepsilon$ ) that has a particular form (e.g., a linear relationship, hence our using a linear model)
- Next, we aimed to fit the model  $f$  by estimating its parameters  $\theta$  (we did so in a **supervised** manner)

# Parametric Models

- So far, we've assumed our data  $\mathbf{X}$  and  $\mathbf{Y}$  can be represented by an underlying model  $f$  (i.e.,  $\mathbf{Y} = f(\mathbf{X}) + \varepsilon$ ) that has a particular form (e.g., a linear relationship, hence our using a linear model)
- Next, we aimed to fit the model  $f$  by estimating its parameters  $\theta$  (we did so in a **supervised** manner)
- **Parametric models** make the above assumptions. Namely, that there exists an underlying model  $f$  that has a fixed number of parameters.

**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

Linear Regression

**Supervised**

**Regression**

**Parametric**

Logistic Regression

**Supervised**

**Classification**

**Parametric**

# Non-Parametric Models

Alternatively, what if we make no assumptions about the underlying model  $f$ ? Specifically, let's **not assume**  $f$ :

- has any particular distribution/shape  
(e.g., Gaussian, linear relationship, etc.)
- can be represented by a finite number of parameters.



# Non-Parametric Models

Alternatively, what if we make no assumptions about the underlying model  $f$ ? Specifically, let's **not assume**  $f$ :

- has any particular distribution/shape  
(e.g., Gaussian, linear relationship, etc.)
- can be represented by a finite number of parameters.

This would constitute a non-parametric model.

# Non-Parametric Models

- Non-parametric models are **allowed to have parameters**; in fact, oftentimes the # of parameters grows as our amount of training data increases
- Since they make no strong assumptions about the form of the function/model, they are free to learn **any functional form** from the training data - *infinitely complex*.

- Returning to our data, let's again predict if a person will **Play**
- If we do not want to assume anything about how **X** and **Y** relate, we could use a different **supervised** model
- Suppose we do not care to build a decision boundary but merely want to make predictions based on similar data that we saw during training

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Temp</b>	<b>Rainy</b>	<b>Play</b>
22	91	Y	N
29	89	N	Y
31	56	N	N
23	71	N	Y
37	72	Y	N
41	83	N	Y
29	97	Y	Y
21	64	N	N
30	68	N	Y

# Playground of Models

Logistic  
Regression

Linear  
Regression



Age	Temp	Play
~	~	~
~	~	~
~	~	~
~	~	~
~	~	~



# Playground of Models

Logistic  
Regression

Linear  
Regression

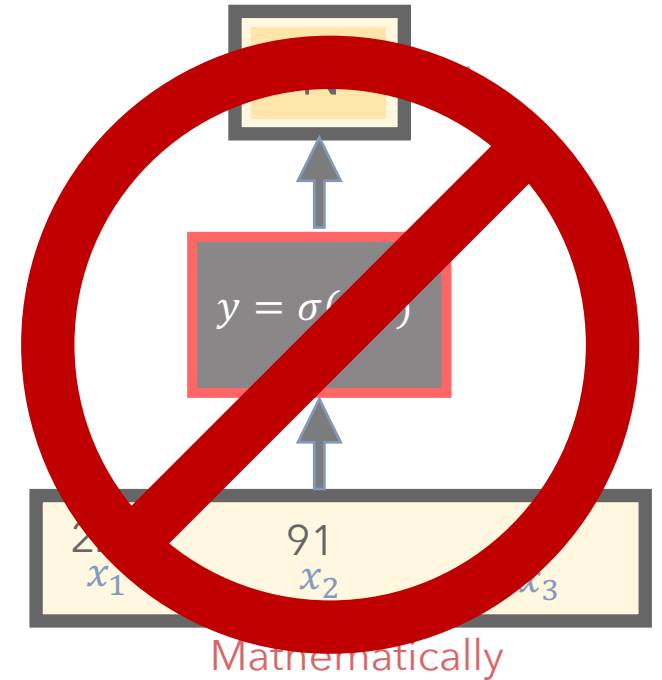


Age	Temp	Play
~	~	~
~	~	~
~	~	~
~	~	~
~	~	~

k-NN

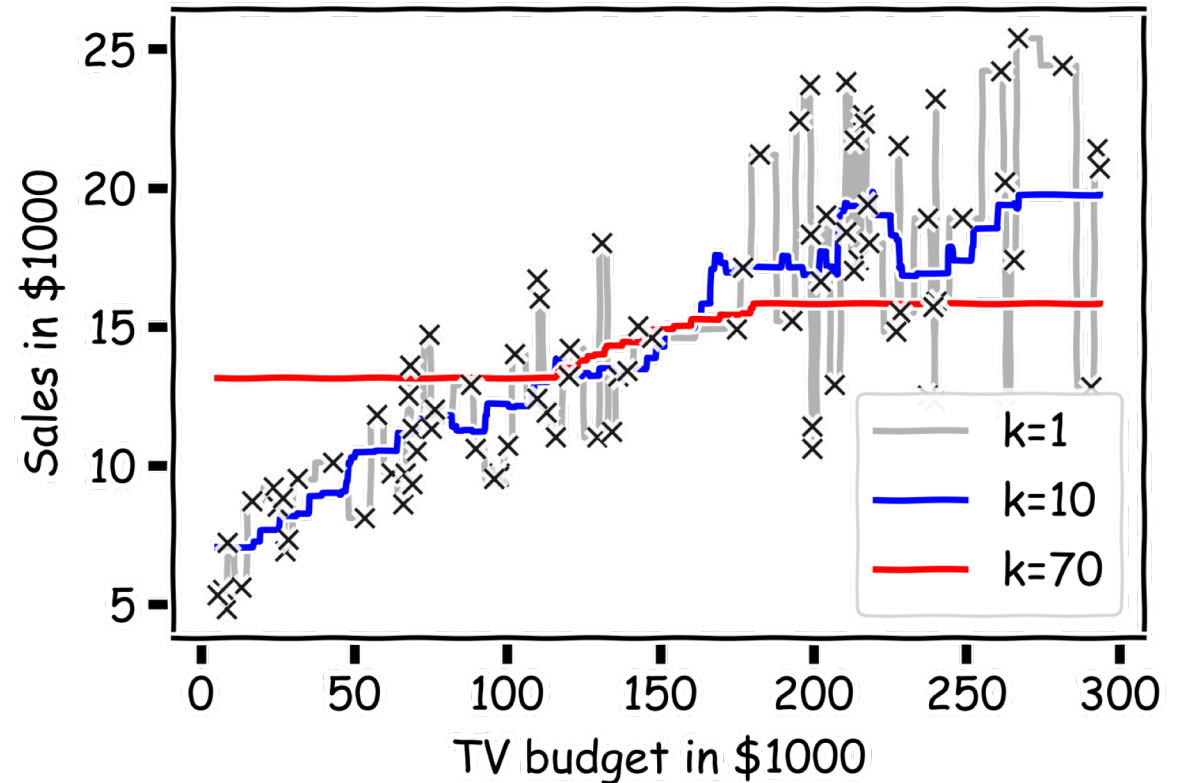
## Refresher:

- k-NN doesn't train a model
- One merely specifies a **k** value
- At test time, a new piece of data **a**:
  - must be compared to all other training data **b**, to determine its k-nearest neighbors, per some distance metric **d(a, b)**
  - is classified as being the majority class (if categorical) or average (if quantitative) of its k-neighbors



## Conclusion:

- k-NN makes no assumptions about the data  $X$  or the form of  $f(X)$
- k-NN is a **non-parametric model**



## PROS

- **Intuitive** and **simple** approach
- Can model any type of data / places no assumptions on the data
- Fairly robust to missing data
- Good for highly sparse data  
(e.g., user data, where the columns are thousands of potential items of interest)

## CONS

- Can be very **computationally expensive** if the data is large or high-dimensional
- Should carefully think about features, including scaling them
- Mixing quantitative and categorical data can be tricky
- Interpretation isn't meaningful
- Often, regression models are better, especially with little data



**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

Linear Regression

**Supervised**

**Regression**

**Parametric**

Logistic Regression

**Supervised**

**Classification**

**Parametric**

k-NN

**Supervised**

**either**

**Non-Parametric**

- Returning to our data *yet again*, let's predict if a person will **Play**
- If we do not want to assume anything about how **X** and **Y** relate, believing that no single equation can model the possibly non-linear relationship
- Suppose we just want our model to have robust decision boundaries with interpretable results

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Temp</b>	<b>Rainy</b>	<b>Play</b>
22	91	Y	N
29	89	N	Y
31	56	N	N
23	71	N	Y
37	72	Y	N
41	83	N	Y
29	97	Y	Y
21	64	N	N
30	68	N	Y

# Playground of Models

Logistic  
Regression

Linear  
Regression



Age	Temp	Play
~	~	~
~	~	~
~	~	~
~	~	~
~	~	~

k-NN

# Playground of Models

Logistic  
Regression

Linear  
Regression



Age Temp Play

k-NN



Decision  
Tree

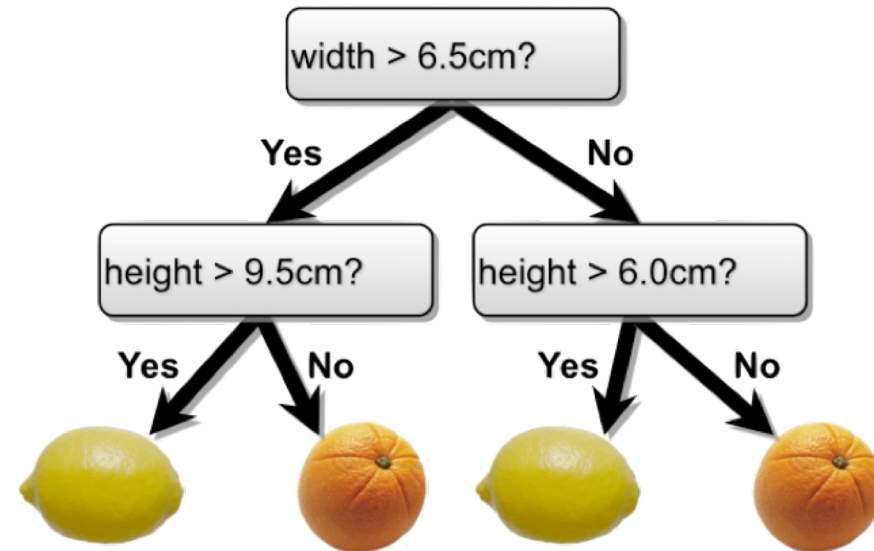
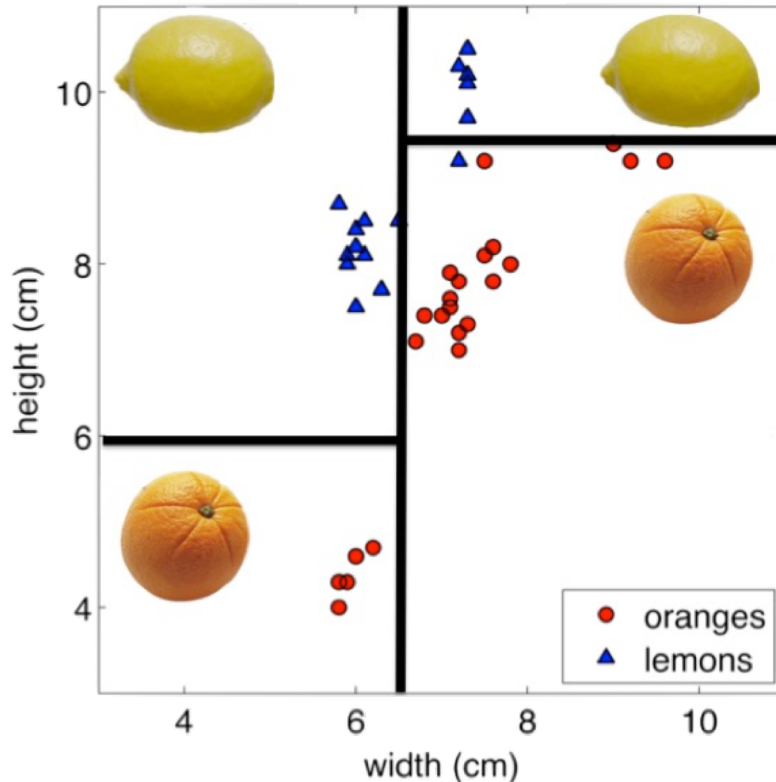
# Decision Tree

## Refresher:

- A **Decision Tree** iteratively determines how to split our data by the best feature value so as to minimize the entropy (uncertainty) of our resulting sets.
- Must specify the:
  - Splitting criterion (e.g., Gini index, Information Gain)
  - Stopping criterion (e.g., tree depth, Information Gain Threshold)

# Decision Tree

**Refresher:** Each comparison and branching represents splitting a region in the feature space on a single feature. Typically, at each iteration, we split once along one dimension (one predictor).



**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

Linear Regression

**Supervised**

**Regression**

**Parametric**

Logistic Regression

**Supervised**

**Classification**

**Parametric**

k-NN

**Supervised**

**either**

**Non-Parametric**

Decision Tree

?

?

?

# Decision Tree

- A **Decision Tree** makes no distributional assumptions about the data.
- The number of parameters / shape of the tree depends entirely on the data (i.e., imagine data that is perfectly separable into disjoint sections by features, vs data that is highly complex with overlapping values)
- Decision Trees make use of the full data (**X** and **Y**) and can handle **Y** values that are categorical or quantitative



**Supervised vs  
Unsupervised**

**Regression vs  
Classification**

**Parametric vs  
Non-Parametric**

Linear Regression

**Supervised**

**Regression**

**Parametric**

Logistic Regression

**Supervised**

**Classification**

**Parametric**

k-NN

**Supervised**

**either**

**Non-Parametric**

Decision Tree

**Supervised**

**either**

**Non-Parametric**

## Your Data $X$

- Returning to our full dataset  $X$ , imagine we do not wish to leverage any particular column  $Y$ , but merely wish to **transform** the data into a smaller, useful representation

$$\hat{X} = f(X)$$

Age	Play	Rainy	Temp
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

# Playground of Models

Logistic  
Regression

Linear  
Regression



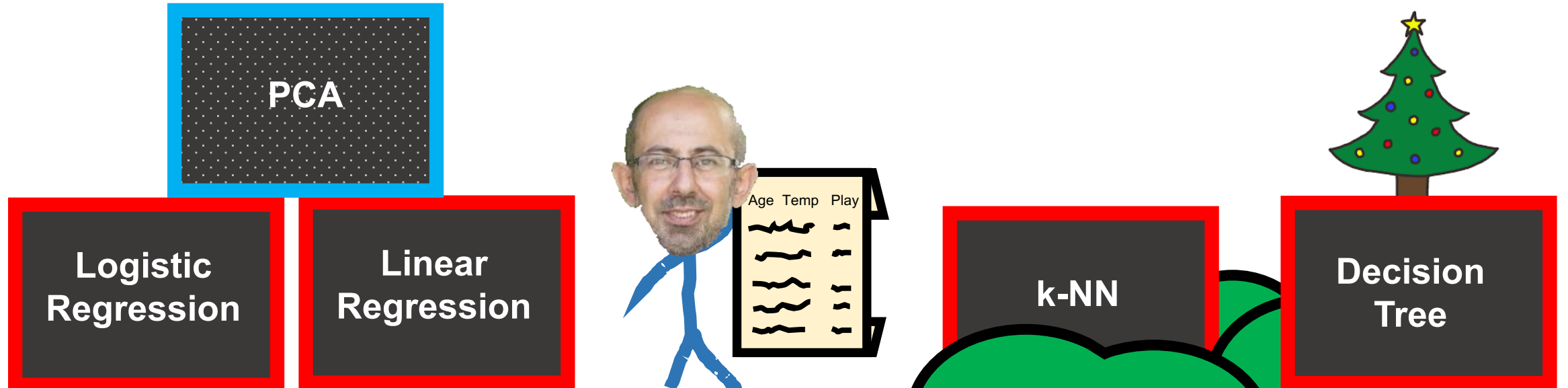
Age Temp Play

k-NN



Decision  
Tree

# Playground of Models



# Principal Component Analysis (PCA)

## Refresher:

- PCA isn't a model per se but is a procedure/technique to transform data, which may have correlated features, into a **new, smaller set of uncorrelated features**
- These new features, by design, are a linear combination of the original features so as to capture the most variance
- Often useful to perform PCA on data before using models that explicitly use data values and distances between them (e.g., clustering)

**Supervised vs  
Unsupervised**

**Regression vs  
Classification**

**Parametric vs  
Non-Parametric**

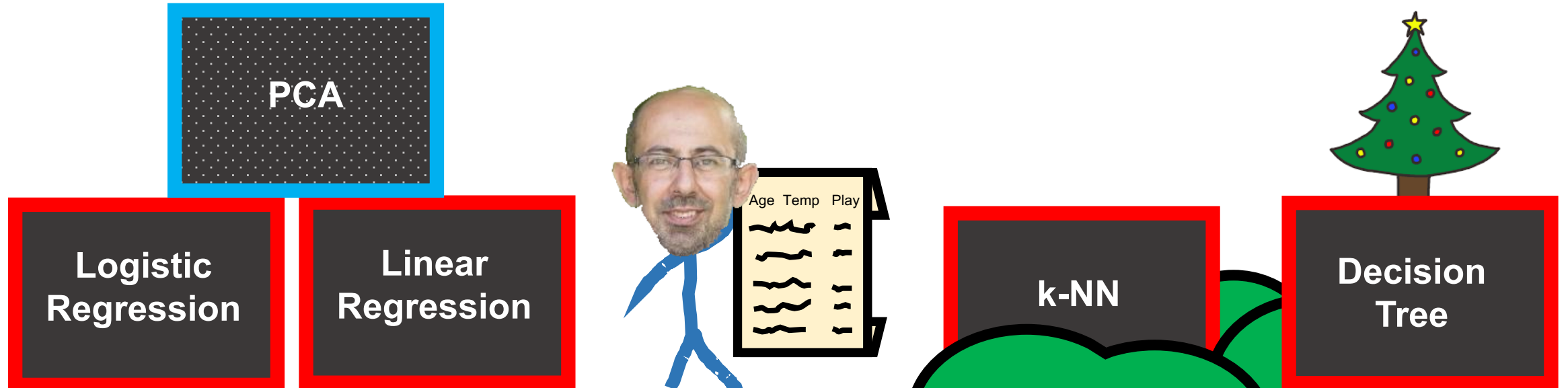
Linear Regression	<b>Supervised</b>	<b>Regression</b>	<b>Parametric</b>
Logistic Regression	<b>Supervised</b>	<b>Classification</b>	<b>Parametric</b>
k-NN	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>
Decision Tree	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>
PCA	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>

## Your Data $X$

- Returning to our full dataset  $X$  yet again, imagine we do not wish to leverage any particular column  $Y$ , but merely wish to discern patterns/groups of similar observations

Age	Play	Rainy	Temp
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

# Playground of Models





# Playground of Models

Clustering

PCA

Logistic  
Regression

Linear  
Regression



Age Temp Play

k-NN



Decision  
Tree

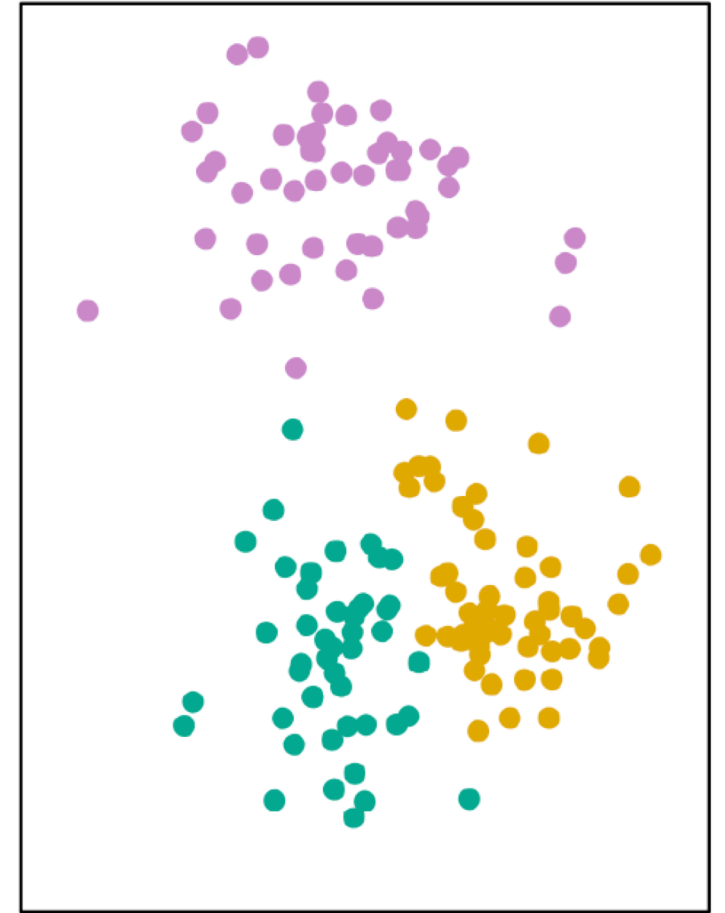
## Refresher:

- There are many approaches to clustering (e.g., k-Means, hierarchical, DBScan)
- Regardless of the approach, we need to specify a distance metric (e.g., Euclidean, Manhattan)
- **Performance:** we can measure the intra-cluster and outer-cluster fit (i.e., [silhouette score](#)), along with an estimate that compares our clustering to the situation had our data been randomly generated ([gap statistic](#))

# Clustering

## k-Means example:

- Although we are not explicitly using any column  $Y$ , one could imagine that the 3 resulting cluster labels are our  $Y$ 's (labels being class **1**, **2**, and **3**)
- Of course, we do not know these class labels ahead of time, as clustering is an unsupervised model

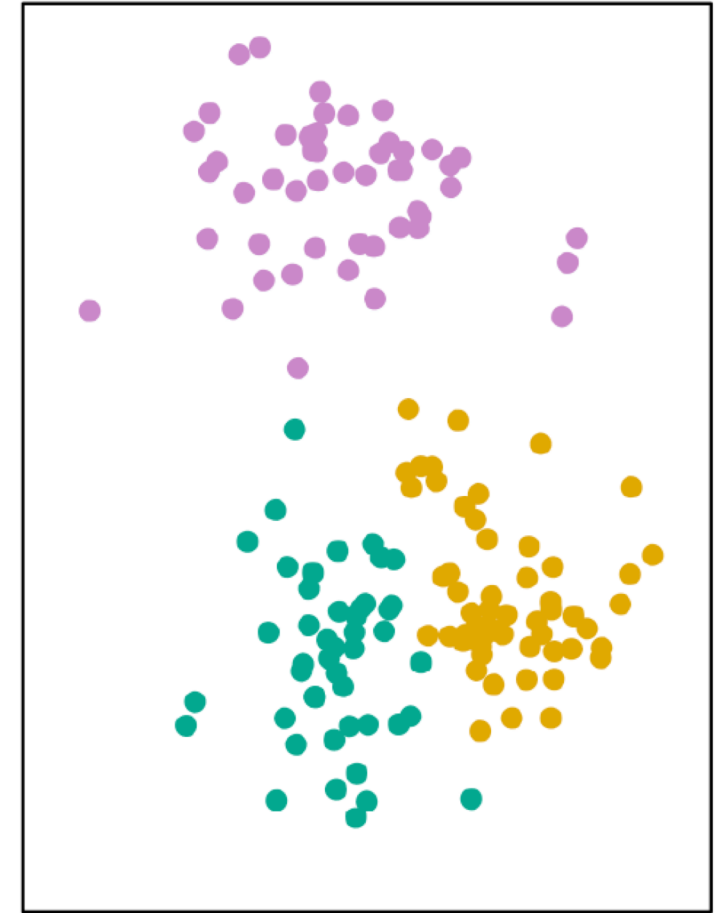


Visual Representation

# Clustering

## k-Means example:

- Although we are not explicitly using any column  $Y$ , one could imagine that the 3 resulting cluster labels are our  $Y$ 's (labels being class **1**, **2**, and **3**)
- Of course, we do not know these class labels ahead of time, as clustering is an unsupervised model
- Yet, one could imagine a narrative whereby our data points were **generated** by these 3 classes.

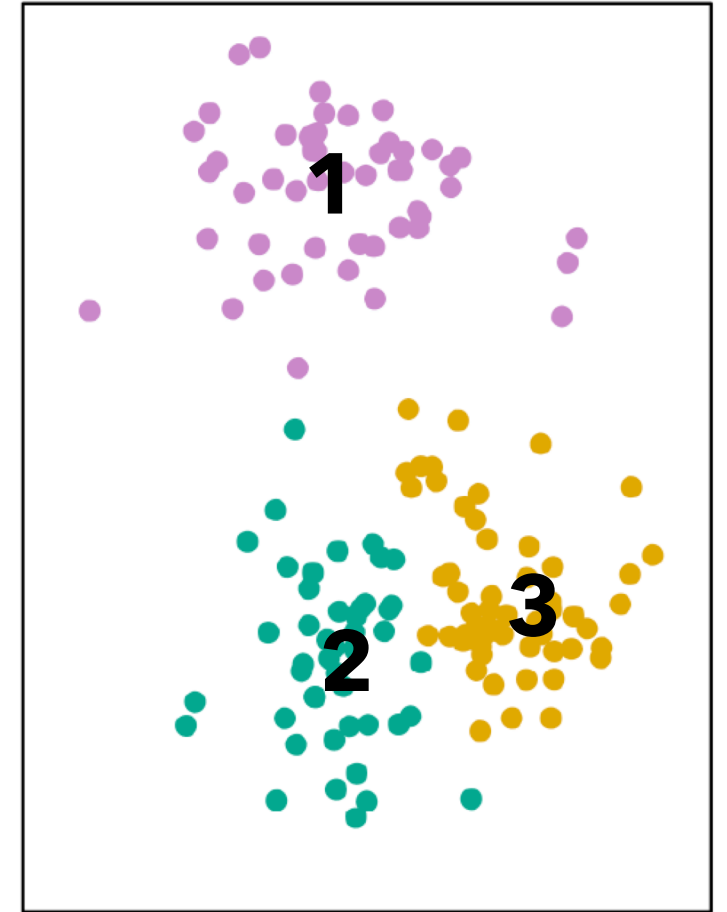


Visual Representation

# Clustering

## k-Means example:

- That is, we are flipping the modelling process on its head; instead of doing our traditional supervised modelling approach of trying to estimate  $P(\mathbf{Y}|\mathbf{X})$ :
  - Imagine centroids for each of the 3 clusters  $\mathbf{Y}_i$ .  
We assert that the data  $\mathbf{X}$  were generated from  $\mathbf{Y}$ .
- We can estimate the joint probability of  $P(\mathbf{Y}, \mathbf{X})$



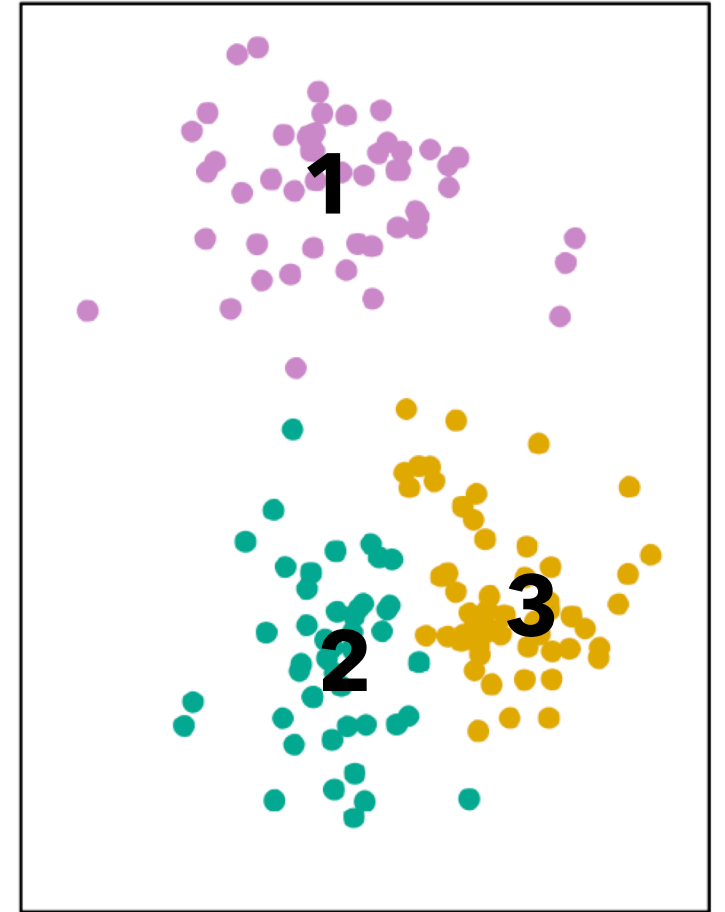
Visual Representation

# Clustering

## k-Means example:

Assuming our data was **generated** from Gaussians centered at 3 centroids, we can estimate the probability of the current situation – that the data  $X$  exists and has the following class labels  $Y$ . This is a **generative** model.

- We can estimate the joint probability of  $P(Y, X)$



Visual Representation

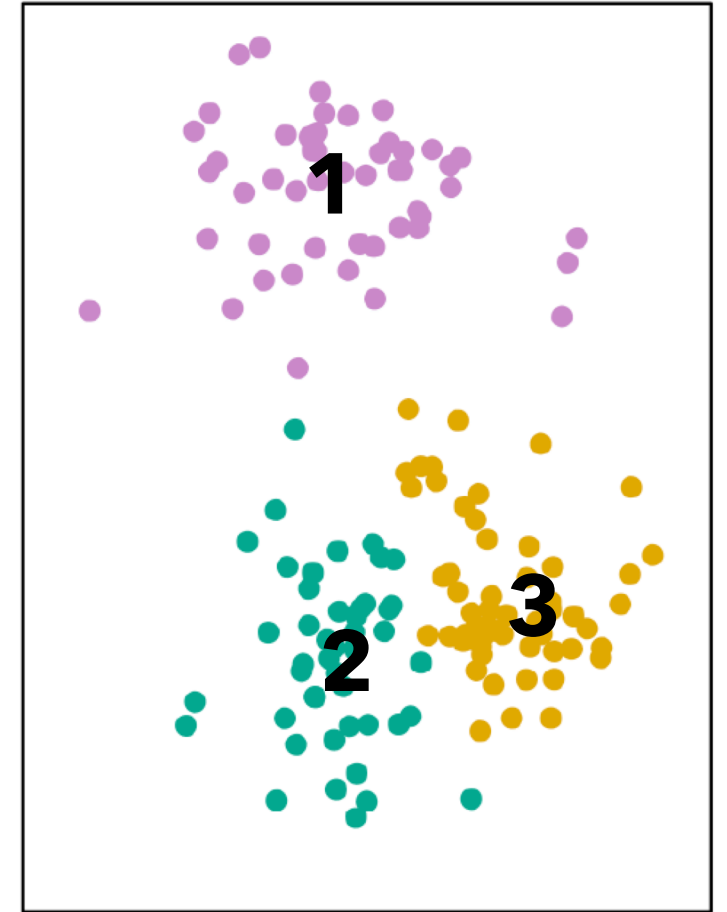
# Clustering

## k-Means example:

- That is, we are flipping the modelling process on its

**Generative models** explicitly model the actual distribution of each class (e.g., data and its cluster assignments).

- We can estimate the joint probability of  $P(\mathbf{Y}, \mathbf{X})$

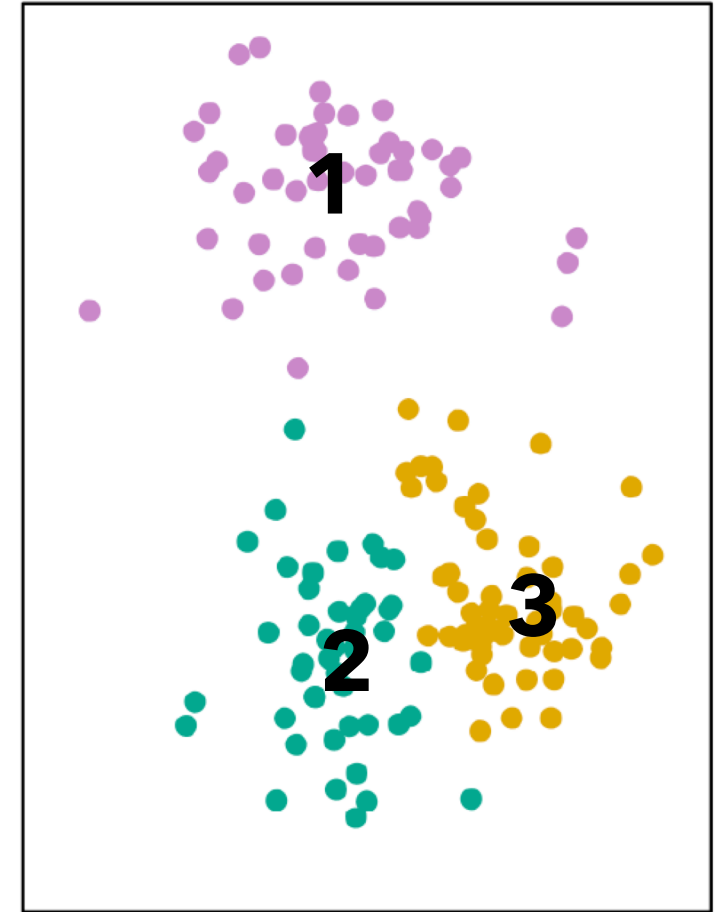


Visual Representation

# Clustering

## k-Means example:

- That is, we are flipping the modelling process on its head; instead of doing our traditional supervised modelling approach of trying to estimate  $P(\mathbf{Y}|\mathbf{X})$ :
  - Imagine centroids for each of the 3 clusters  $\mathbf{Y}_i$ .  
We assert that the data  $\mathbf{X}$  were generated from  $\mathbf{Y}$ .
- We can estimate the joint probability of  $P(\mathbf{Y}, \mathbf{X})$



Visual Representation



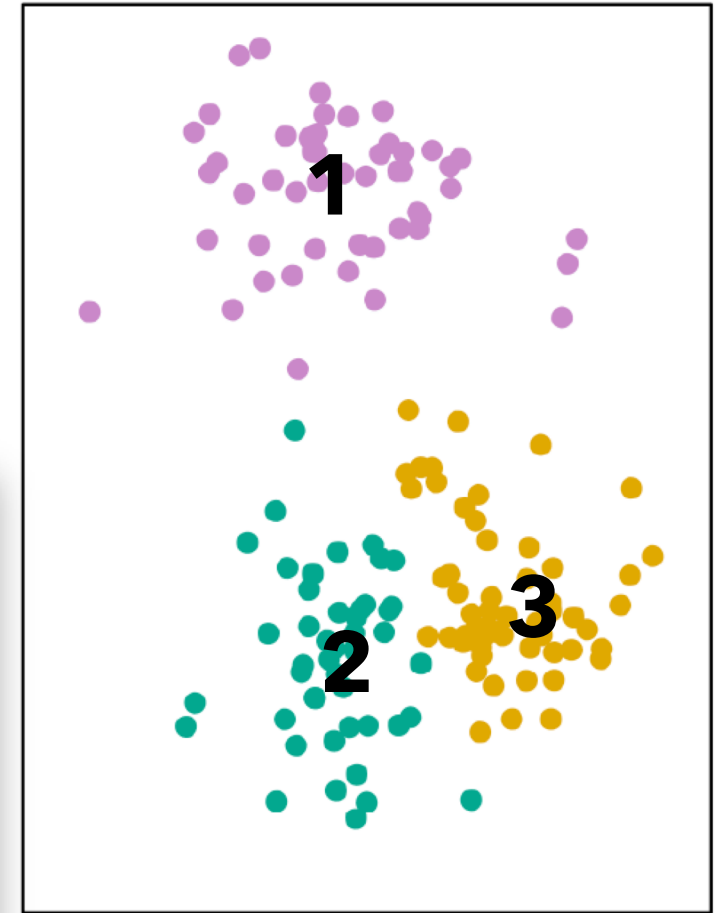
# Clustering

## k-Means example:

- That is, we are flipping the modelling process on its head; instead of doing our traditional supervised modelling approach of trying to estimate  $P(Y|X)$ :

Supervised models are given some data  $X$  and want to calculate the probability of  $Y$ .

They learn to **discriminate** between different values of possible  $Y$ 's (learns a **decision boundary**).



Visual Representation

# Generative vs Discriminative Models

## To recap:

By definition, a **generative model** is concerned with estimating the joint probability of  $P(\mathbf{Y}, \mathbf{X})$

By definition, a **discriminative model** is concerned with estimating the conditional probability  $P(\mathbf{Y}|\mathbf{X})$

**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

**Generative** vs  
**Discriminative**

Linear Regression	<b>Supervised</b>	<b>Regression</b>	<b>Parametric</b>	<b>Discriminative</b>
Logistic Regression	<b>Supervised</b>	<b>Classification</b>	<b>Parametric</b>	<b>Discriminative</b>
k-NN	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
Decision Tree	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
PCA	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>neither</b>
Clustering	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>Generative</b>

**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

**Generative** vs  
**Discriminative**

Linear Regression	Supervised	Regression	Parametric	Discriminative
Logistic Regression	Supervised	Classification	Parametric	Discriminative
k-NN	Supervised	Classification	Non-Parametric	Discriminative
Decision Tree	Supervised	Classification	Non-Parametric	Discriminative
PCA	Unsupervised	Classification	Non-Parametric	neither
Clustering	Unsupervised	Classification	Non-Parametric	Generative

Particularly, **k-Means** is generative, as it can be seen as a special case of Gaussian Mixture Models

**Supervised vs Unsupervised**

**Regression vs Classification**

**Parametric vs Non-Parametric**

**Generative vs Discriminative**

Linear Regression

Given training  $X$ , learns to discriminate between possible  $Y$  values (quantitative)

**Discriminative**

Logistic Regression

**Discriminative**

k-NN

**Discriminative**

Decision Tree

**Discriminative**

PCA

**Unsupervised**

**neither**

**Non-Parametric**

**neither**

Clustering

**Unsupervised**

**neither**

**Non-Parametric**

**Generative**

**Supervised vs Unsupervised**

**Regression vs Classification**

**Parametric vs Non-Parametric**

**Generative vs Discriminative**

Linear Regression  
Logistic Regression  
k-NN  
Decision Tree  
PCA  
Clustering

Supervised

Regression

Parametric

Discriminative

S

Given training  $X$ , learns to discriminate between possible  $Y$  classes (categorical)

S

**Discriminative**

S

etric

Discriminative

S

etric

Discriminative

Unsupervised

neither

Non-Parametric

neither

Unsupervised

neither

Non-Parametric

Generative

**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

**Generative** vs  
**Discriminative**

	<b>Supervised</b> vs <b>Unsupervised</b>	<b>Regression</b> vs <b>Classification</b>	<b>Parametric</b> vs <b>Non-Parametric</b>	<b>Generative</b> vs <b>Discriminative</b>
Linear Regression	Supervised	Regression	Parametric	Discriminative
Logistic Regression	Supervised	Classification	Parametric	Discriminative
k-NN			metric	<b>Discriminative</b>
Decision Tree			metric	Discriminative
PCA			metric	<b>neither</b>
Clustering	Unsupervised	<b>neither</b>	Non-Parametric	Generative

Given training  $X$ , learns to discriminate between possible  $Y$  values (quantitative or categorical)

**Supervised vs Unsupervised**

**Regression vs Classification**

**Parametric vs Non-Parametric**

**Generative vs Discriminative**

Linear Regression	Supervised	Regression	Parametric	Discriminative
Logistic Regression	Supervised	Classification	Parametric	Discriminative
k-NN	Supervised	either	Non-Parametric	Discriminative
Decision Tree			metric	Discriminative
PCA			metric	neither
Clustering			metric	Generative

Given training  $X$ , learns decision boundaries so as to discriminate between possible  $Y$  values (quantitative or categorical)



**Supervised vs Unsupervised**

**Regression vs Classification**

**Parametric vs Non-Parametric**

**Generative vs Discriminative**

Linear Regression	Supervised	Regression	Parametric	Discriminative
Logistic Regression	Supervised	Classification	Parametric	Discriminative
k-NN	Supervised	either	Non-Parametric	Discriminative
Decision Tree	Supervised	either	Non-Parametric	Discriminative
PCA				neither
Clustering				Generative

PCA is a **process**, not a model, so it doesn't make sense to consider it as a Discriminate or Generative model

**Supervised** vs  
**Unsupervised**

**Regression** vs  
**Classification**

**Parametric** vs  
**Non-Parametric**

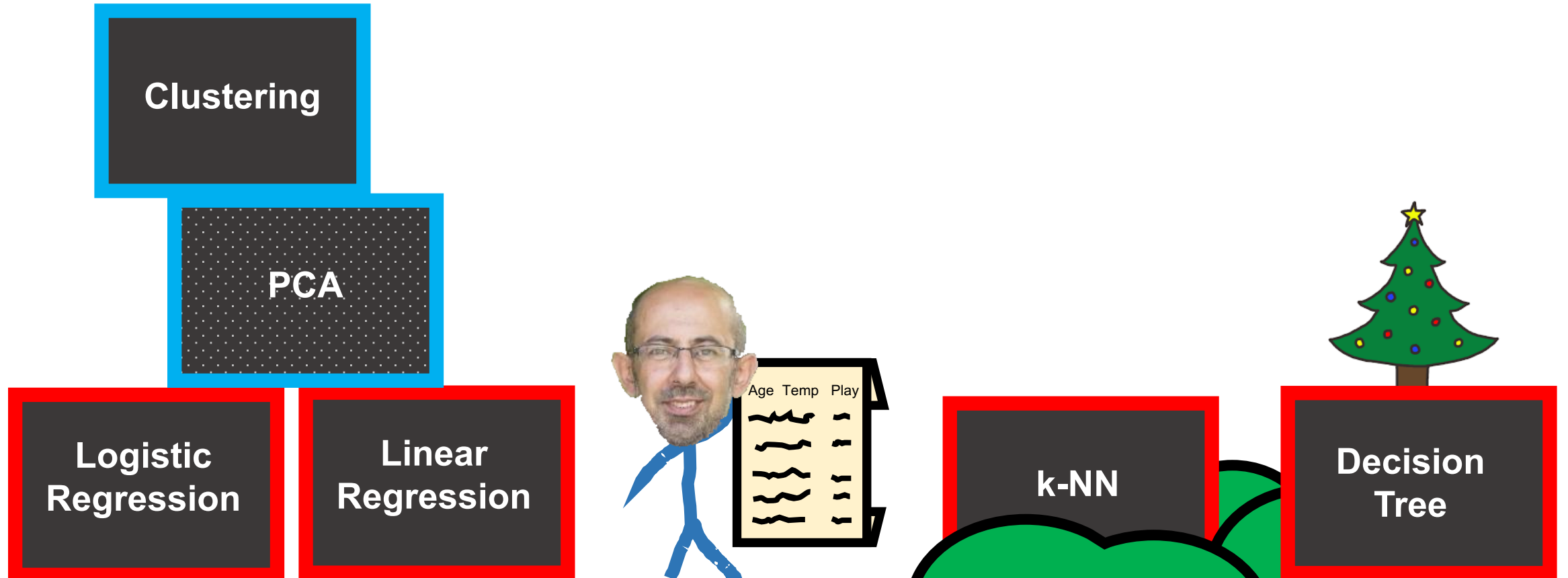
**Generative** vs  
**Discriminative**

Linear Regression	<b>Supervised</b>	<b>Regression</b>	<b>Parametric</b>	<b>Discriminative</b>
Logistic Regression	<b>Supervised</b>	<b>Classification</b>	<b>Parametric</b>	<b>Discriminative</b>
k-NN	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
Decision Tree	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
PCA	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>neither</b>
Clustering	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>Generative</b>

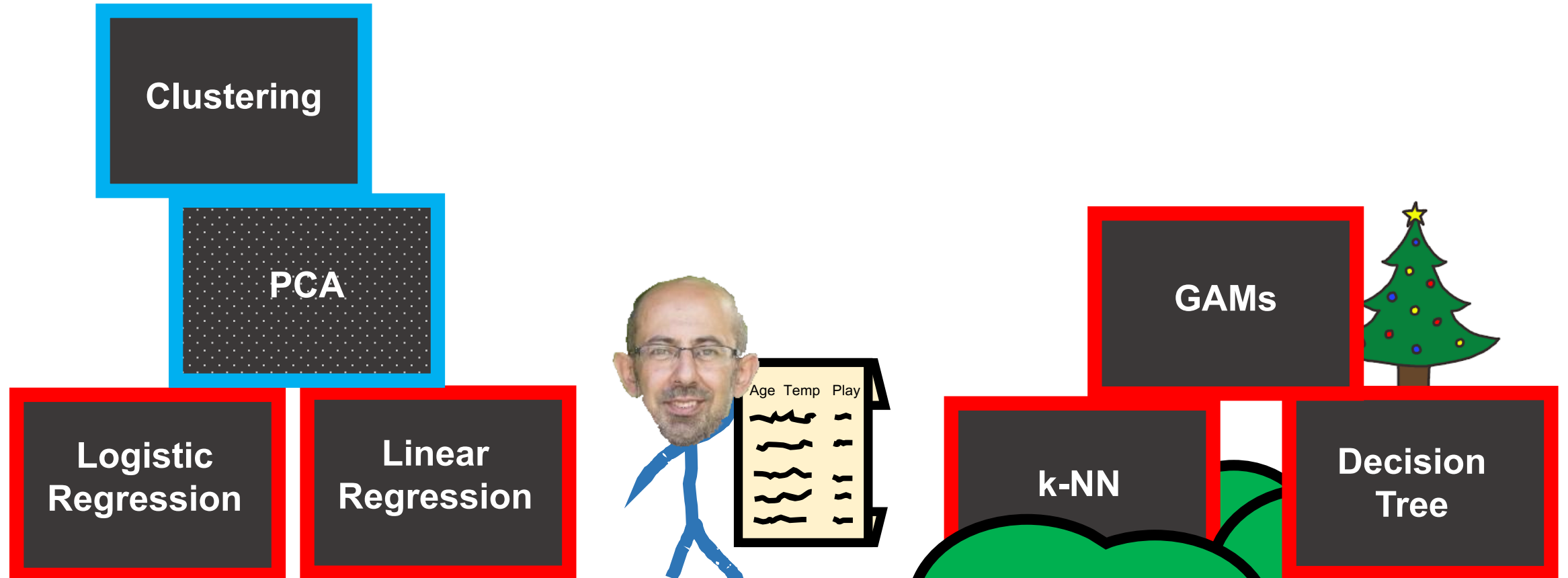
- Returning our data yet again, perhaps we've plotted our data **X** and see it's **non-linear**
- Knowing how unnatural and finnickily polynomial regression can be, we prefer to let our model learn how to make its own non-linear functions for each feature  $x_i$

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Play</b>	<b>Rainy</b>	<b>Temp</b>
22	N	Y	91
29	Y	N	89
31	N	N	56
23	Y	N	71
37	N	Y	72
41	Y	N	83
29	Y	Y	97
21	N	N	64
30	Y	N	68

# Playground of Models



# Playground of Models

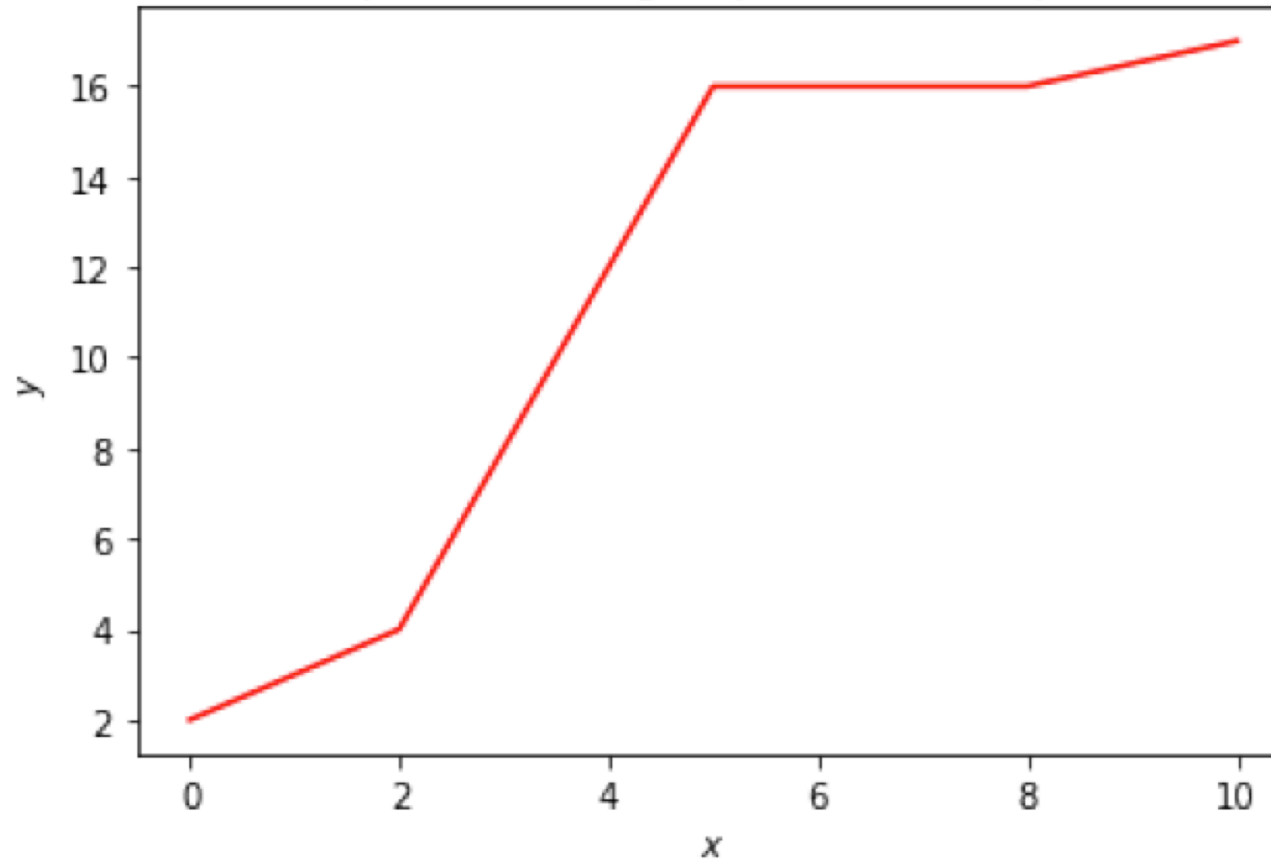


# Generalized Additive Models (GAMs)

## Refresher:

Not our data, but imagine it's plotting **age** vs **temp**:

Piecewise linear spline with knots at  $x=2, 5,$  and  $8$   
plus a starting slope and intercept



# Generalized Additive Models (GAMs)

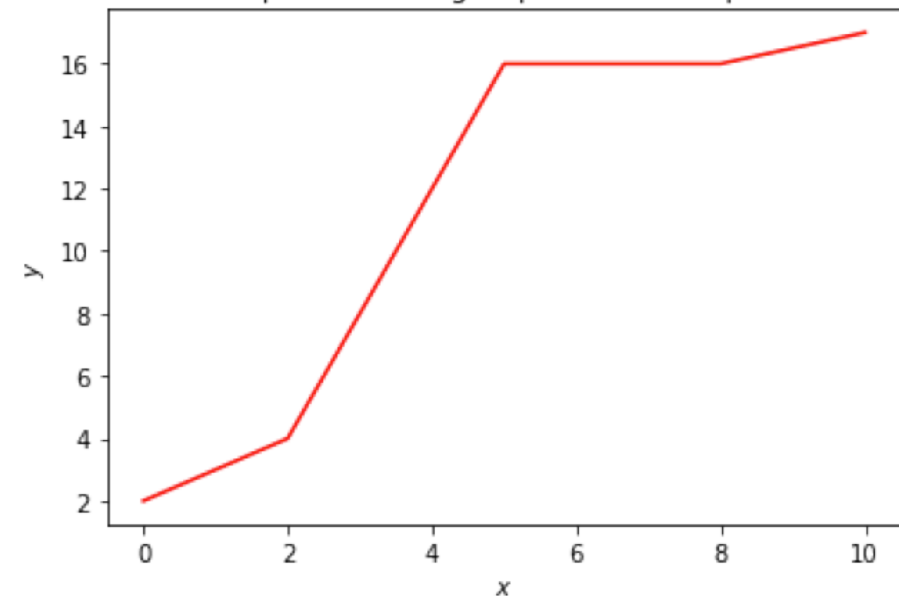
## Refresher:

- We can make the line smoother by using a **cubic spline** or “**B-spline**”
- Imagine having 3 of these models:
  - $f_1(\text{age})$
  - $f_2(\text{play})$
  - $f_3(\text{rainy})$
- We can model **Temp** as:

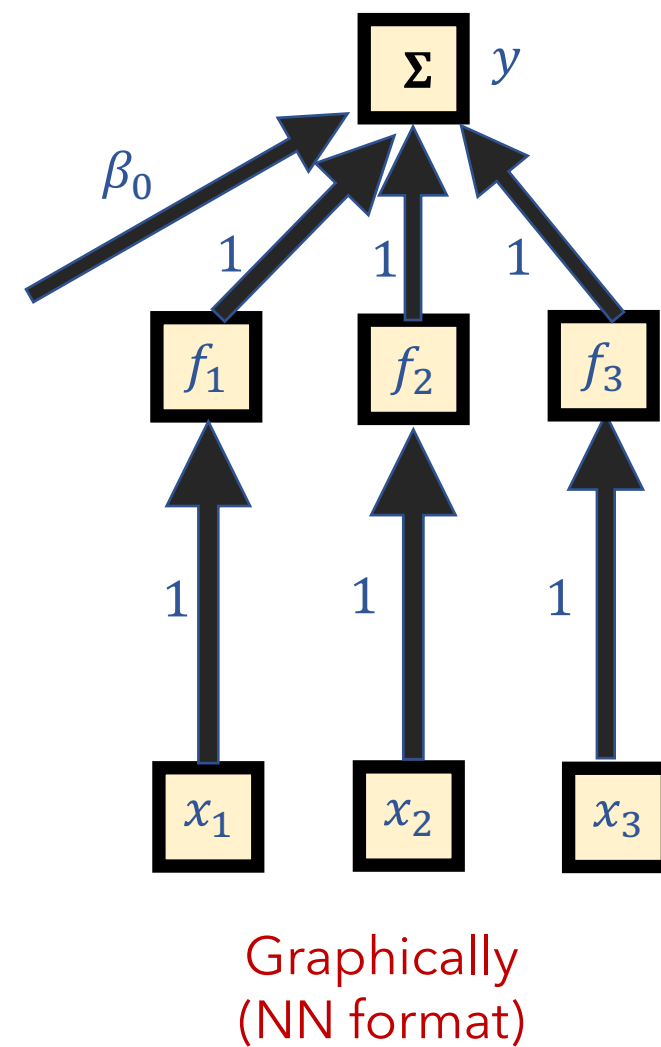
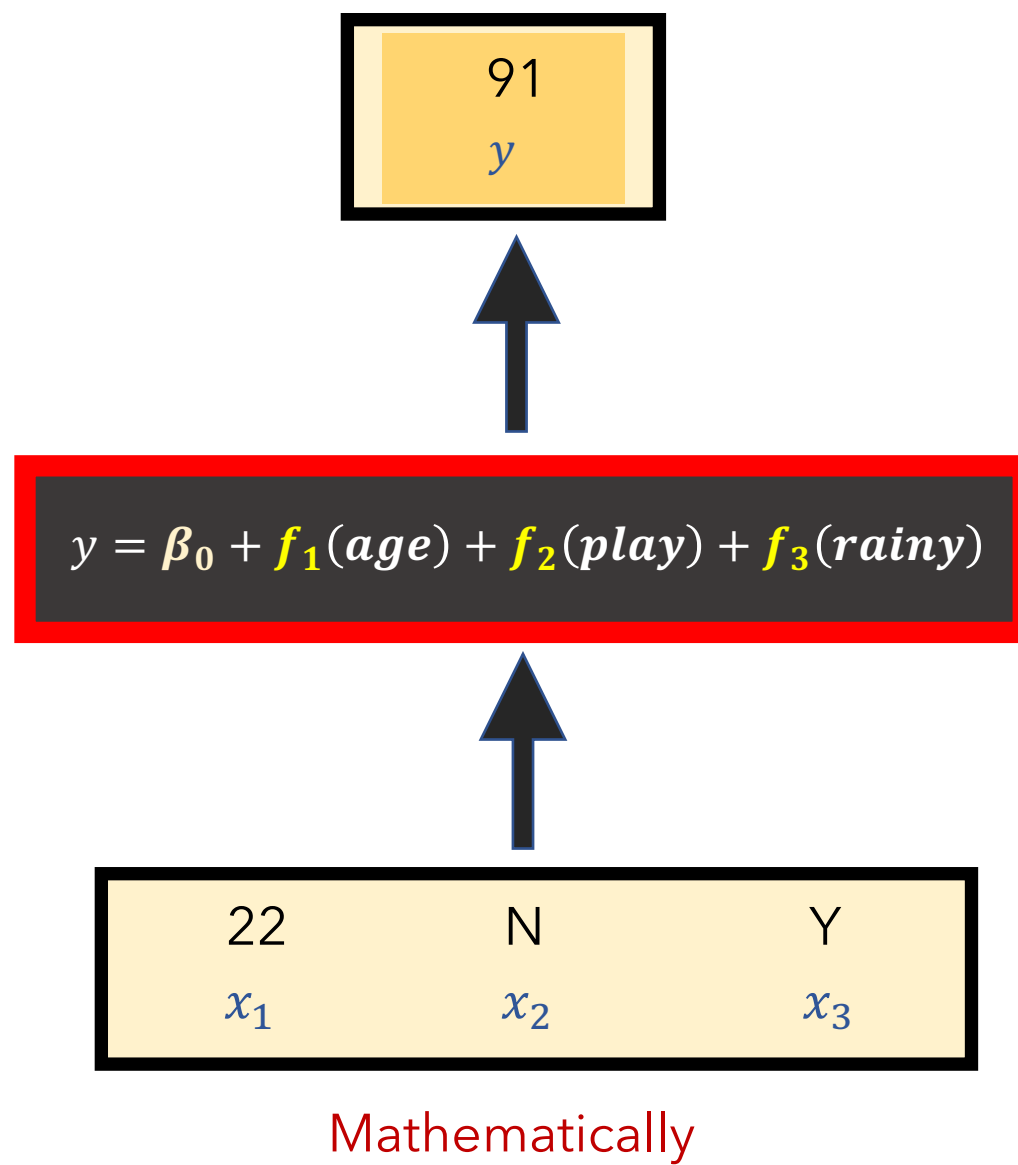
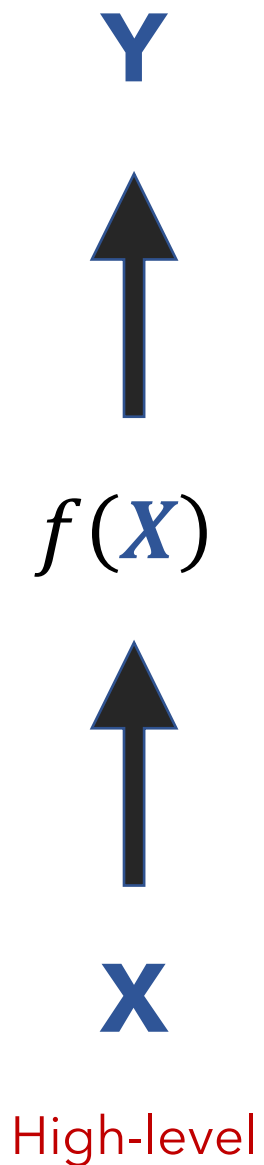
$$\text{Temp} = \beta_0 + f_1(\text{age}) + f_2(\text{play}) + f_3(\text{rainy})$$

Not our data, but imagine  
it's plotting **age** vs **Temp**:

Piecewise linear spline with knots at  $x=2, 5,$  and  $8$   
plus a starting slope and intercept



# Generalized Additive Models (GAMs)





# Generalized Additive Models (GAMs)

It is called an additive model because we calculate a separate  $f_i$  for each  $x_i$ , and then add together all of their contributions.

$$y = \beta_0 + f_1(\text{age}) + f_2(\text{play}) + f_3(\text{rainy})$$

$f(X)$

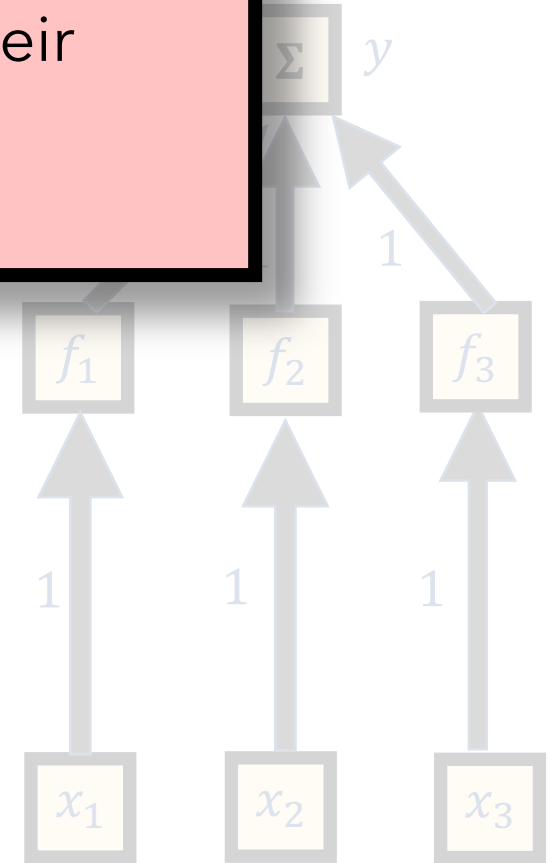


$X$

High-level

22	N	Y
$x_1$	$x_2$	$x_3$

Mathematically



Graphically  
(NN format)

# Generalized Additive Models (GAMs)

It is called an additive model because we calculate a separate  $f_i$  for each  $x_i$ , and then add together all of their contributions.

$$y = \beta_0 + f_1(\text{age}) + f_2(\text{play}) + f_3(\text{rainy})$$

$f_i$  doesn't have to be a spline; can be any regression model

$f(X)$

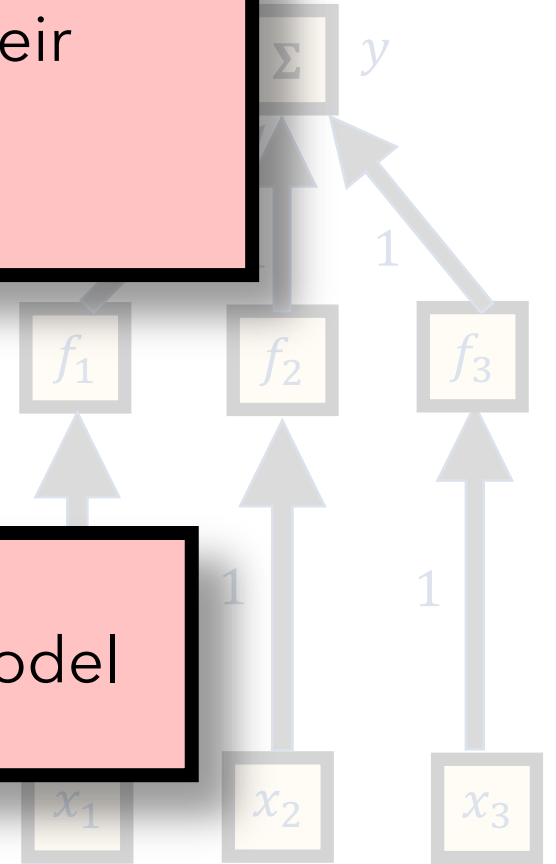


$X$

High-level

Mathematically

Graphically  
(NN format)



# Generalized Additive Models (GAMs)

## PROS

- Fits a **non-linear** function  $f_i$  to each feature  $x_i$
- Much easier than guessing polynomial terms and multinomial interaction terms.
- Model is additive, allowing us to exam the effects of each  $x_i$  on  $y$  by holding the other features  $x_{j \neq i}$  constant
- The smoothness is easy to adjust

## CONS

- Restricted to being additive; important interactions may not be captured
- Providing interactions via  $f_1(\mathit{age}, \mathit{rainy})$  can only capture so much, a la multinomial interaction terms

**Supervised vs  
Unsupervised**

**Regression vs  
Classification**

**Parametric vs  
Non-Parametric**

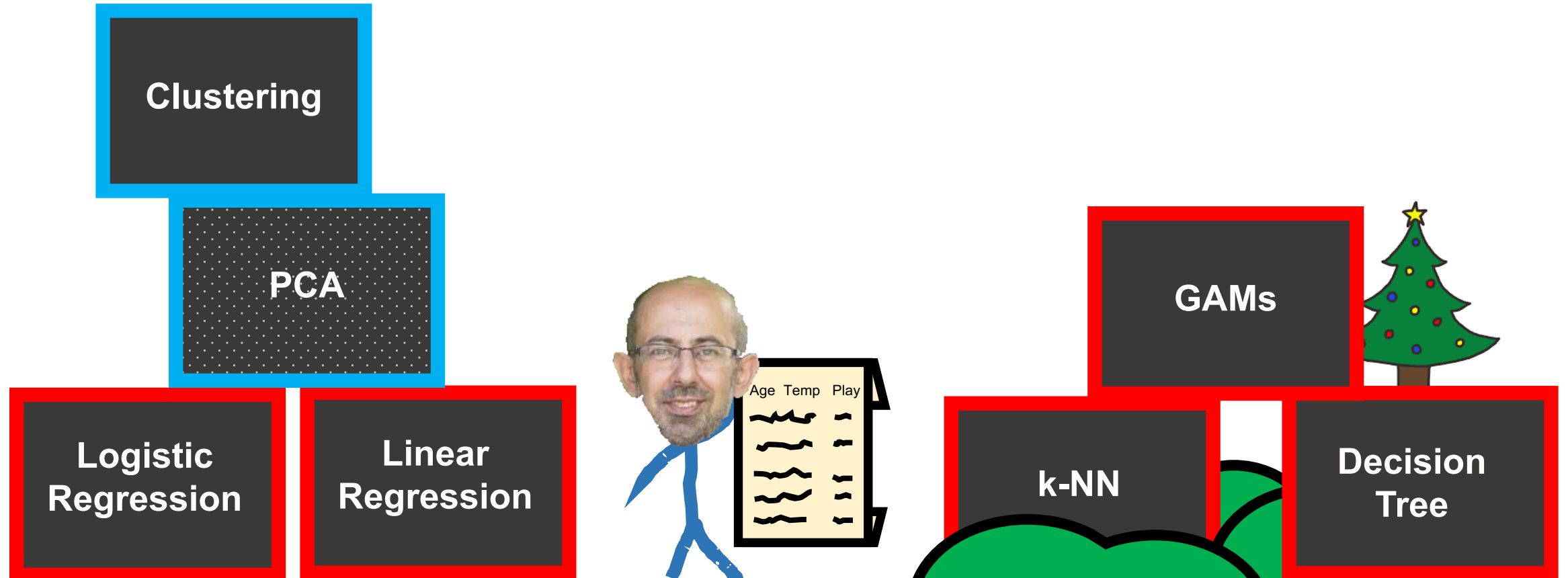
**Generative vs  
Discriminative**

Linear Regression	<b>Supervised</b>	<b>Regression</b>	<b>Parametric</b>	<b>Discriminative</b>
Logistic Regression	<b>Supervised</b>	<b>Classification</b>	<b>Parametric</b>	<b>Discriminative</b>
k-NN	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
Decision Tree	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
PCA	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>neither</b>
Clustering	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>Generative</b>
GAMs	<b>Supervised</b>	<b>either</b>	<b>Parametric</b>	<b>Discriminative</b>

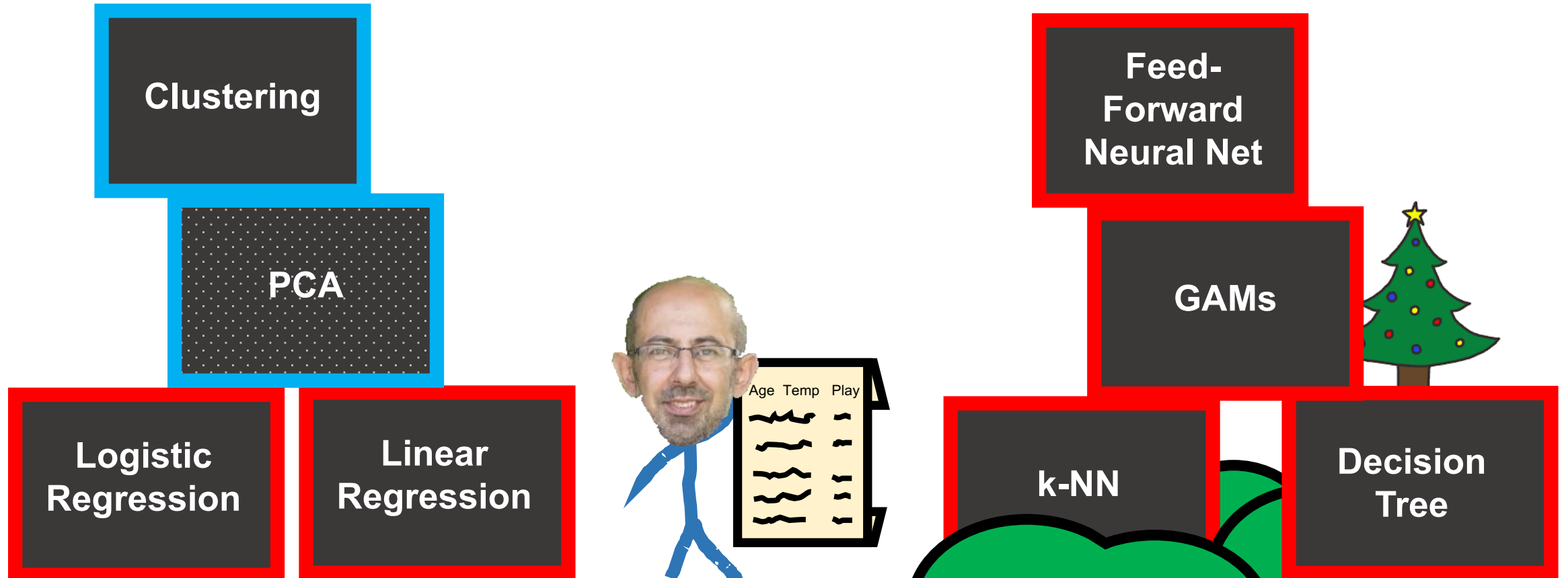
- Returning our data yet again, perhaps we've plotted our data **X** and see it's **non-linear**
- We further suspect that there are complex interactions that cannot be represented by polynomial regression and GAMs
- We just want great results and don't care about interpretability

<b>X</b>			<b>Y</b>
<b>Age</b>	<b>Temp</b>	<b>Rainy</b>	<b>Play</b>
22	91	Y	N
29	89	N	Y
31	56	N	N
23	71	N	Y
37	72	Y	N
41	83	N	Y
29	97	Y	Y
21	64	N	N
30	68	N	Y

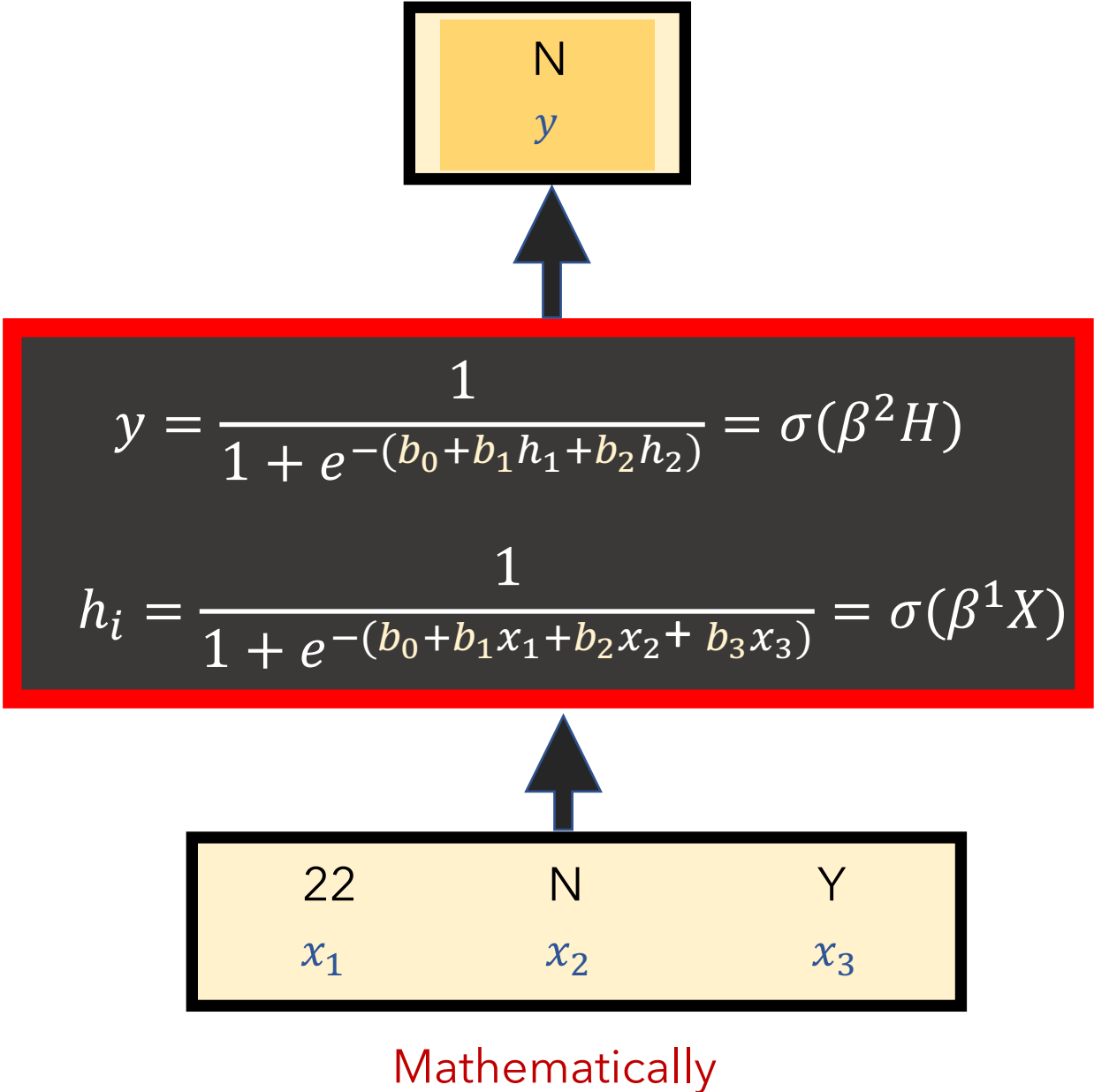
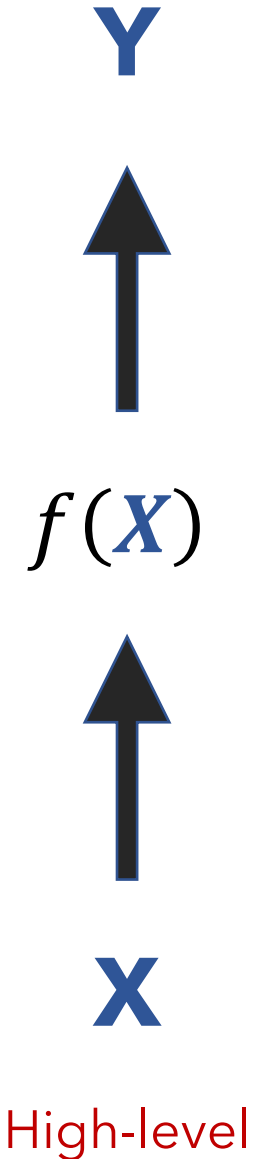
# Playground of Models



# Playground of Models



# Feed-Forward Neural Network





# Feed-Forward Neural Network

Y

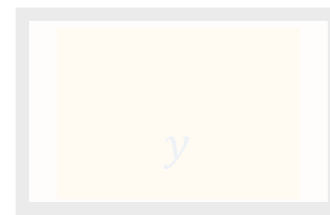


$f(\mathbf{X})$



X

High-level





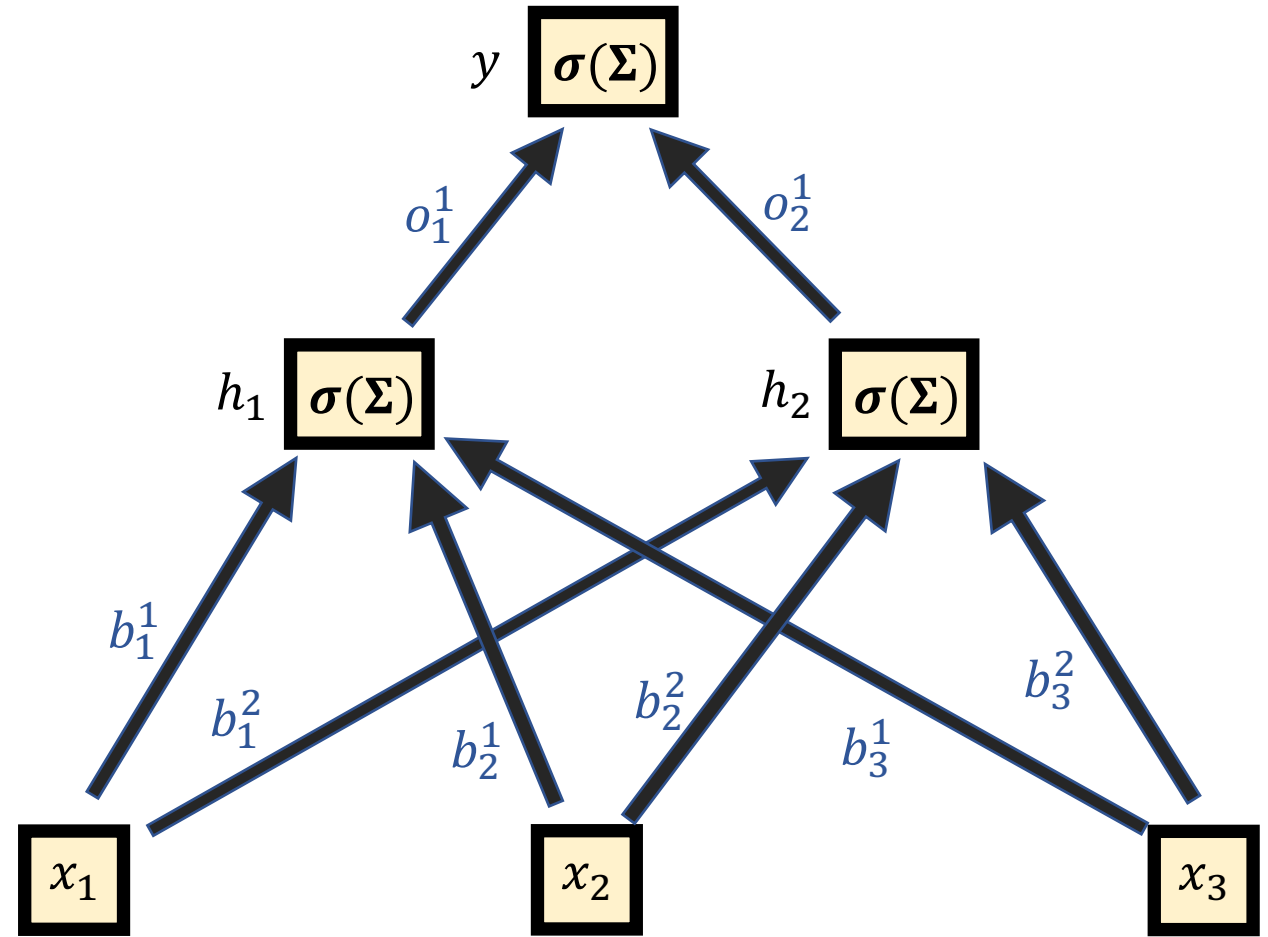
$$y = \frac{1}{1 + e^{-(b_0 + b_1 h_1 + b_2 h_2)}} = \sigma(\beta^2 H)$$
$$h_i = \frac{1}{1 + e^{-(b_0 + b_1 x_1 + b_2 x_2 + b_3 x_3)}} = \sigma(\beta^1 X)$$

**NOTE: a Neural Network can be viewed as a function  $f(\mathbf{X})$ , just like all of our past models**

# Feed-Forward Neural Network

## General Notes:



- It's a fully connected network
- Every  is a weight, which is multiplied by its input
- Every  is a scalar value
- Parameters  $\theta = \{\beta, O\}$  (weights)



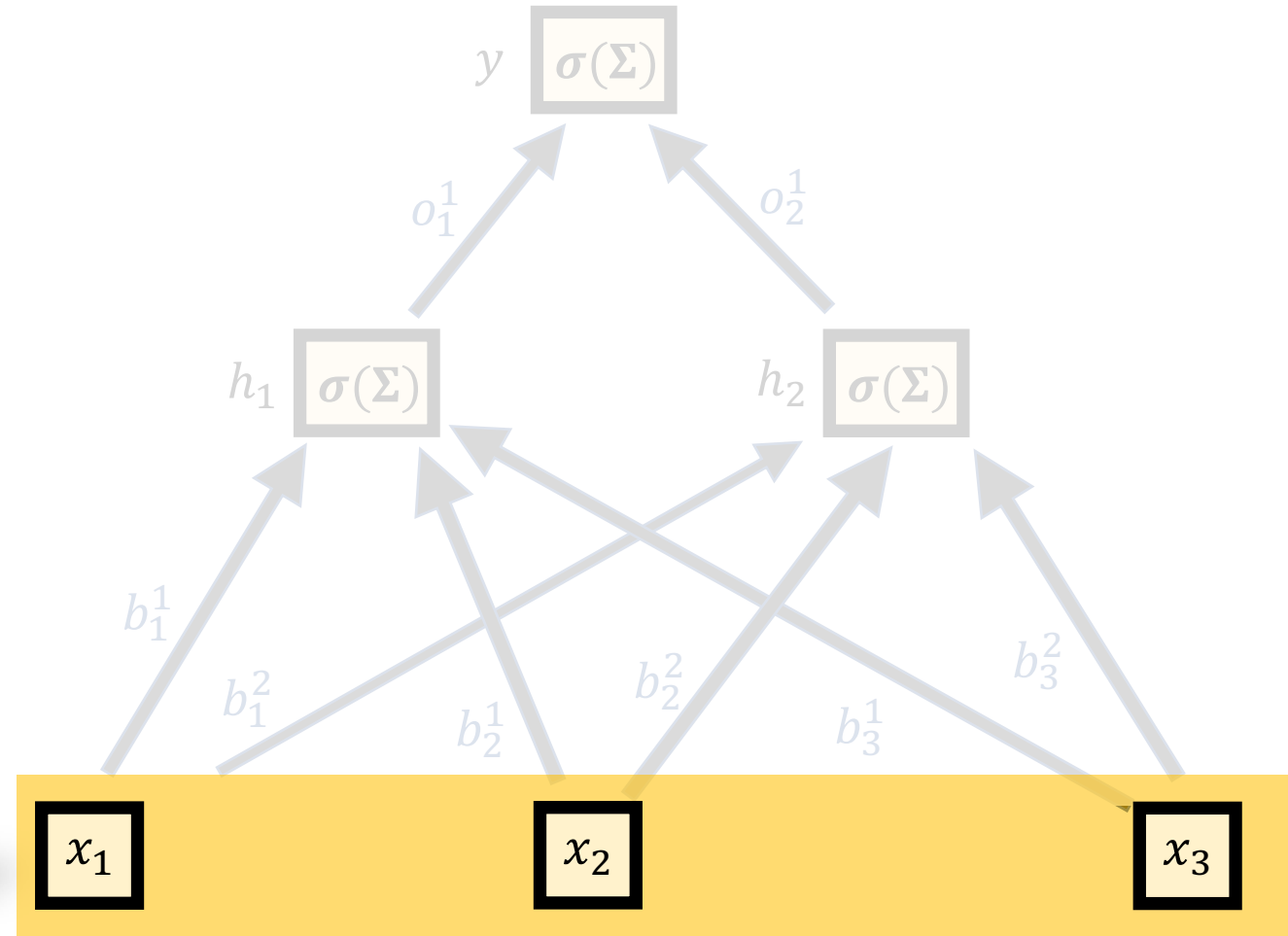
Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:

- It's a fully connected network
- Every  is a weight, which is multiplied by its input
- Every  is a scalar value
- Parameters  $\theta = \{\beta, O\}$  (weights)


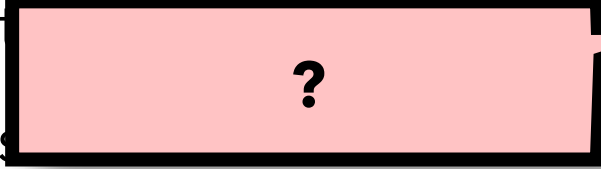

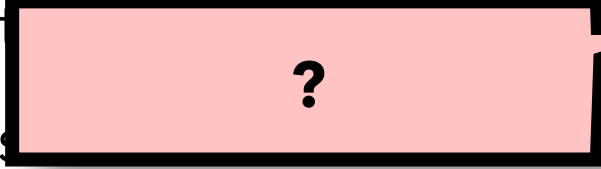
Input layer

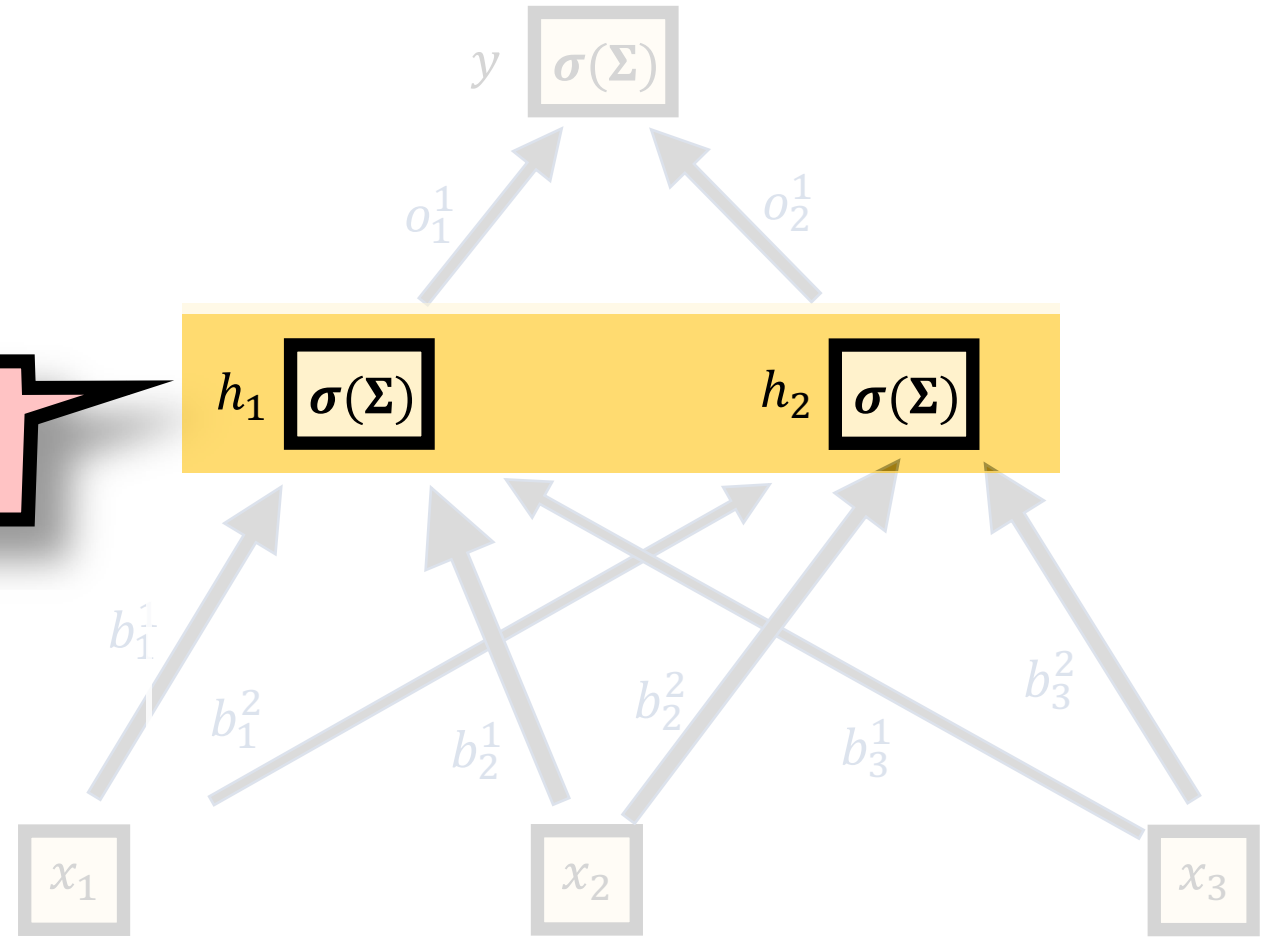


Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:



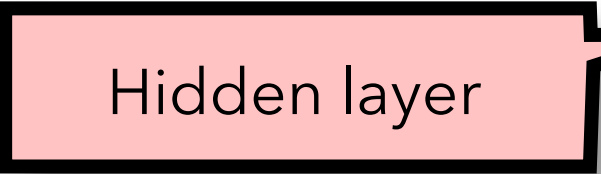
- It's a fully connected network
- Every  is a weight, which is multiplied by 
- Every  is a 
- Parameters  $\theta = \{\beta, O\}$  (weights)

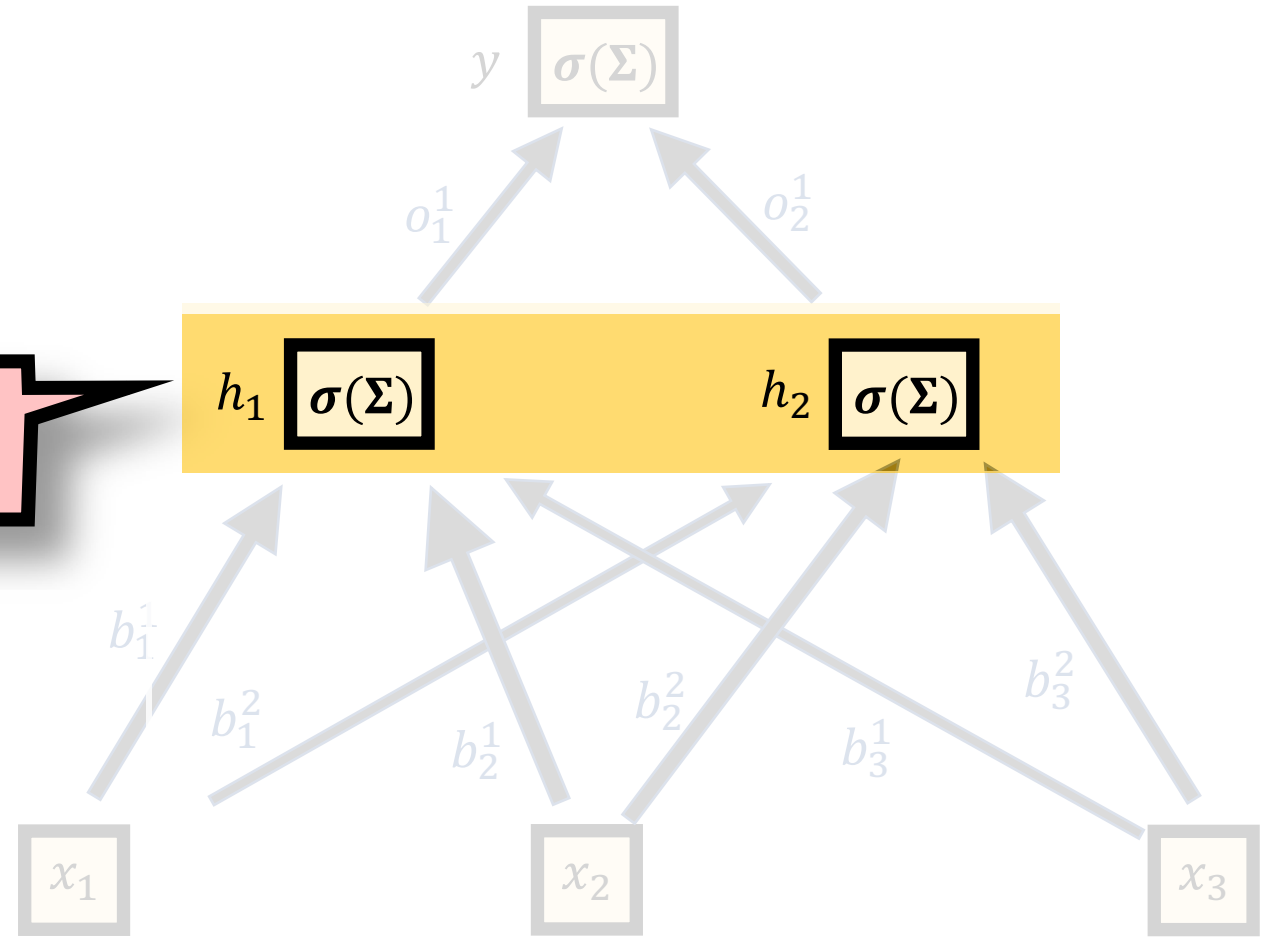


Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:



- It's a fully connected network
- Every  is a weight, which is multiplied
- Every  is a  Hidden layer
- Parameters  $\theta = \{\beta, O\}$  (weights)

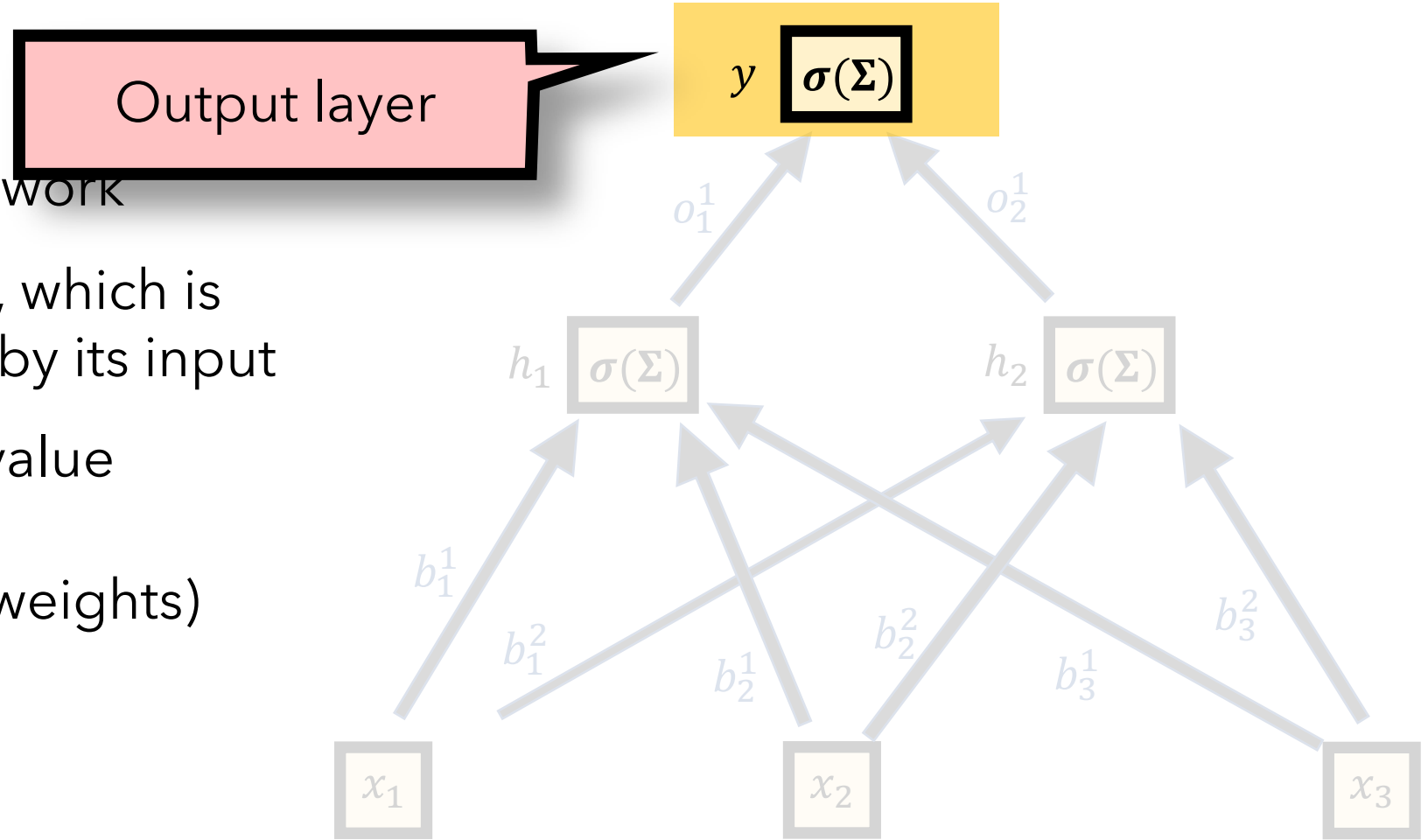


Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:



- It's a fully connected network
- Every  is a weight, which is multiplied by its input
- Every  is a scalar value
- Parameters  $\theta = \{\beta, O\}$  (weights)

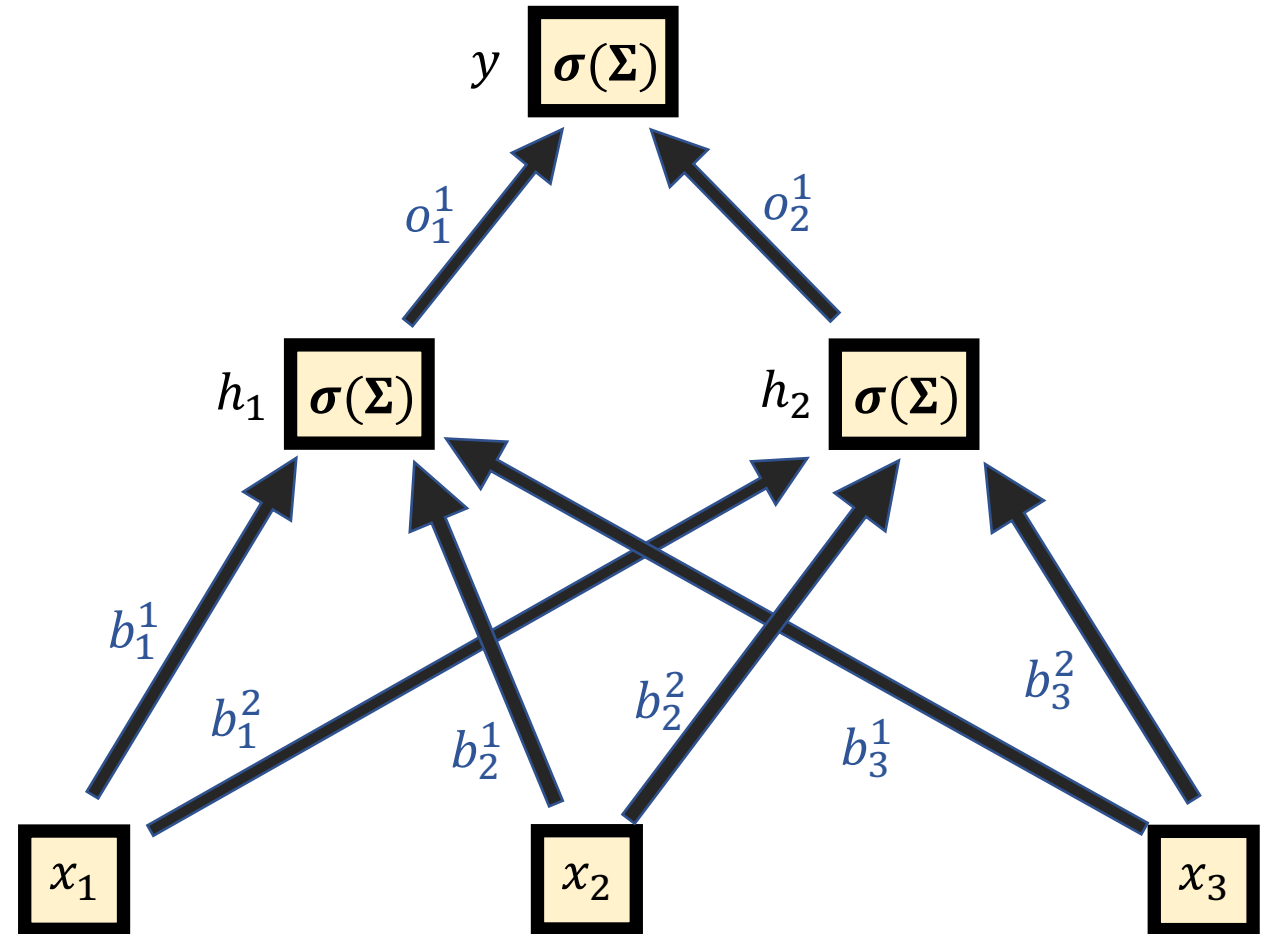


Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:



- It's a fully connected network
- Every  is a weight, which is multiplied by its input
- Every  is a scalar value
- Parameters  $\theta = \{\beta, O\}$  (weights)

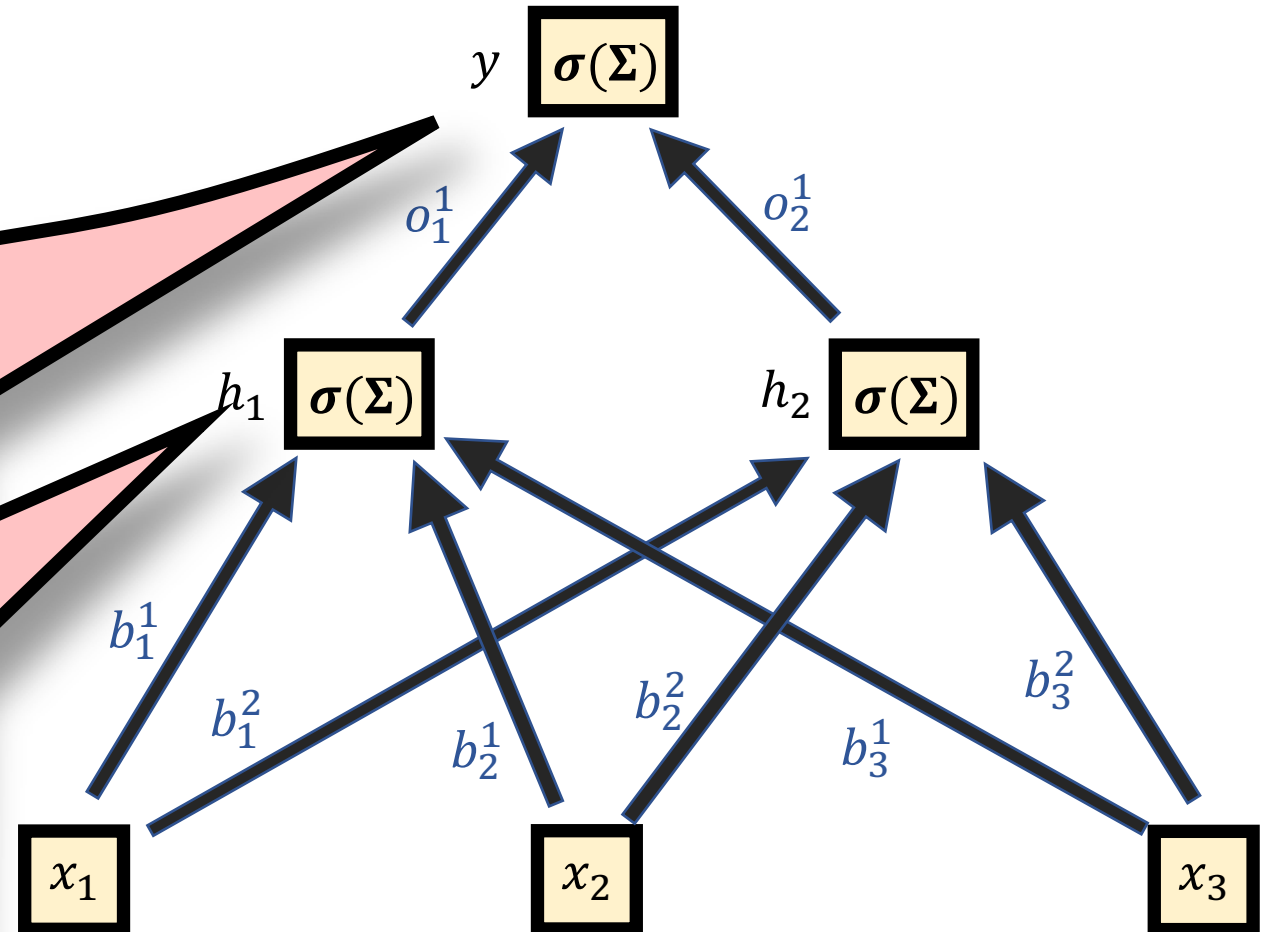


Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:

- It's a fully connected network
- Every , except for the input layer's, is called an **activation function**.
- Every  takes input(s), apply some aggregate operation(s) -- often a **non-linear transformation** -- and yield a scalar value.
- Pa




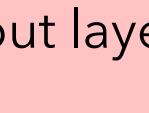
Graphically  
(NN format)

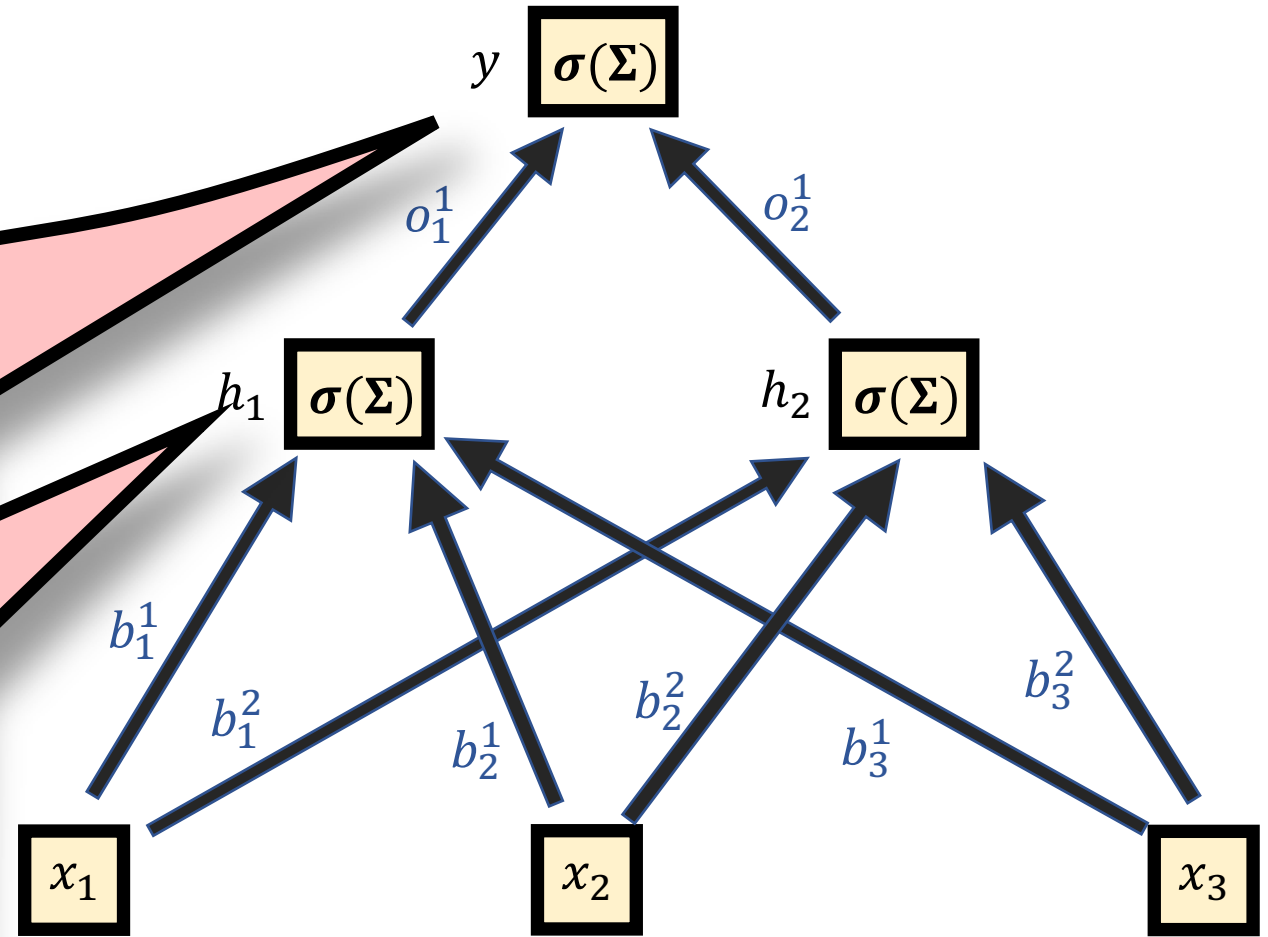


# Feed-Forward Neural Network

## General Notes:

- It's a fully connected network



- Every , except for the input layer's, is called an **activation function**.
- Every  is called a **neuron**.
- Parameters are  $w$  and  $b$ . The sigmoid function  $\sigma$  is a common choice and is equivalent to performing **logistic regression** on its given inputs.

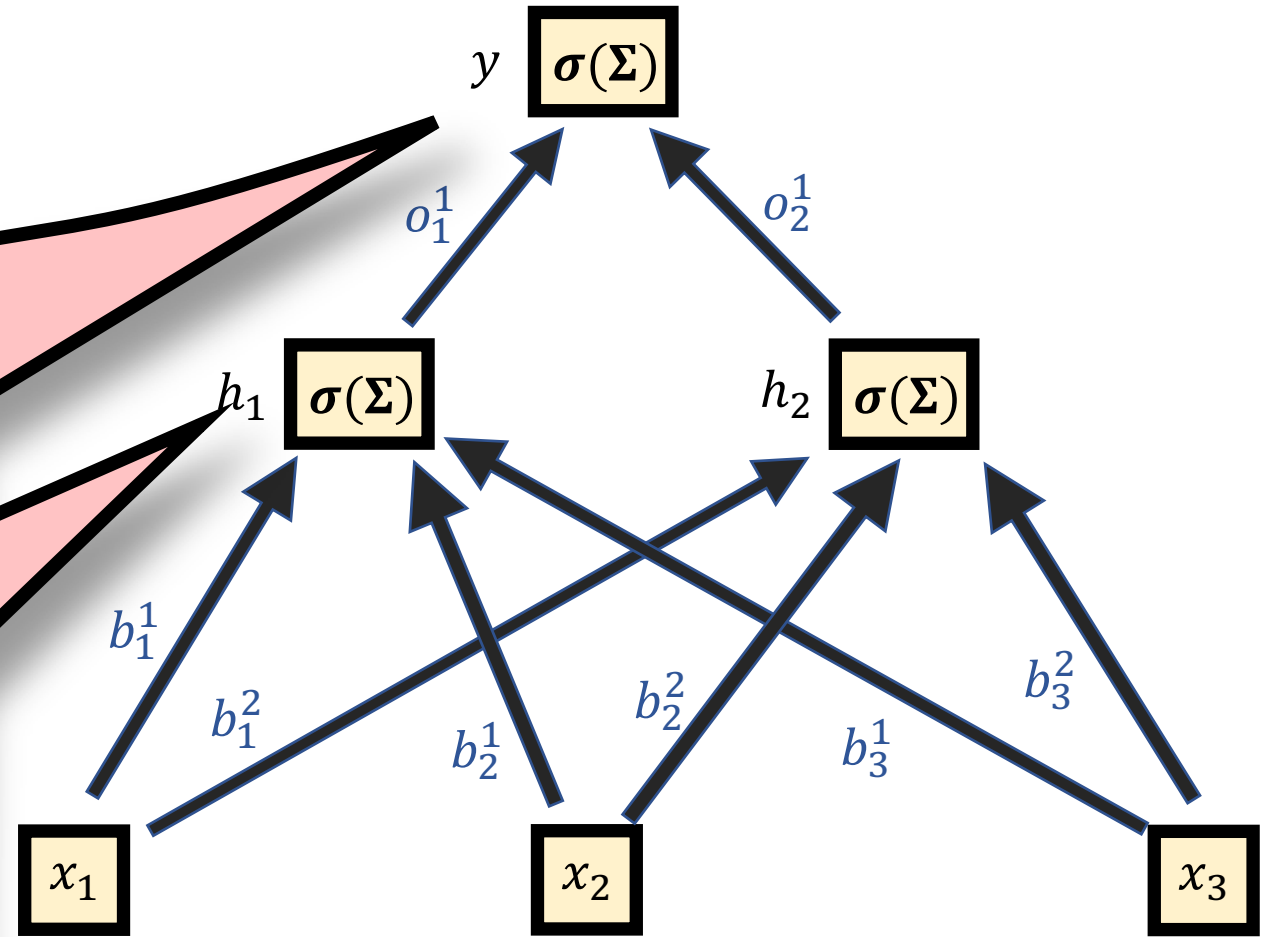


Graphically  
(NN format)

# Feed-Forward Neural Network

## General Notes:

- It's a fully connected network
  - Every , except for the input layer's, is called an **activation function**.
  - Every  is called a **neuron**.
  - Parameters are weights and biases.
- Thus, neural nets can be viewed as being a fully-connected set of logistic regressions, oftentimes stacked (multiple hidden layers)

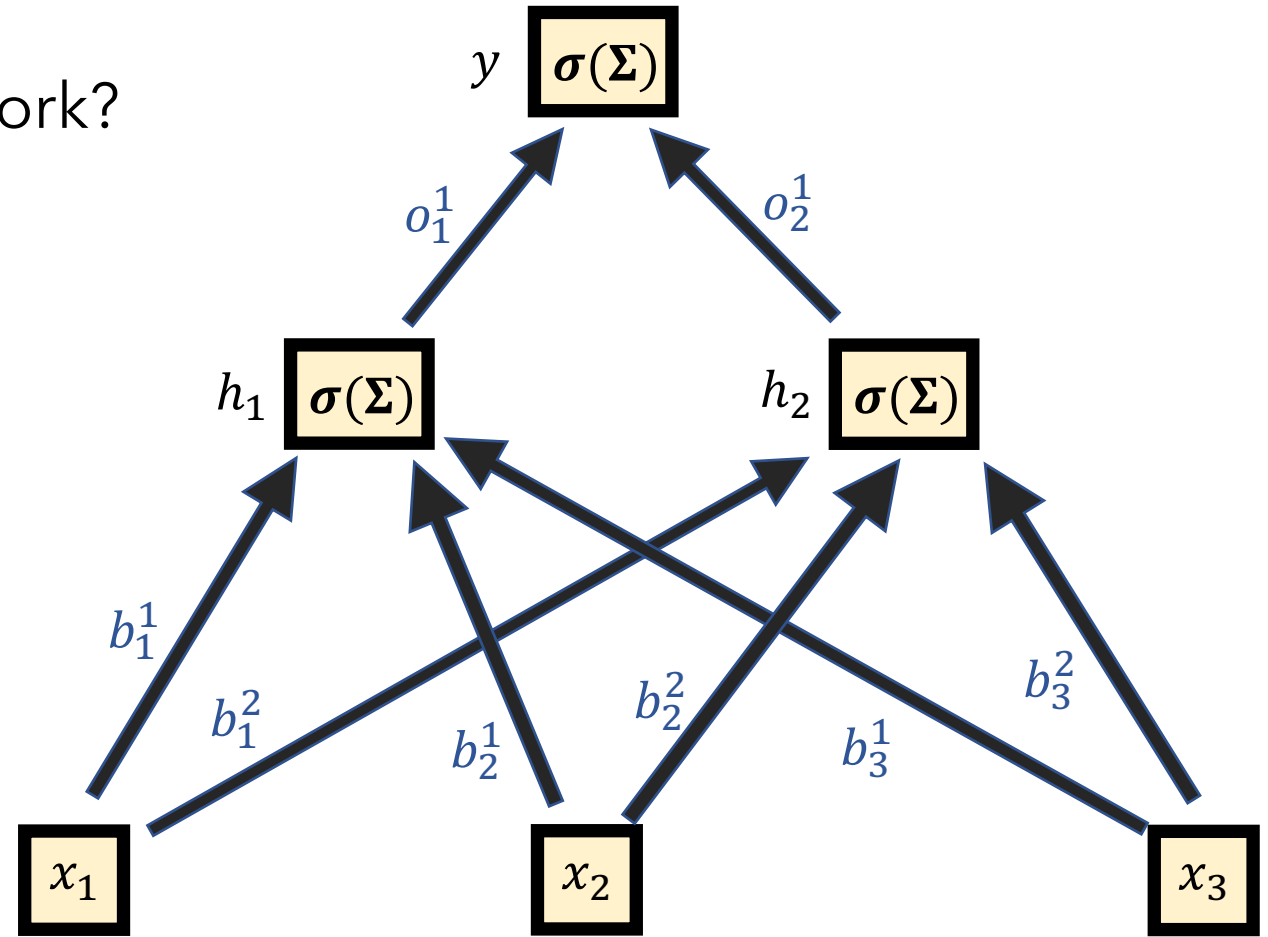


Graphically  
(NN format)

# Feed-Forward Neural Network

## Training:

- **Q1** How do we train a neural network?



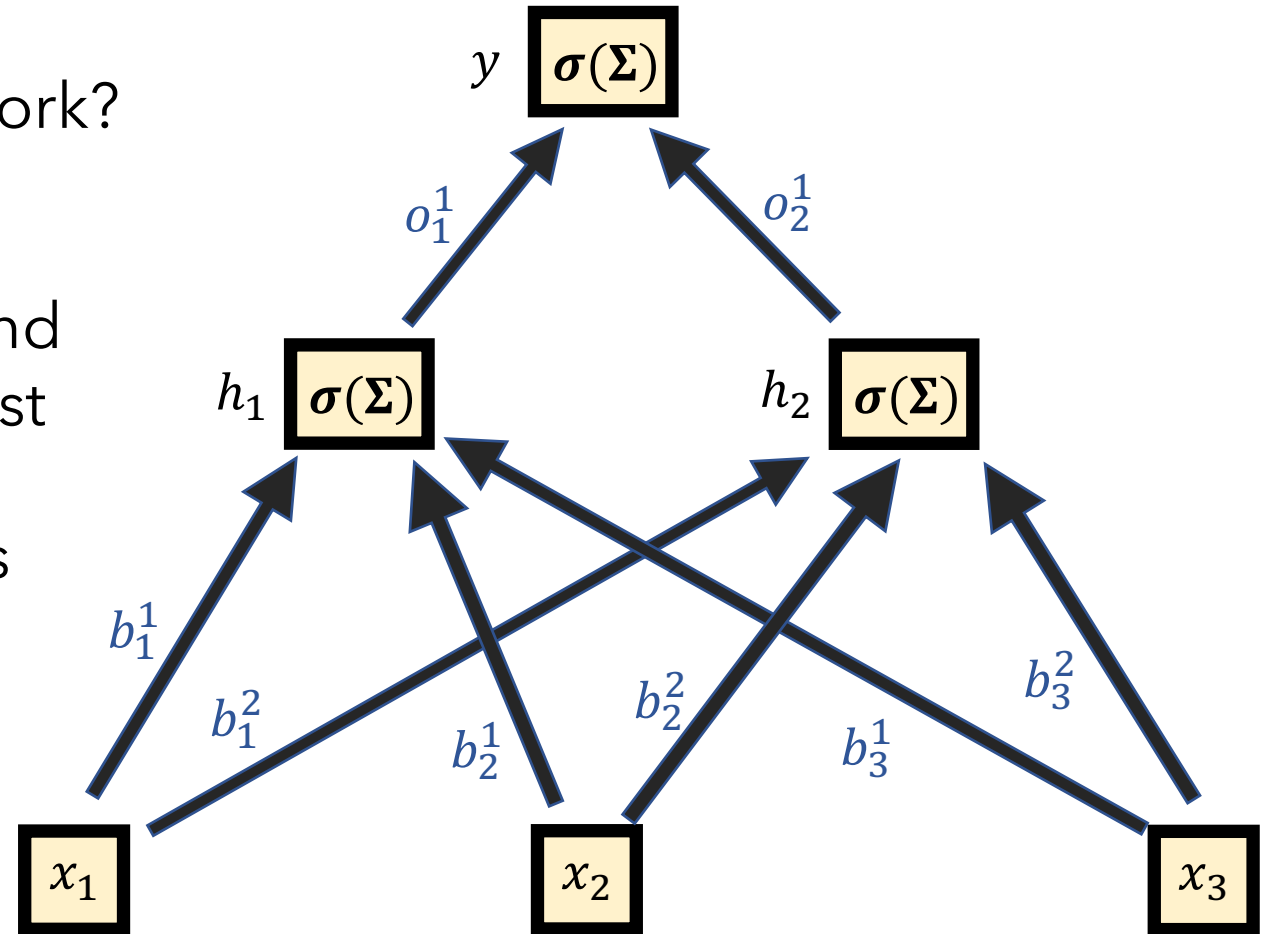
Graphically  
(NN format)

# Feed-Forward Neural Network

## Training:

- **Q1** How do we train a neural network?

**A1** First, specify a **cost function** and an **optimization algorithm**, just like we did for our other supervised, parametric models



Graphically  
(NN format)

# Feed-Forward Neural Network

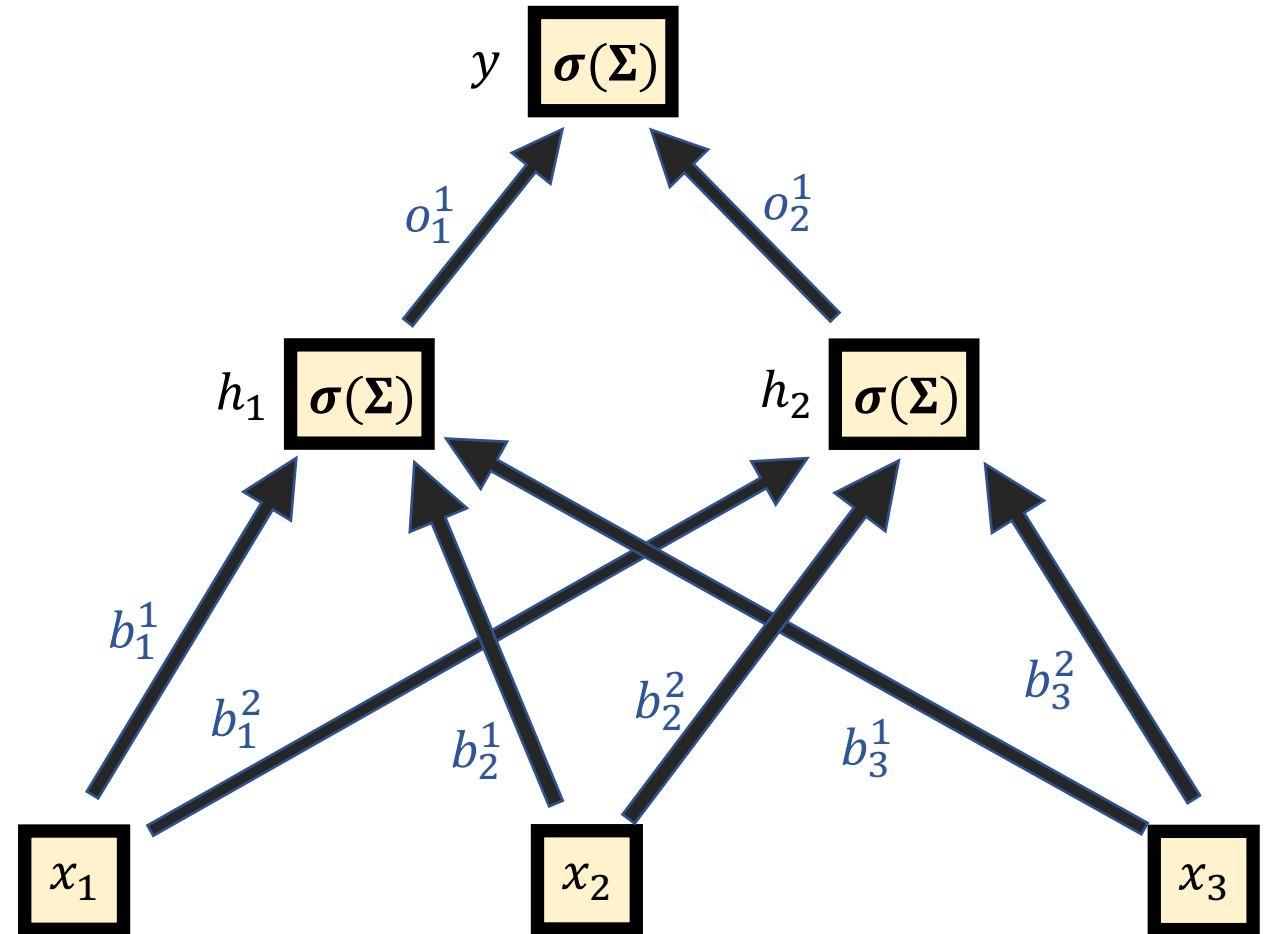
## Training:

Cost function

$$J(\theta) = -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]$$

"Cross-Entropy" aka "Log loss"

Update the  $\theta$  via  
**gradient descent**



Graphically  
(NN format)

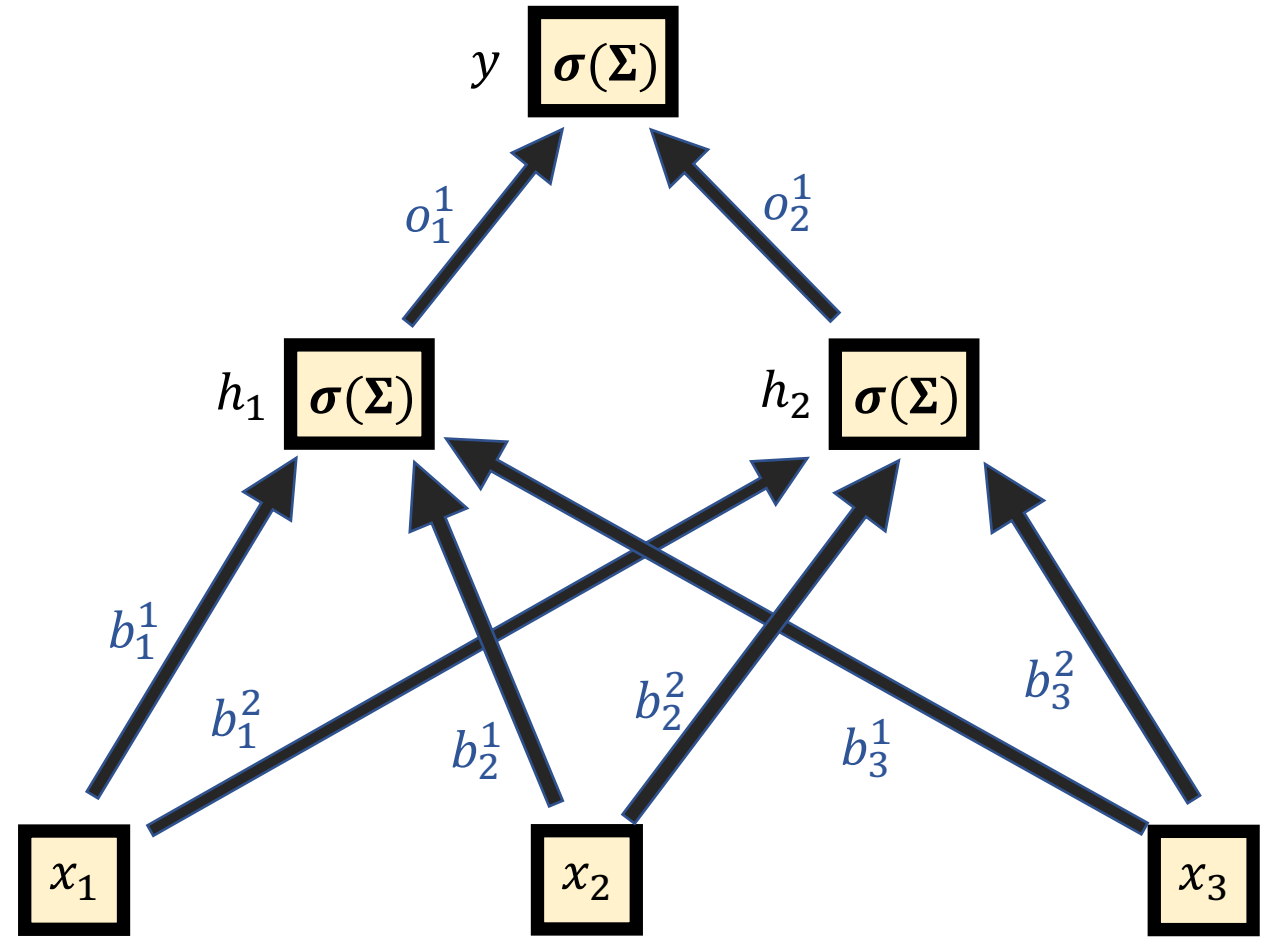
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss
4. Calculate gradients via **backpropagation**
5. Update the weights (aka  $\theta$ ) via **gradient descent**

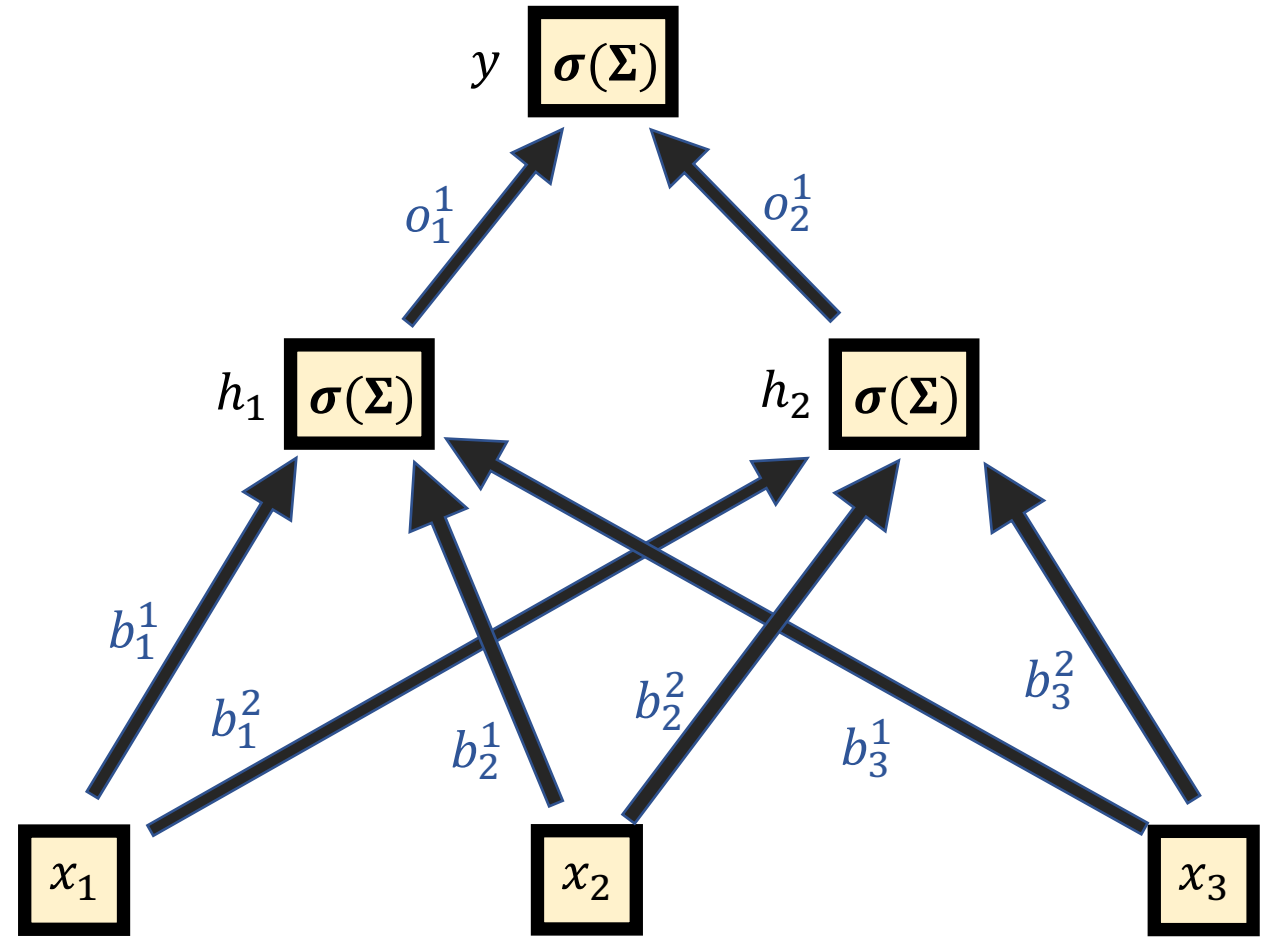


Graphically  
(NN format)

# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

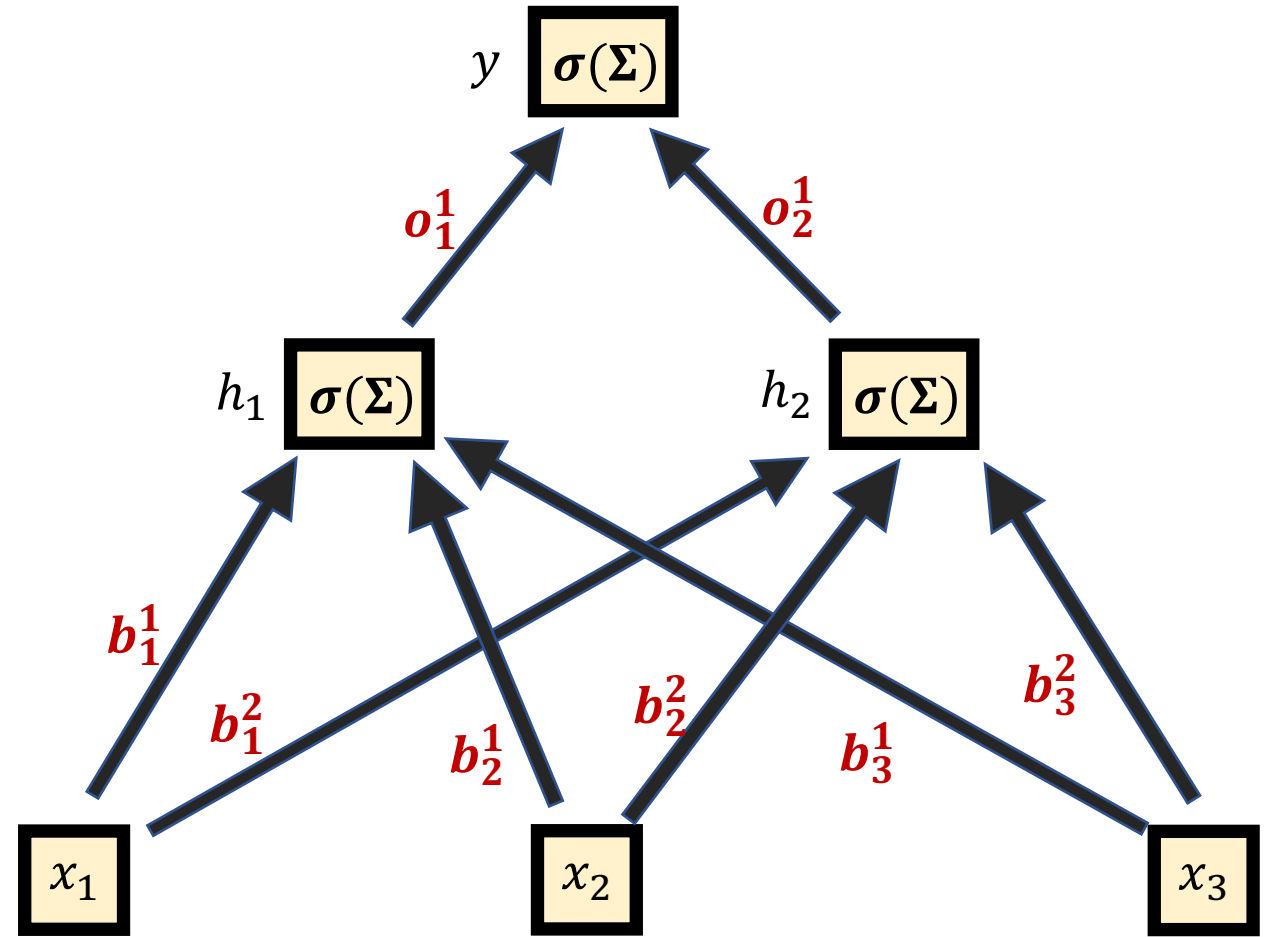


Graphically  
(NN format)

# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values



Graphically  
(NN format)



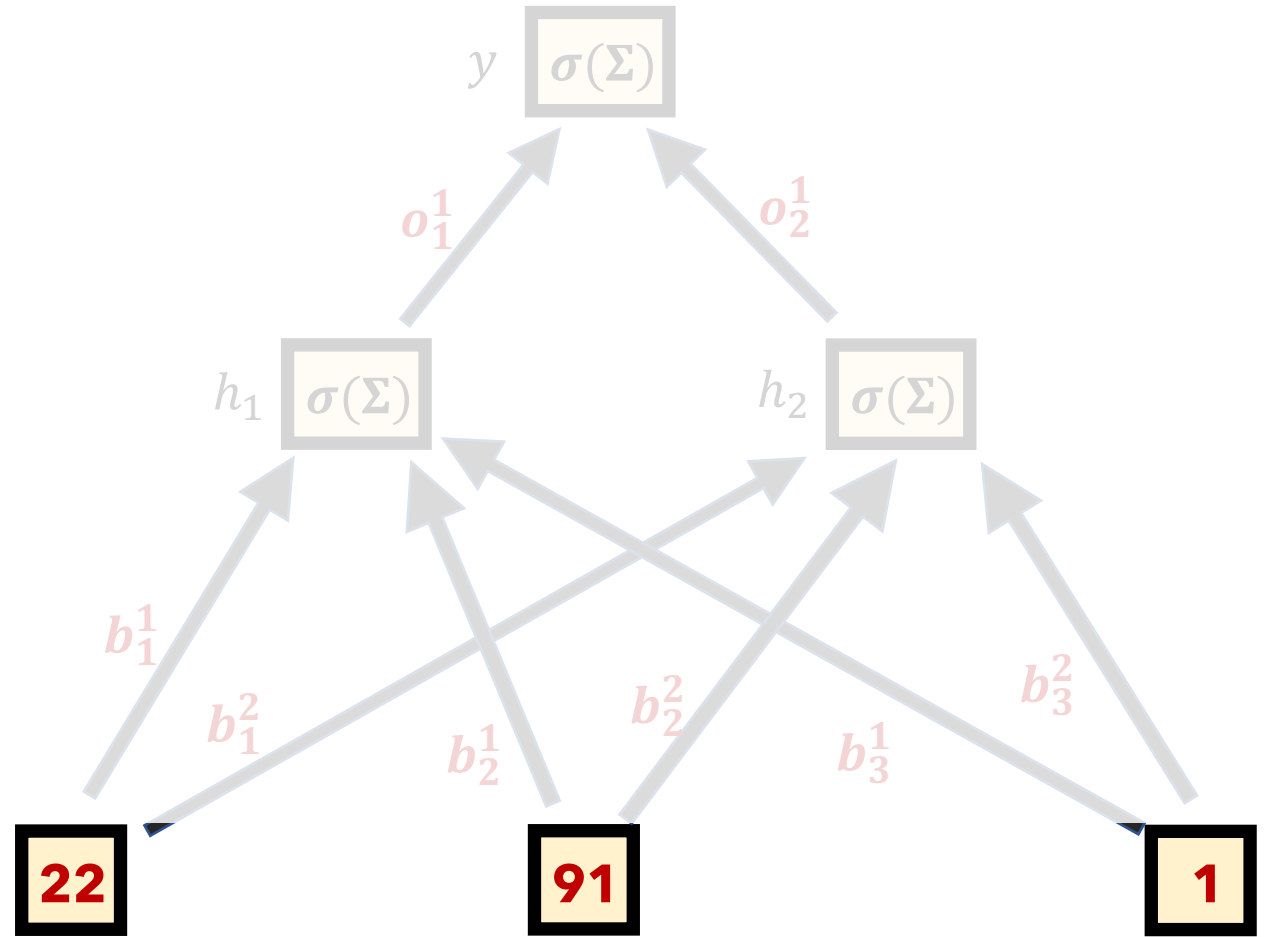
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network



Graphically  
(NN format)

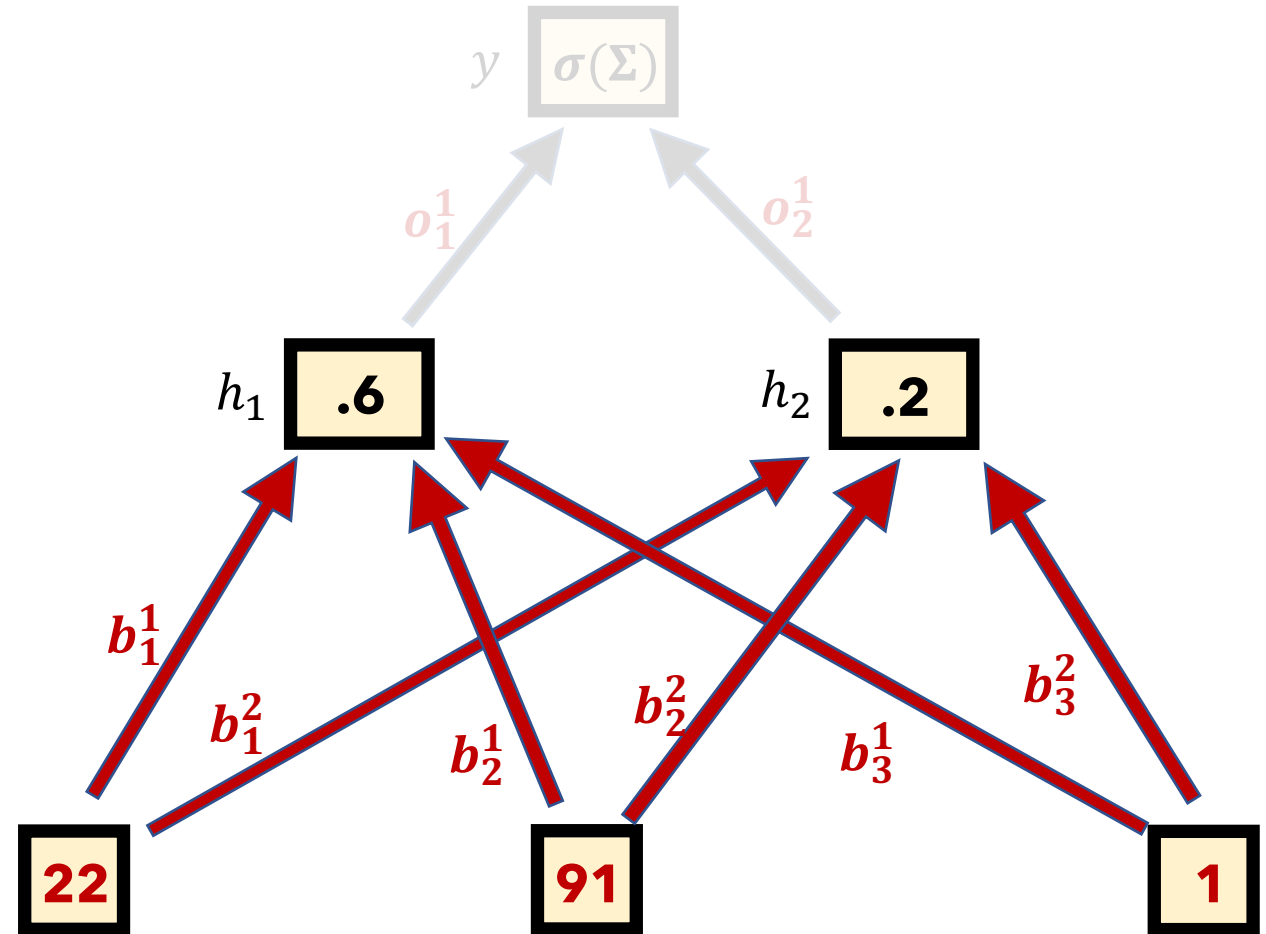
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network



Graphically  
(NN format)

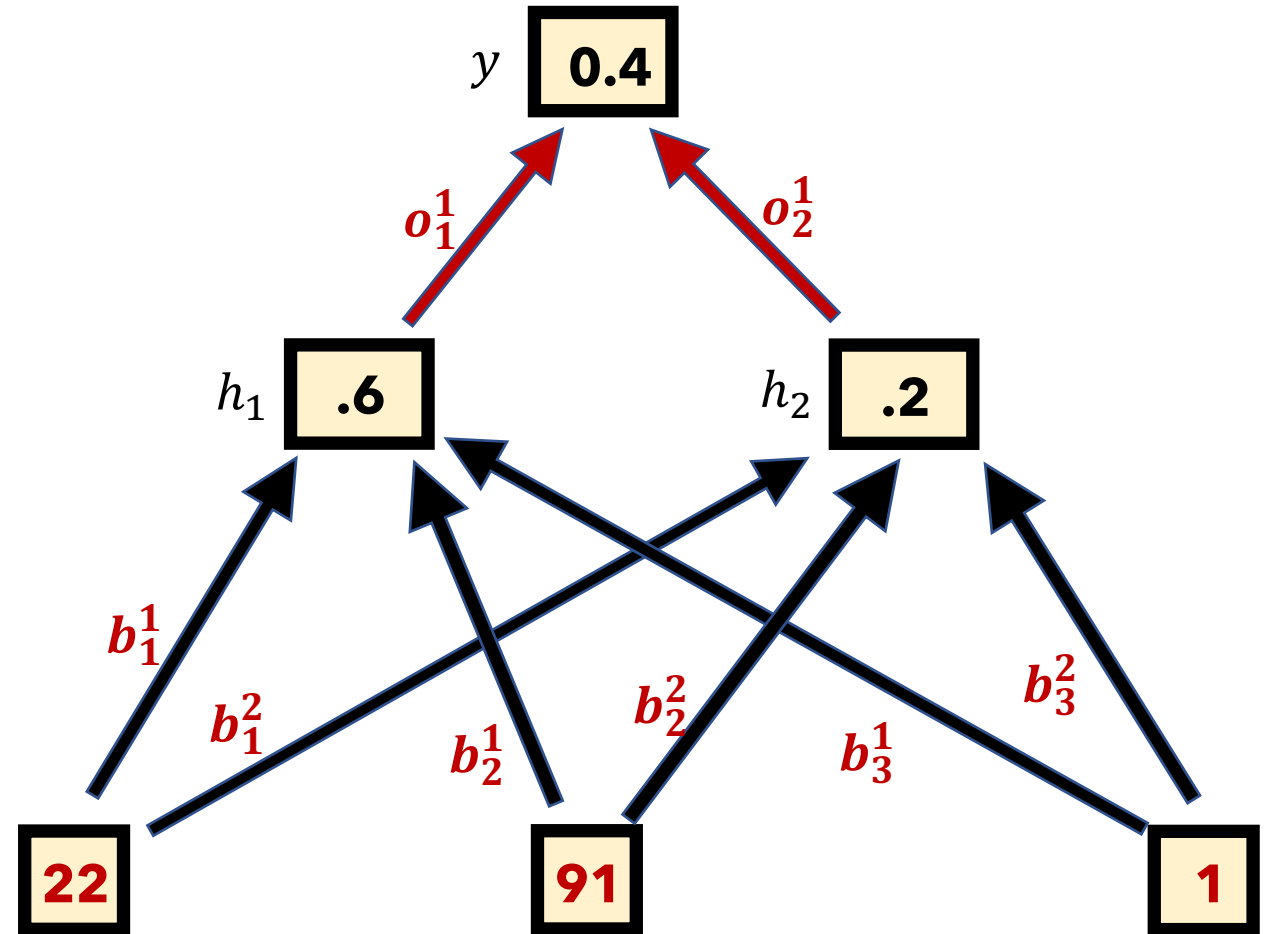
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network



Graphically  
(NN format)

# Feed-Forward Neural Network

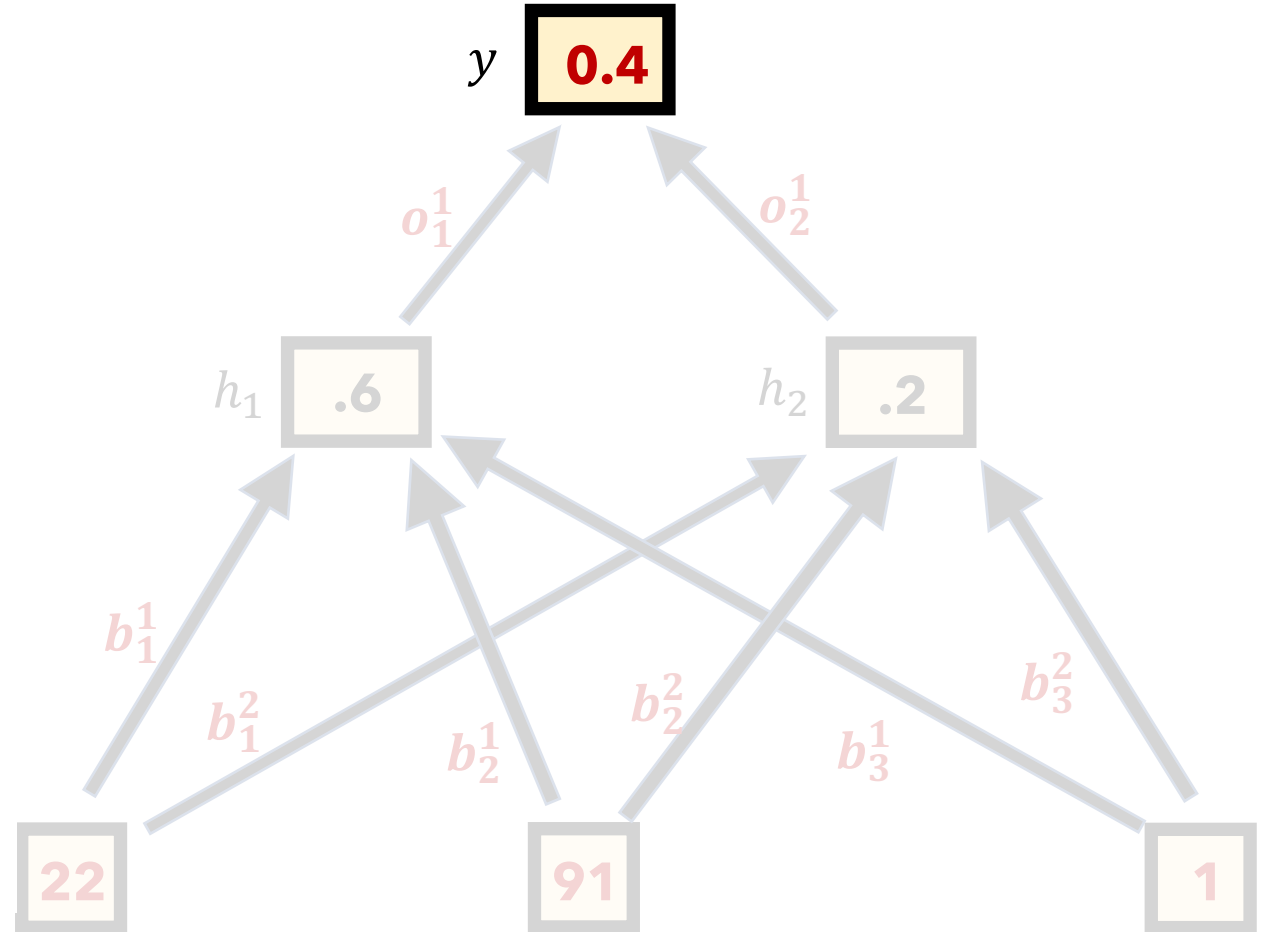
## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss

$$J(\theta) = -[y \log \hat{y} + (1 - y) \log(1 - \hat{y})]$$



Graphically  
(NN format)

# Feed-Forward Neural Network

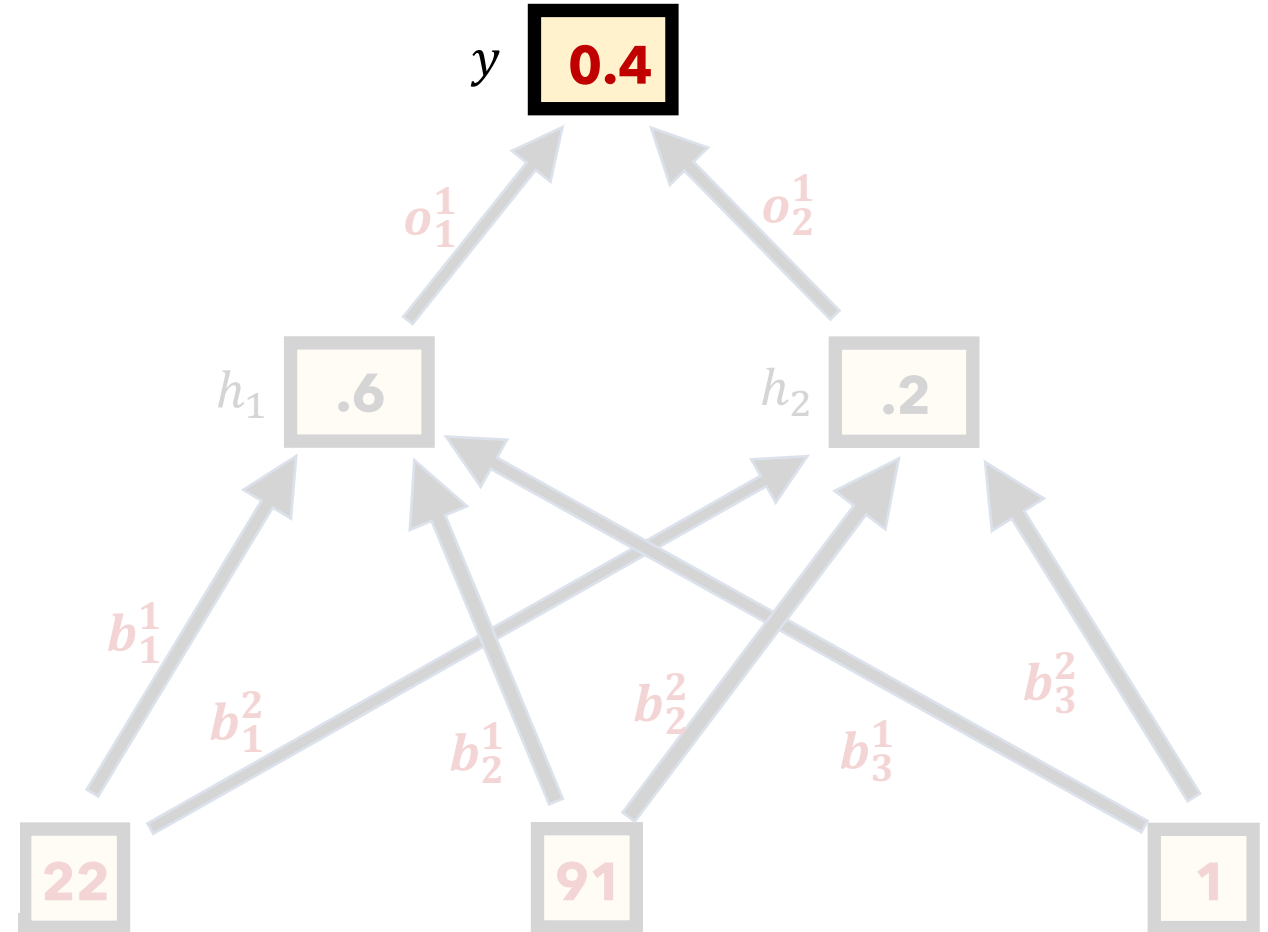
## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss

$$J(\theta) = -[0 + (1 - 0) \log(1 - 0.4)]$$



Graphically  
(NN format)

# Feed-Forward Neural Network

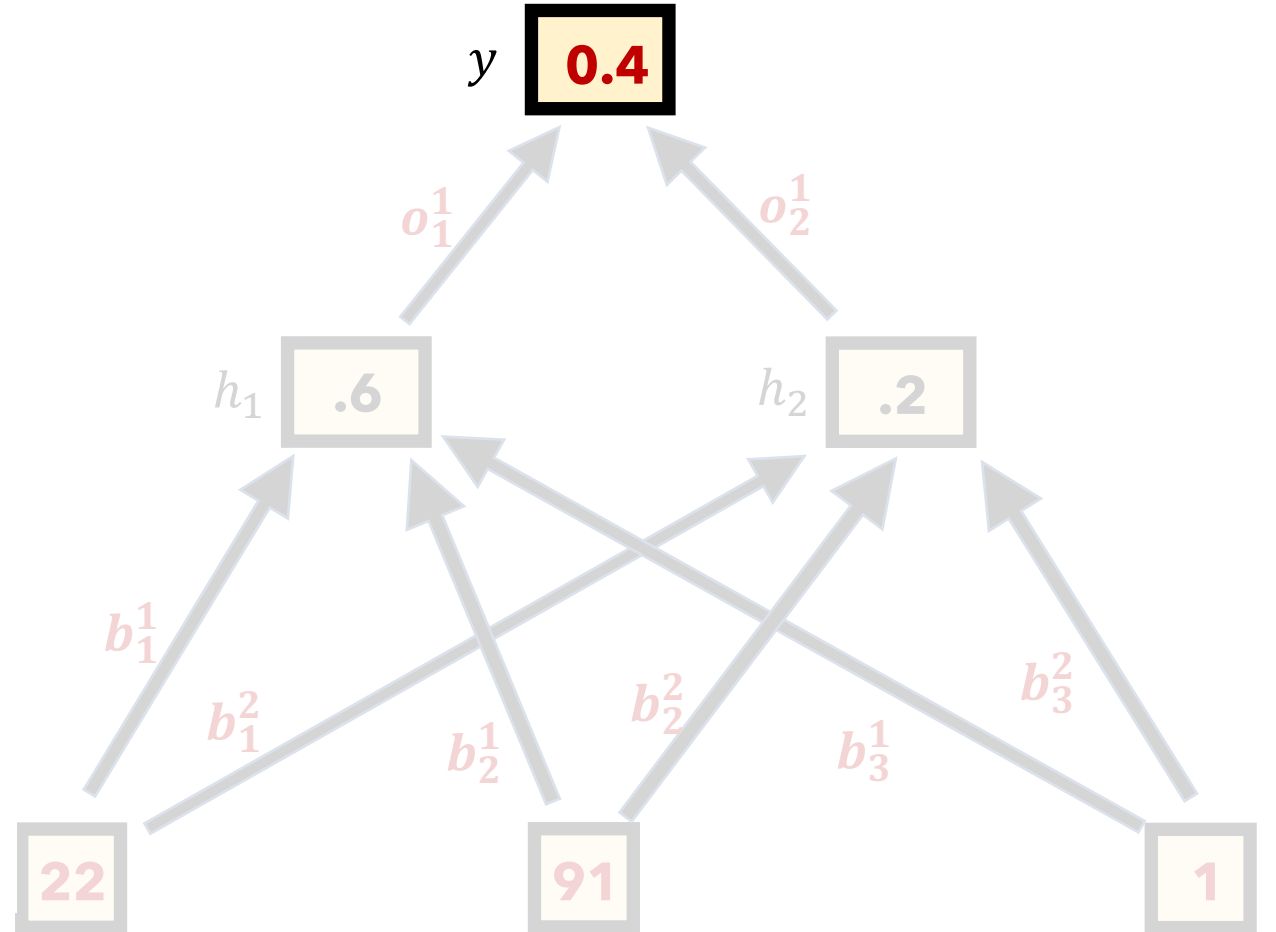
## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss

$$J(\theta) = -[0 + (1 - 0) \log(0.6)]$$



Graphically  
(NN format)

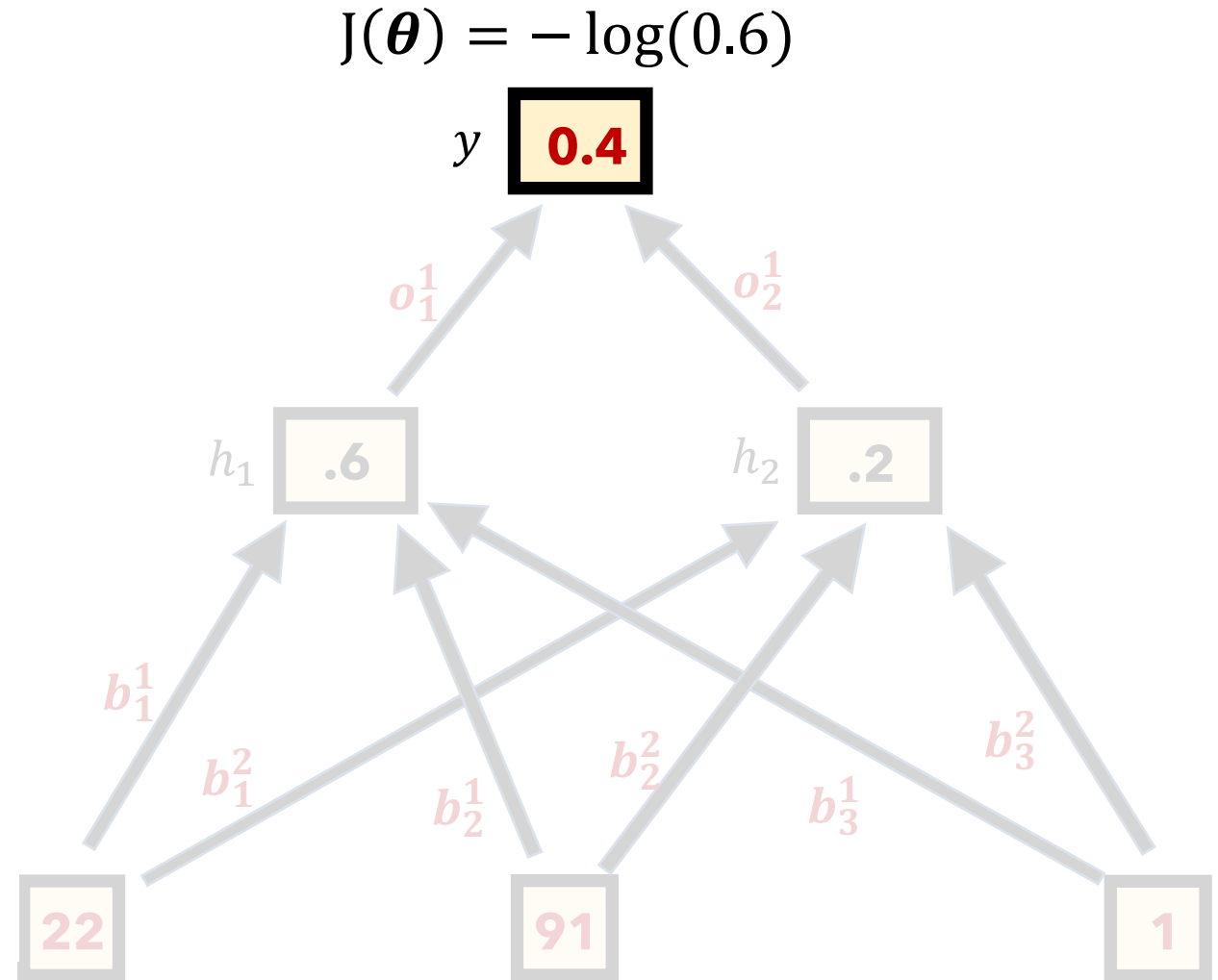
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss



Graphically  
(NN format)

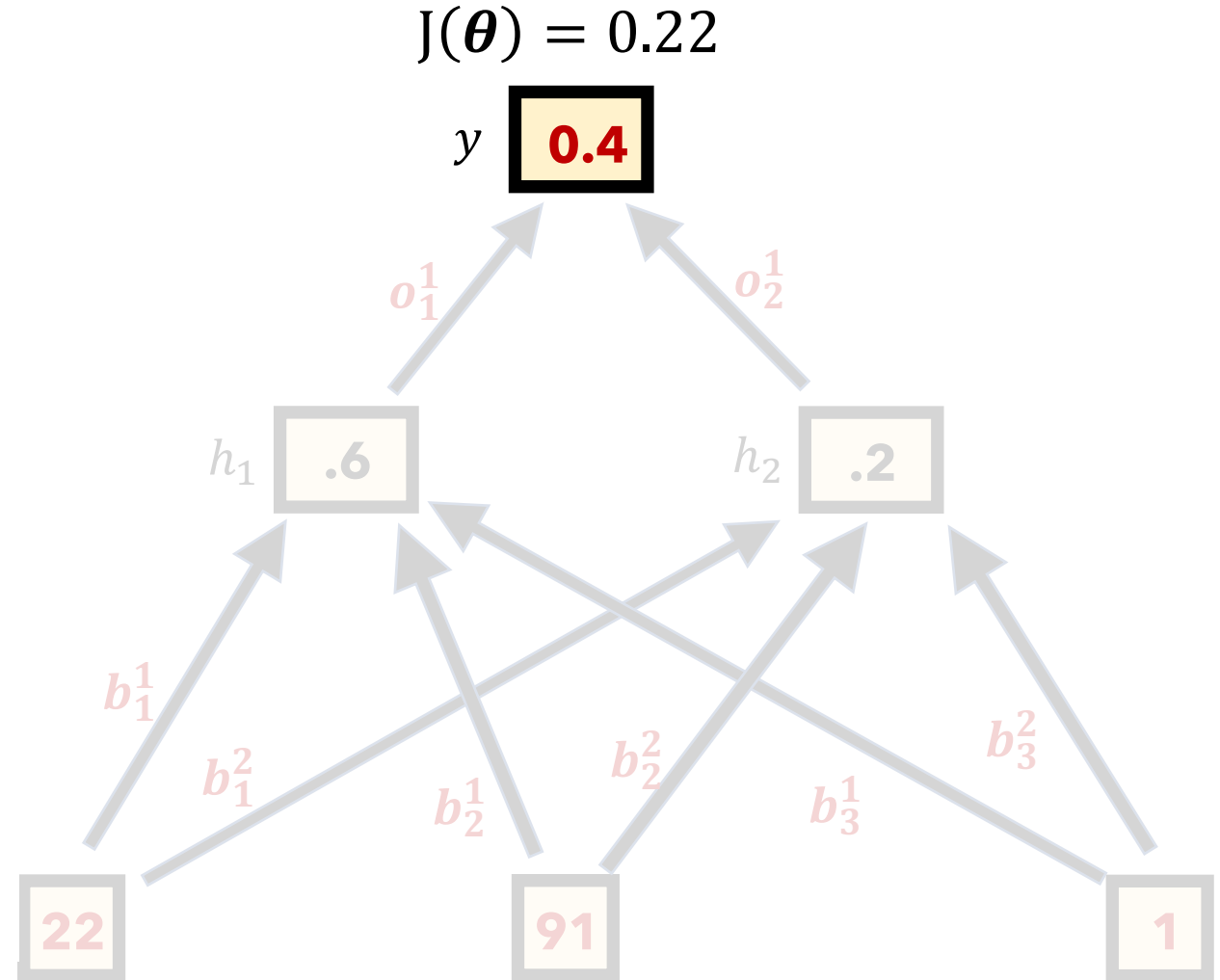
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss



Graphically  
(NN format)



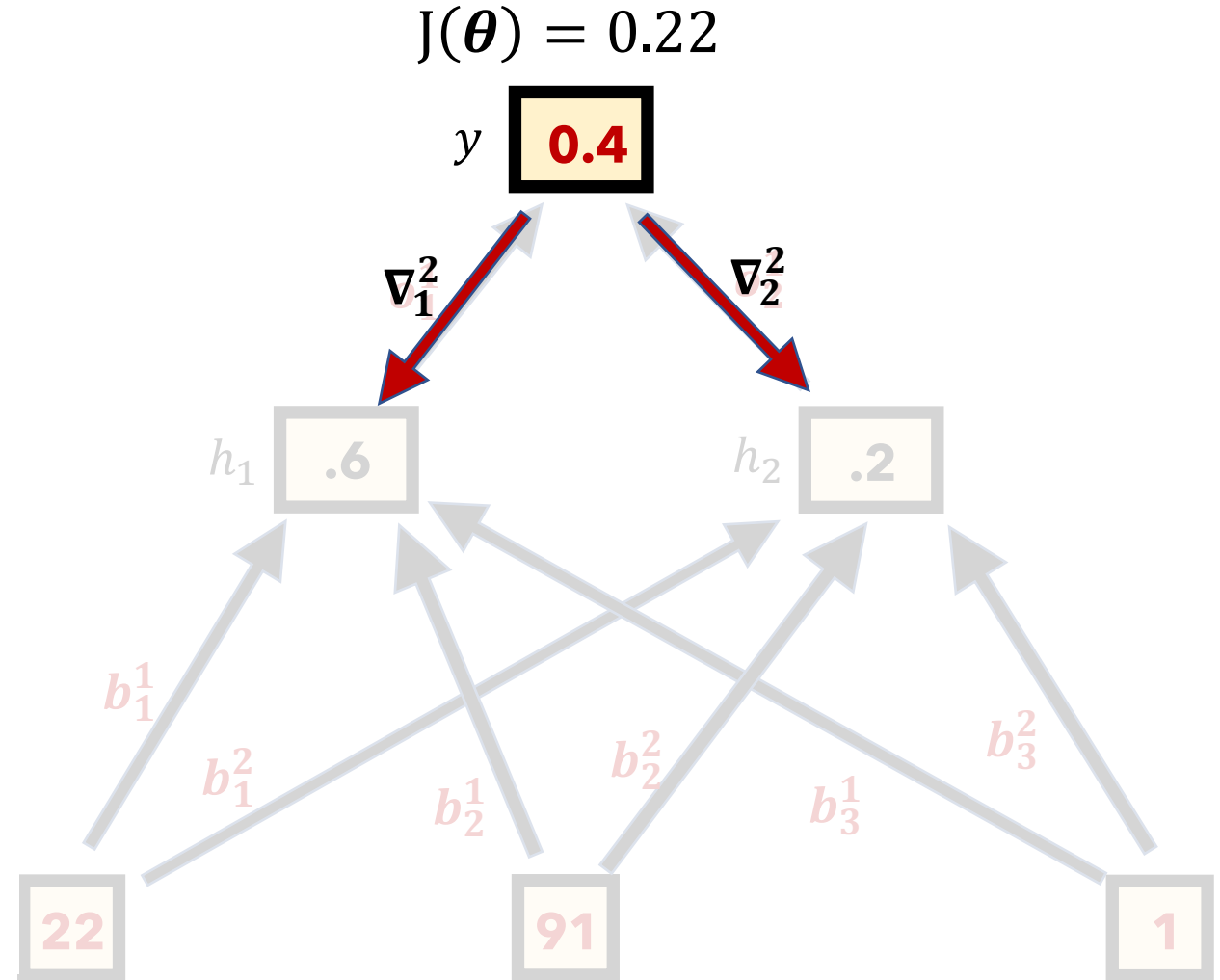
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss
4. Calculate gradients via **backpropagation**



Graphically  
(NN format)

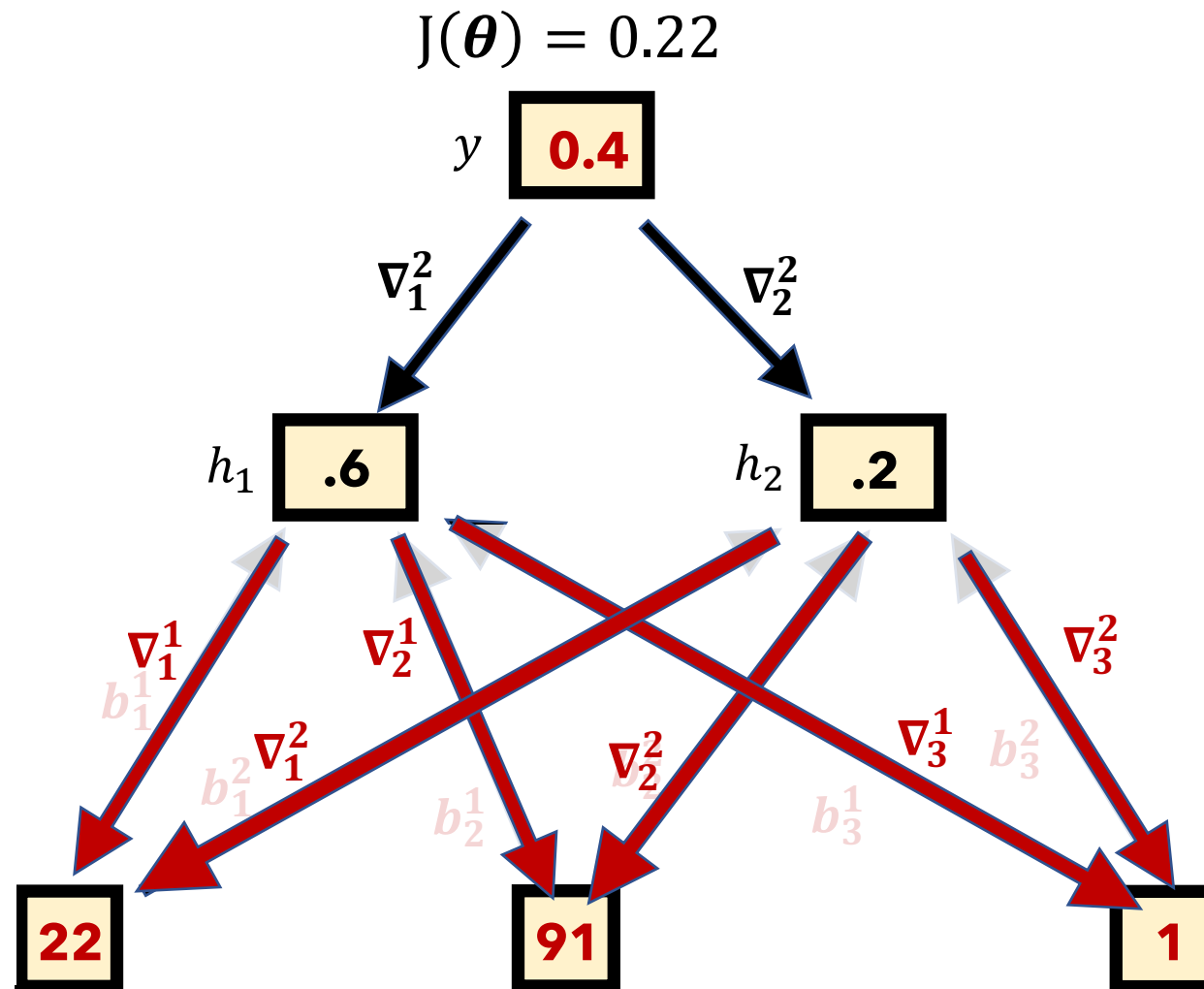
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss
4. Calculate gradients via **backpropagation**



Graphically  
(NN format)

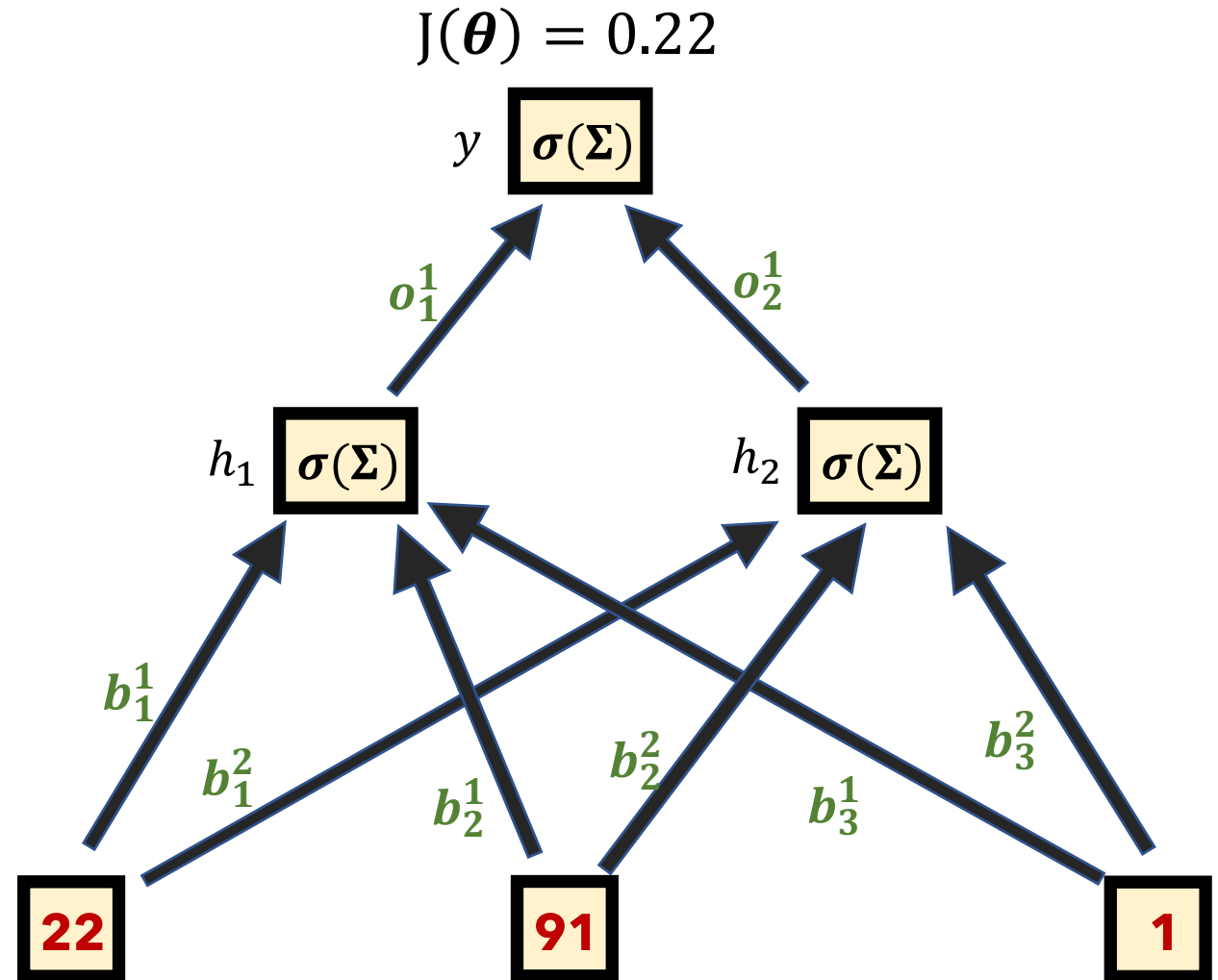
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss
4. Calculate gradients via **backpropagation**
5. Update the weights (aka  $\theta$ ) via **gradient descent**



Graphically  
(NN format)

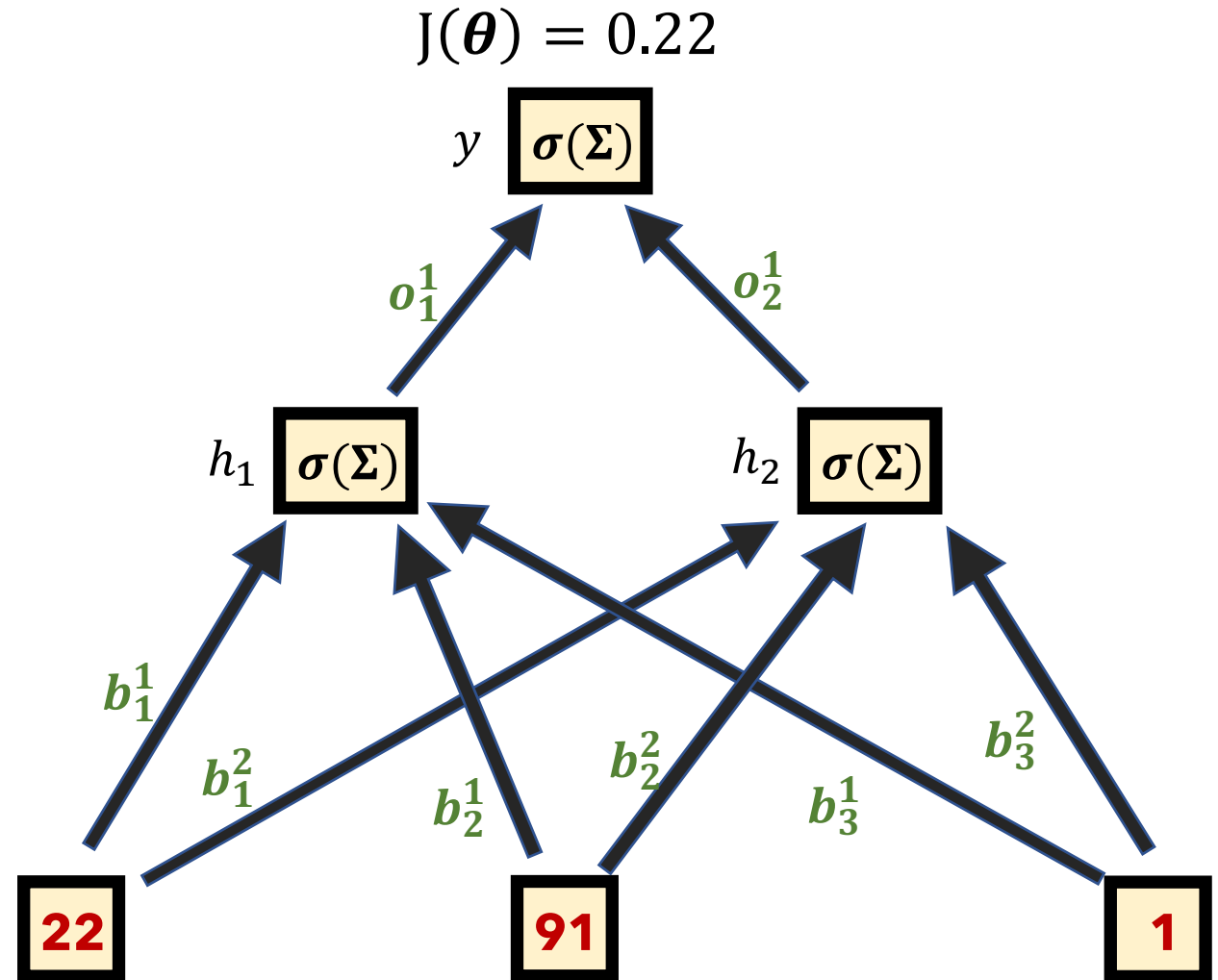
# Feed-Forward Neural Network

## Training:

Initialize  $\theta$  with random values

Repeat until convergence:

1. Provide input  $x_i$  to the network
2. Propagate the values through the network
3. Calculate the cost/loss
4. Calculate gradients via **backpropagation**
5. Update the weights (aka  $\theta$ ) via **gradient descent**



Graphically  
(NN format)

# Feed-Forward Neural Network

## PROS

- Fits many linear or **non-linear** activation functions  $f_i$  to combinations of input  $X$
- Can model highly complex behavior
- When designed well, can provide state-of-the-art results on most tasks
- Incredible resources, libraries, and support

## CONS

- Sensitive to architecture choices and hyperparameters
- Tricky to debug
- Can be computationally expensive
- Poor interpretability

**Supervised vs  
Unsupervised**

**Regression vs  
Classification**

**Parametric vs  
Non-Parametric**

**Generative vs  
Discriminative**

Linear Regression	<b>Supervised</b>	<b>Regression</b>	<b>Parametric</b>	<b>Discriminative</b>
Logistic Regression	<b>Supervised</b>	<b>Classification</b>	<b>Parametric</b>	<b>Discriminative</b>
k-NN	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
Decision Tree	<b>Supervised</b>	<b>either</b>	<b>Non-Parametric</b>	<b>Discriminative</b>
PCA	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>neither</b>
Clustering	<b>Unsupervised</b>	<b>neither</b>	<b>Non-Parametric</b>	<b>Generative</b>
GAMs	<b>Supervised</b>	<b>either</b>	<b>Parametric</b>	<b>Discriminative</b>
Feed-Forward Net	<b>Supervised</b>	<b>either</b>	<b>Parametric</b>	<b>Discriminative</b>

## IMPORTANT

When **training** any supervised model, be careful of **overfitting** your model

A good model should generalize well to unseen (i.e., testing) data

---

Consider adding **regularization** term  $R(\theta)$  to your cost function

**Imposes a penalty based on your parameter values  $\theta$**

**L1** regularization:  $R(\theta) = \sum_{i=1}^n |\theta_i|$  Prefers sparse weights (many 0's)

**L2** regularization:  $R(\theta) = \sum_{i=1}^n \theta_i^2$  Prefers many small-weight values

Additionally, you can add dropout to Neural Networks

# IMPORTANT

When **training** any supervised model, wisely use your training data

A good model should generalize well to unseen (i.e., testing) data

---

- a. Shuffle your training data and optionally bootstrap samples
- b. Perform cross-validation



# MLE vs MAP

So far, whenever we've discussed training a model, we've assumed our data was i.i.d. and we framed the problem as maximizing the similarity of the predictions and the gold truth by adjusting the parameters  $\theta$

e.g.

**Q1**

When training our model, how do we measure its  $m$  predictions  $\hat{y}$  ?

**A1**

Cost function  $J(\theta) = \frac{1}{2} \sum_{i=1}^m (\hat{y} - y)^2$

"Least Squares"

# MLE vs MAP

We were performing the **maximum likelihood estimate**

## Def:

maximum likelihood estimate (MLE) asserts that we should choose  $\theta$  so as to maximize the probability of the observed data (i.e., our  $\hat{y}$  should become as close to  $y$  as possible)

# MLE vs MAP

In other words, we were searching for  $\hat{\theta}_{MLE}$

Say we have the likelihood function  $P(D|\theta)$

$$\hat{\theta}_{MLE} = \operatorname{argmax}_{\theta} P(D|\theta)$$

# MLE vs MAP

**MAP** stands for maximum a posteriori and is interested in calculating  $P(\theta|D)$

If we have knowledge about the prior distribution  $P(\theta)$ , we can calculate:

$$P(\theta|D) = \frac{P(D|\theta)P(\theta)}{P(X)} = \propto P(D|\theta)P(\theta)$$

# MLE vs MAP

**MAP** stands for maximum a posteriori and is interested in calculating  $P(\theta|D)$

If we have knowledge about the prior distribution  $P(\theta)$ , we can calculate:

$$P(\theta|D) = \frac{P(D|\theta)P(\theta)}{P(X)} = \propto P(D|\theta)P(\theta)$$

$$\hat{\theta}_{MAP} = \operatorname{argmax}_{\theta} P(D|\theta)P(\theta)$$

# MLE vs MAP

**MAP** stands for maximum a posteriori and is interested in calculating  $P(\theta|D)$

**NOTE:** If the prior  $P(\theta)$  is uniform (i.e., not Gaussian or any other distribution), then  $\hat{\theta}_{MAP} = \hat{\theta}_{MLE}$

**Thus, MLE is a special case of MAP!**

$$\hat{\theta}_{MAP} = \operatorname{argmax}_{\theta} P(D|\theta)P(\theta)$$

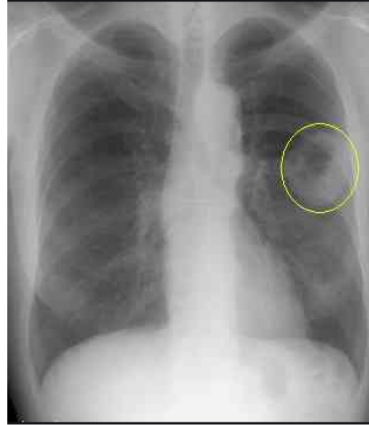
## CS109B: What's next

We have learned a lot so far, with the assumption that our data is “flat” (each feature/column is independent of the others)

But what if our data is different?

## CS109B: What's next

**Scenario:** imagine having picture data, whereby each pixel is a feature. Obviously, pixels near one another in 2D space (both vertically and horizontally) are highly correlated.



Detecting lung cancer

A flattened vector wouldn't work well.



Solution: **CNNs**

## CS109B: What's next

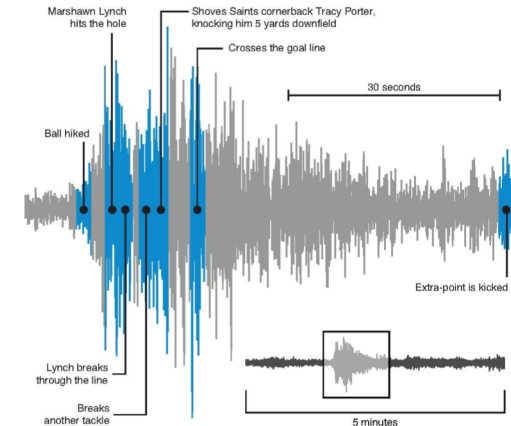
We have learned a lot so far, with the assumption that our data is **i.i.d.** (each row is independent from one another)

But what if our data is different?

# CS109B: What's next

**Scenario:** imagine having data that is sequential in nature (e.g., natural text, speech, video frames, time series data)

"Today, I went to the \_\_\_\_\_"



UNDERSTANDING  
LANGUAGE

PREDICTING  
EARTHQUAKES

Solution: **RNNs / LSTMs**

## CS109B: What's next

We have learned that PCA can transform our data while maintaining variance. However, it's unsupervised. Can we **learn** a better representation of our data?

Perhaps, we can learn how the data was "generated"?

Solution: **Autoencoders**

Can we generate realistic, synthetic data, and do so in such a realistic way that it **increases the performance** of our classifiers?

Solution: **GANs** (not **GAMs**)

DeepFake is an example that uses GANs

## CS109B: What's next

Instead of making just 1 prediction per preset input, sometimes we may want to get real-time feedback as to what our prediction's effects were. For example, navigating through an environment or game (Mars or Chess Board)

We need to represent the updated environment, possible actions to take, risks of those actions, etc.

Solution: **Reinforcement Learning**

Questions?