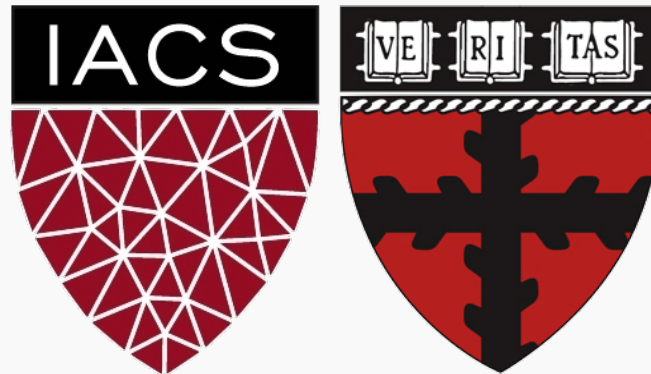


Part A: Universal Approximators; Nodes and Layers

CS109A Introduction to Data Science
Pavlos Protopapas, Kevin Rader and Chris Tanner



Design Choices

Activation function

Loss function

Output units

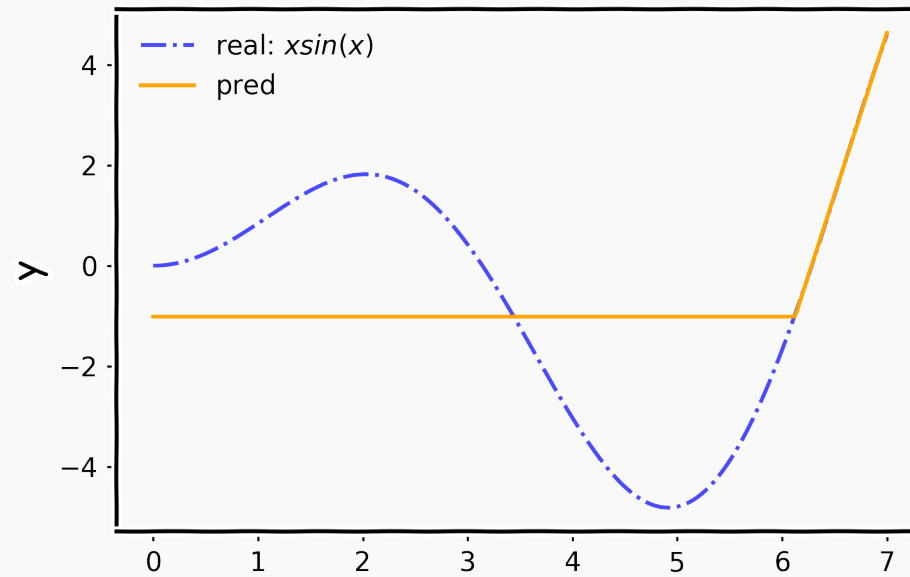
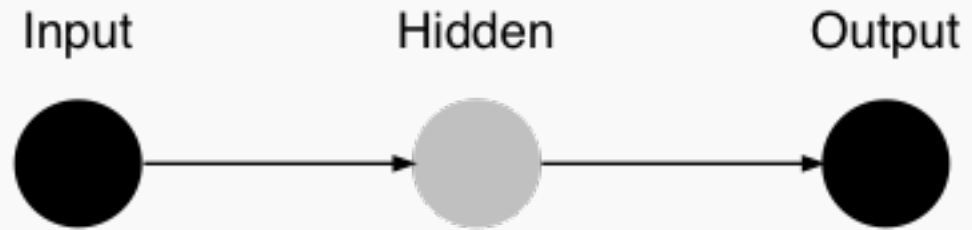
Architecture

Optimizer

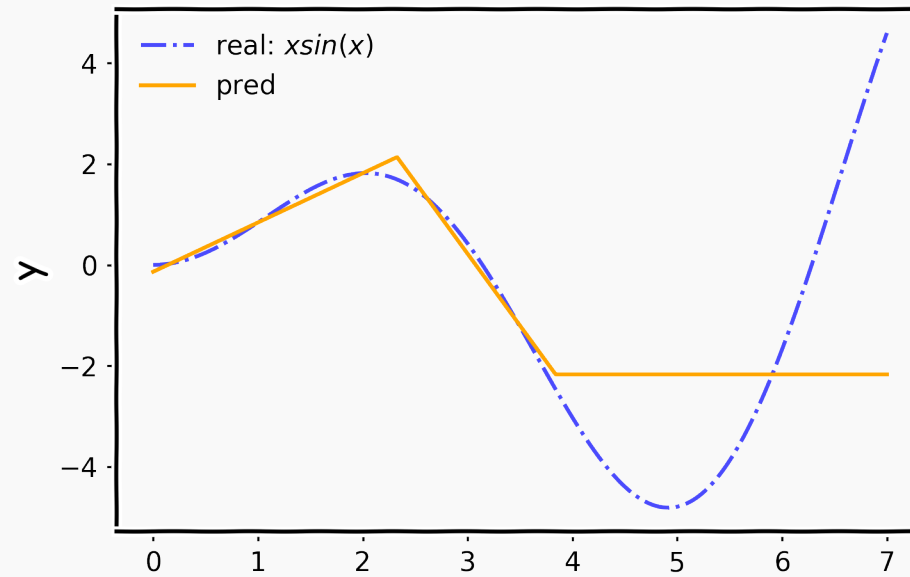
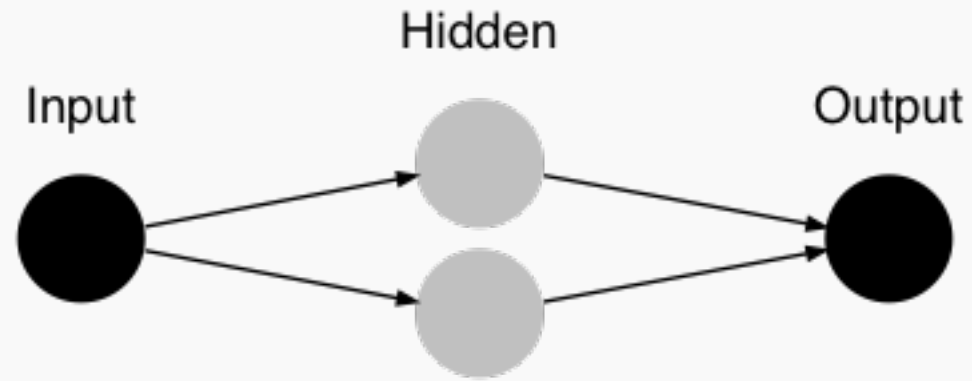


How to bully machine learning training

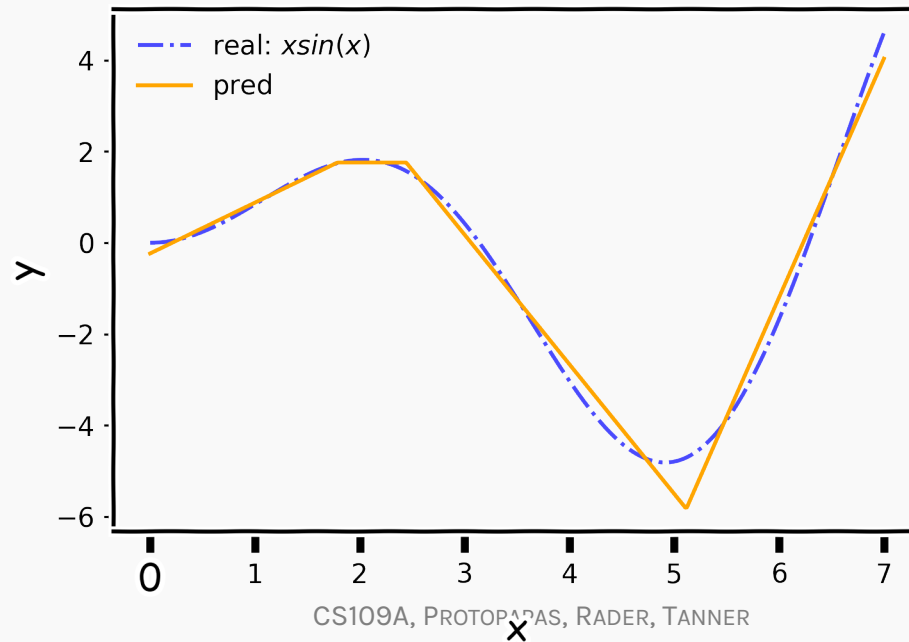
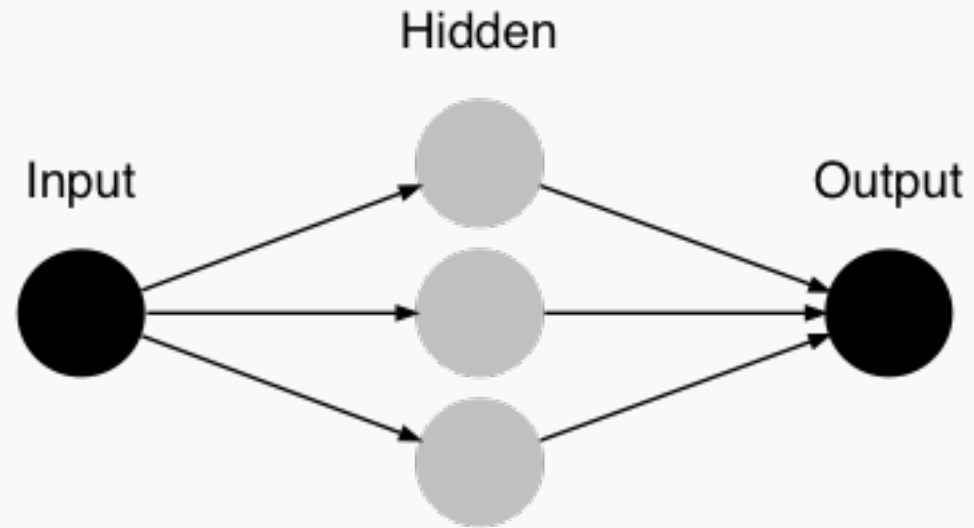
Number of nodes



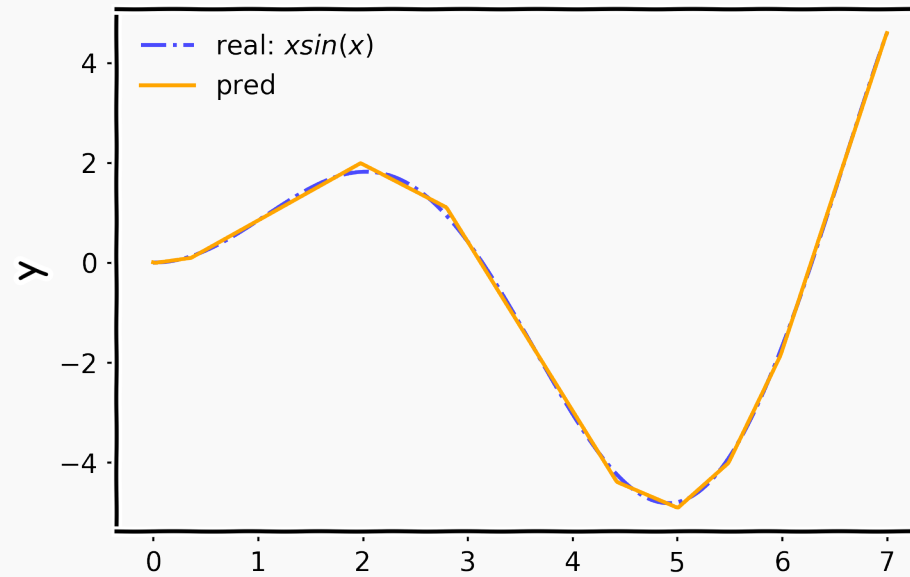
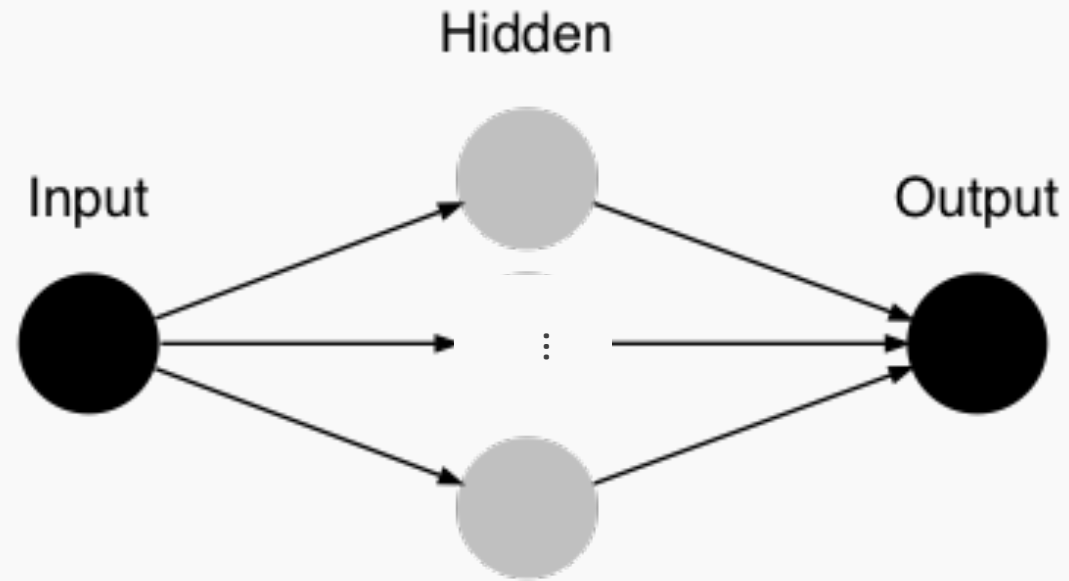
Number of nodes



Number of nodes

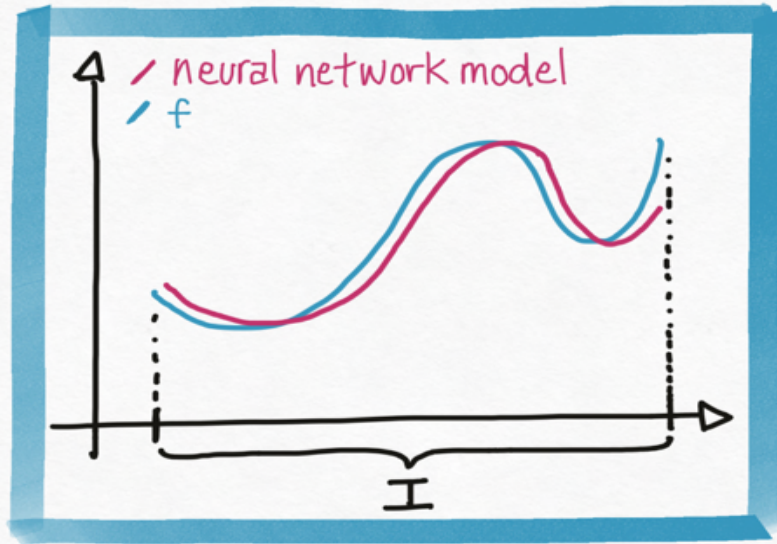


Number of nodes





Neural Networks as Universal Approximators



We have seen that neural networks can represent complex functions, but are there limitations on what a neural network can express?

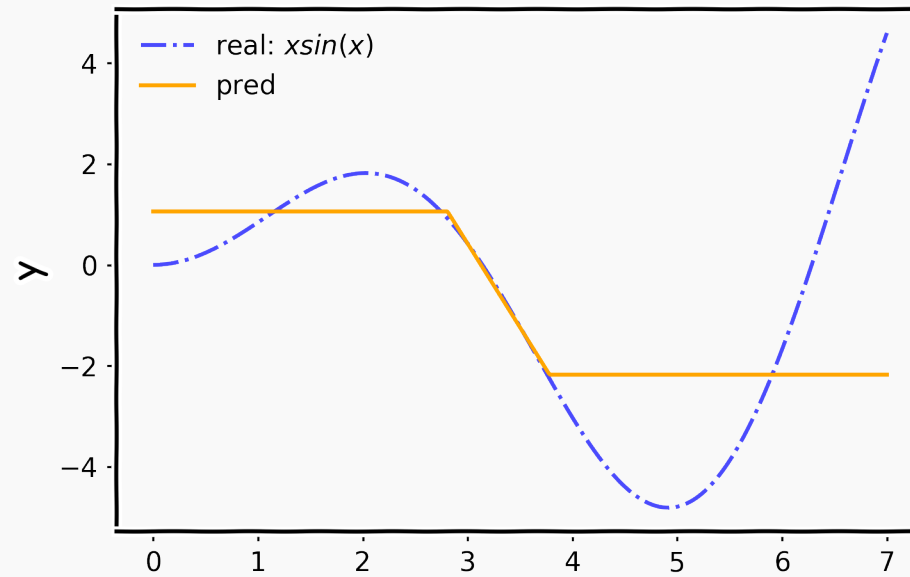
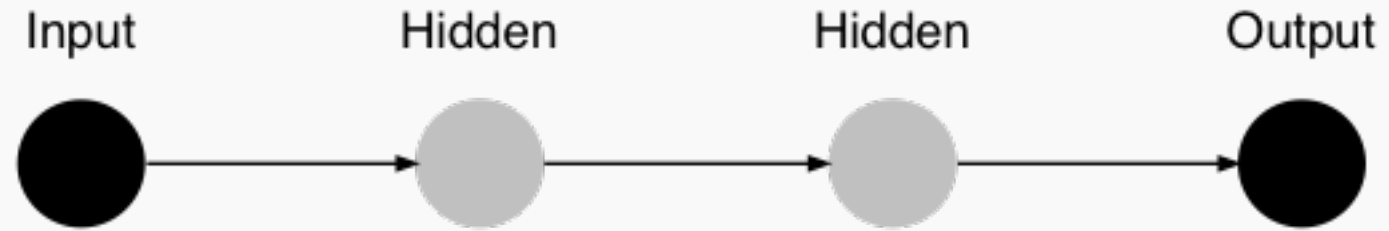
Theorem:

For any continuous function f defined on a bounded domain, we can find a neural network that approximates f with an arbitrary degree of accuracy.

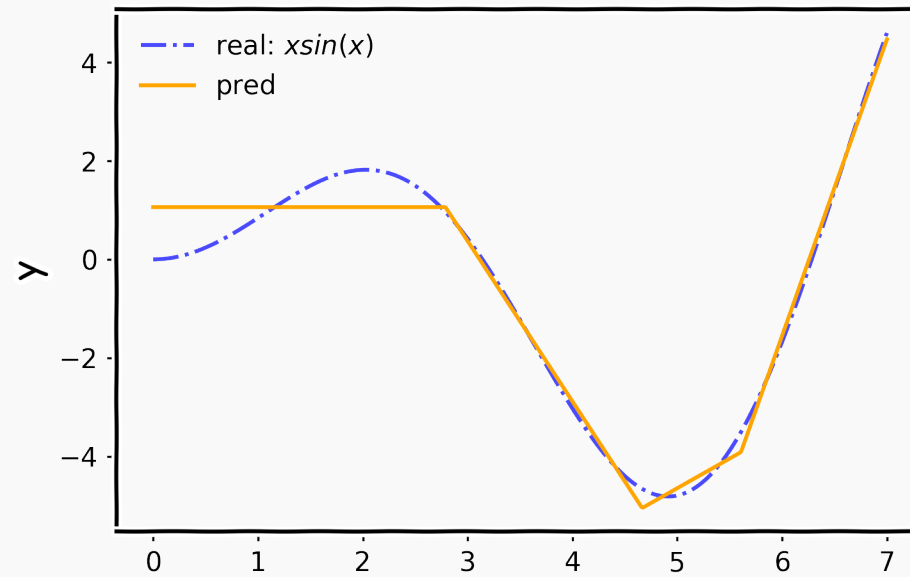
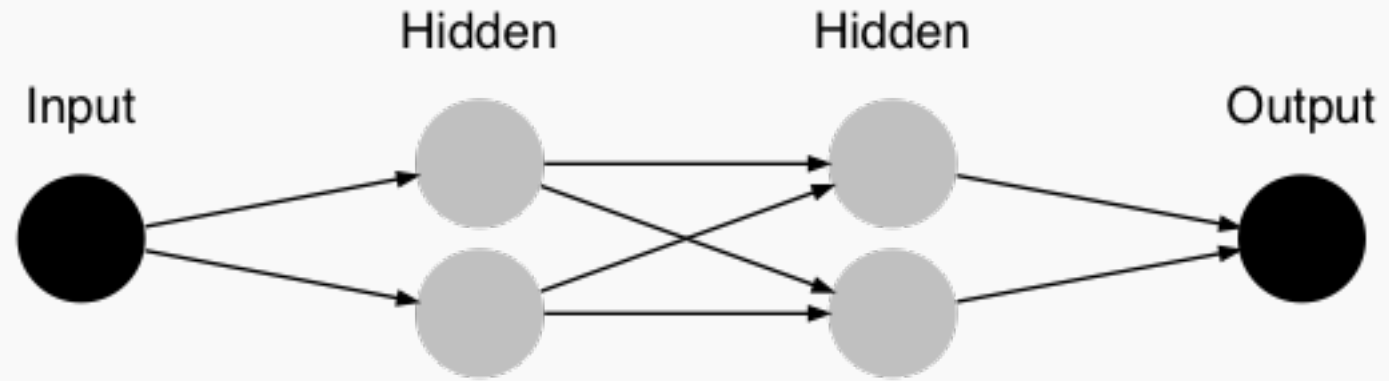
One hidden layer is enough to represent an approximation of any function to an arbitrary degree of accuracy.

So why deeper?

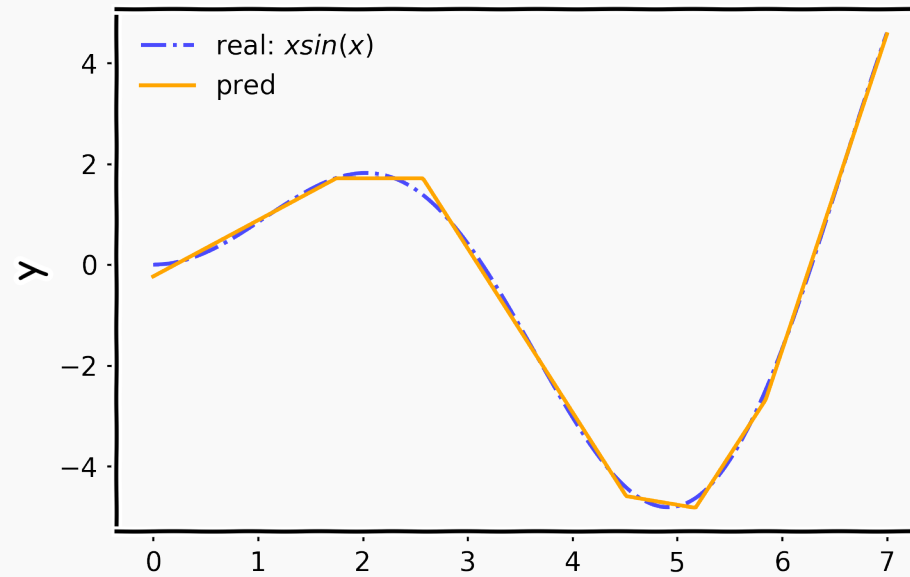
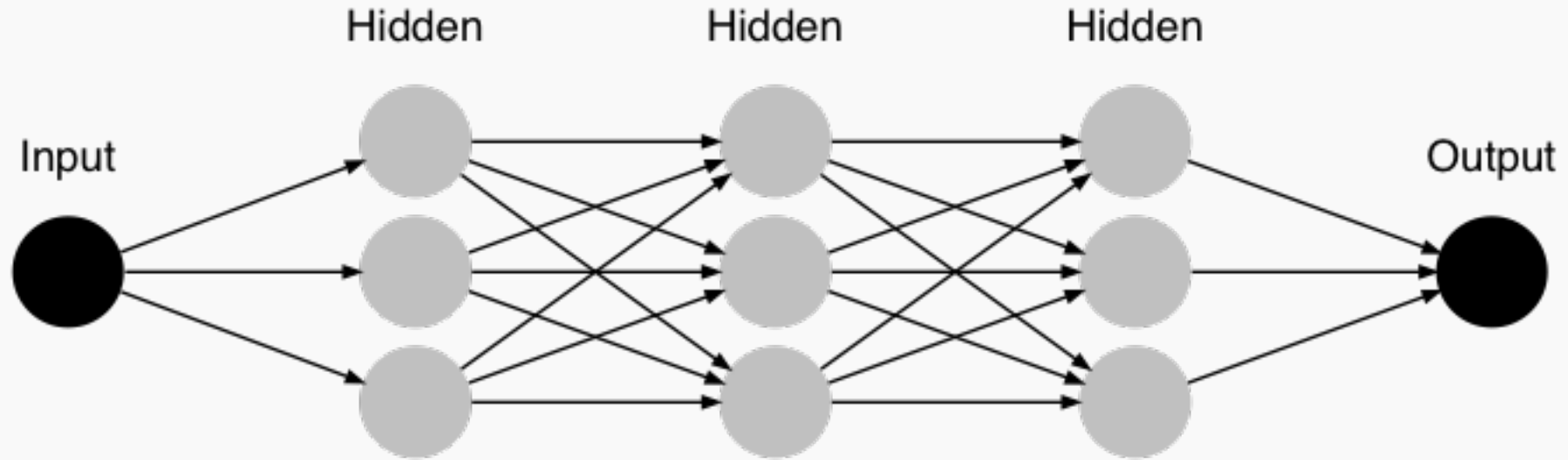
Layers



Layers

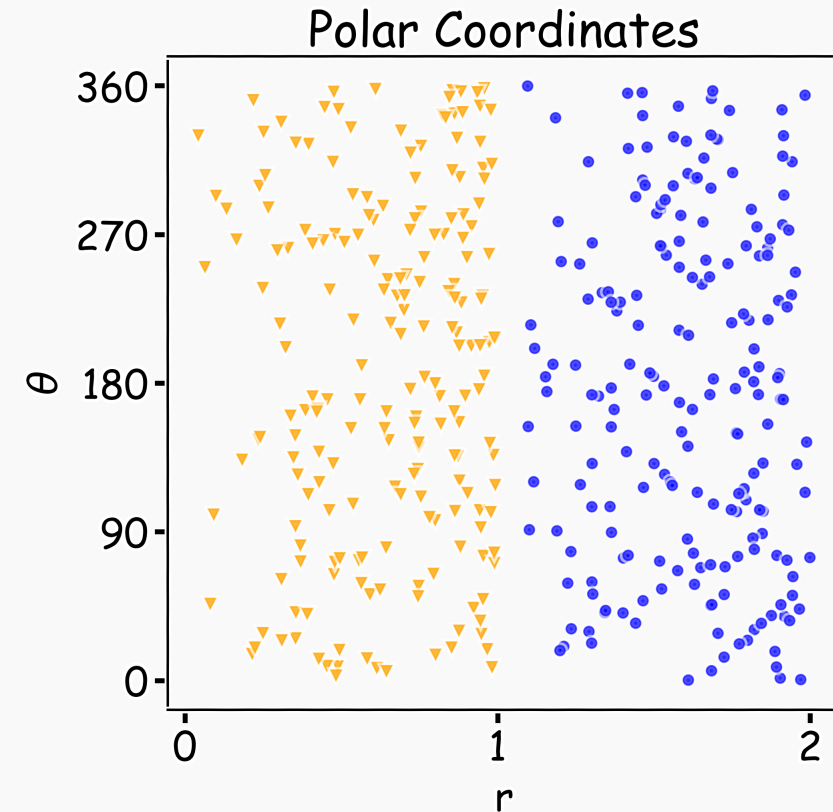
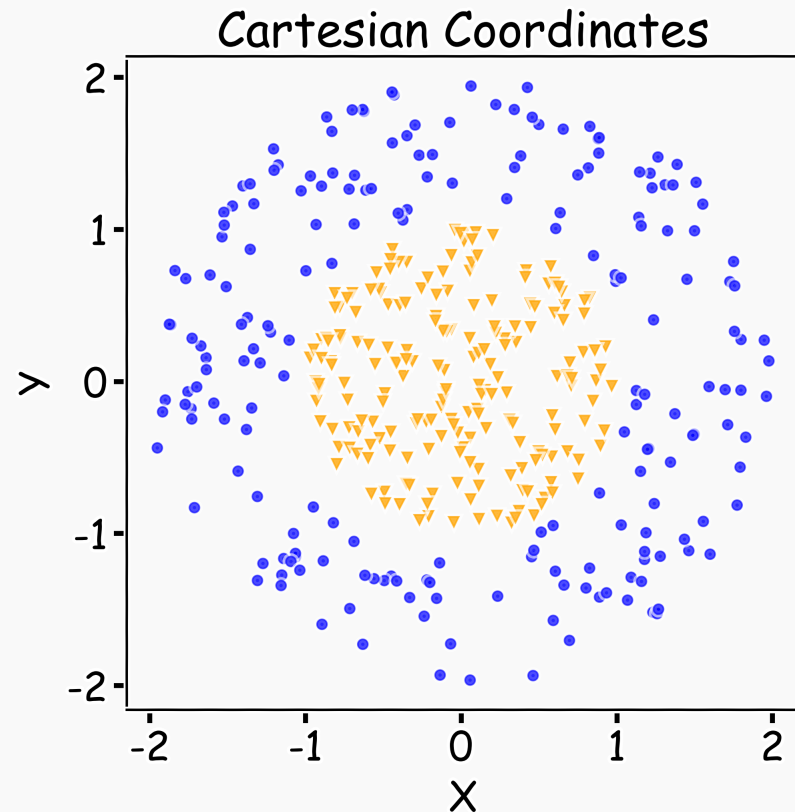


Layers

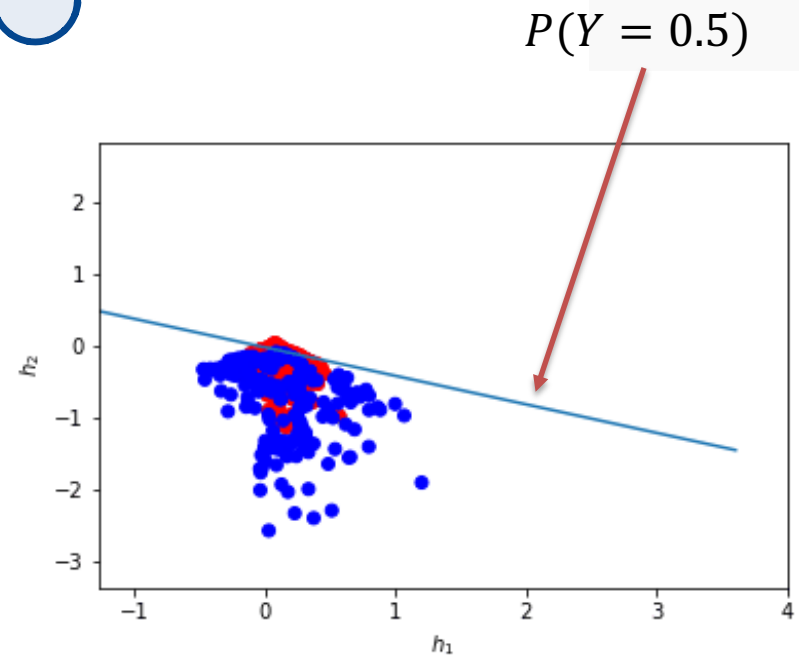
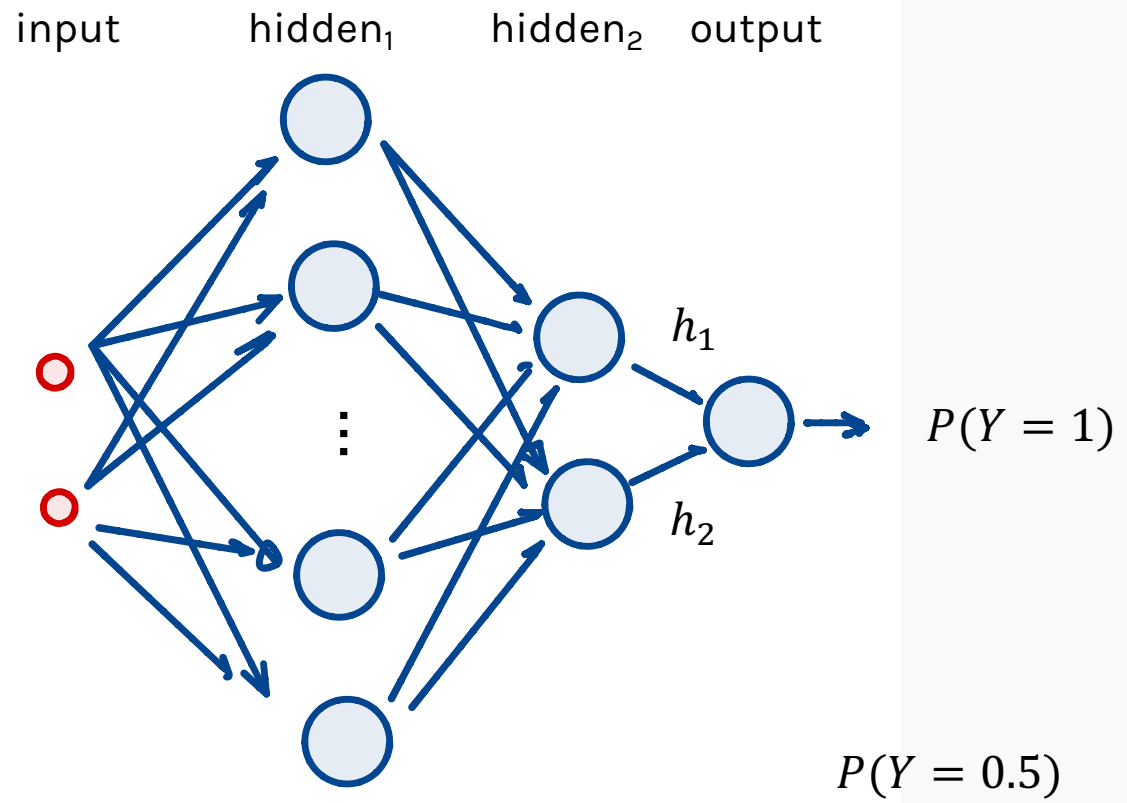
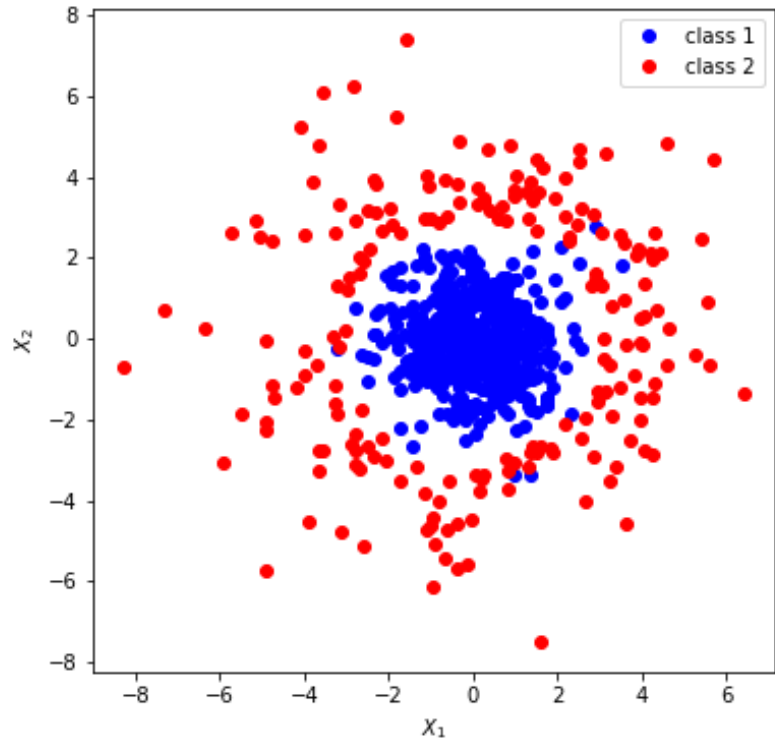


Why layers?

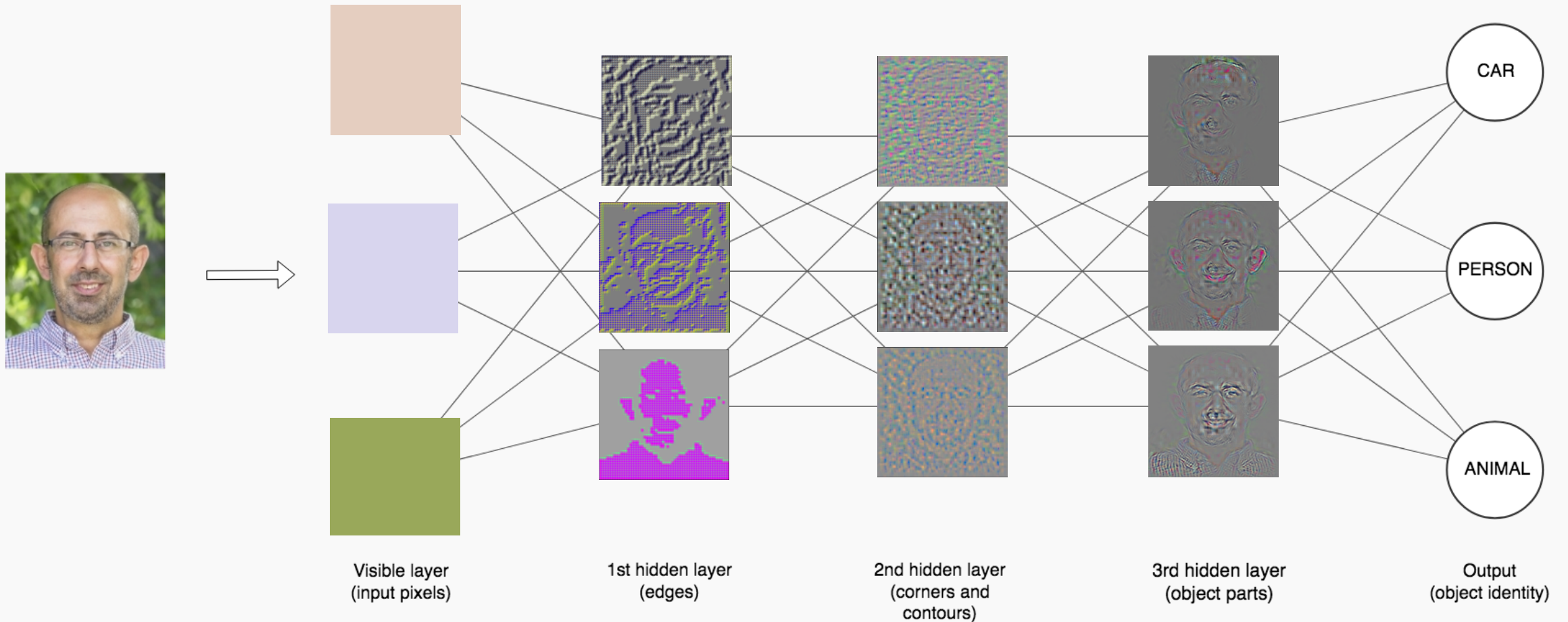
Representation matters!



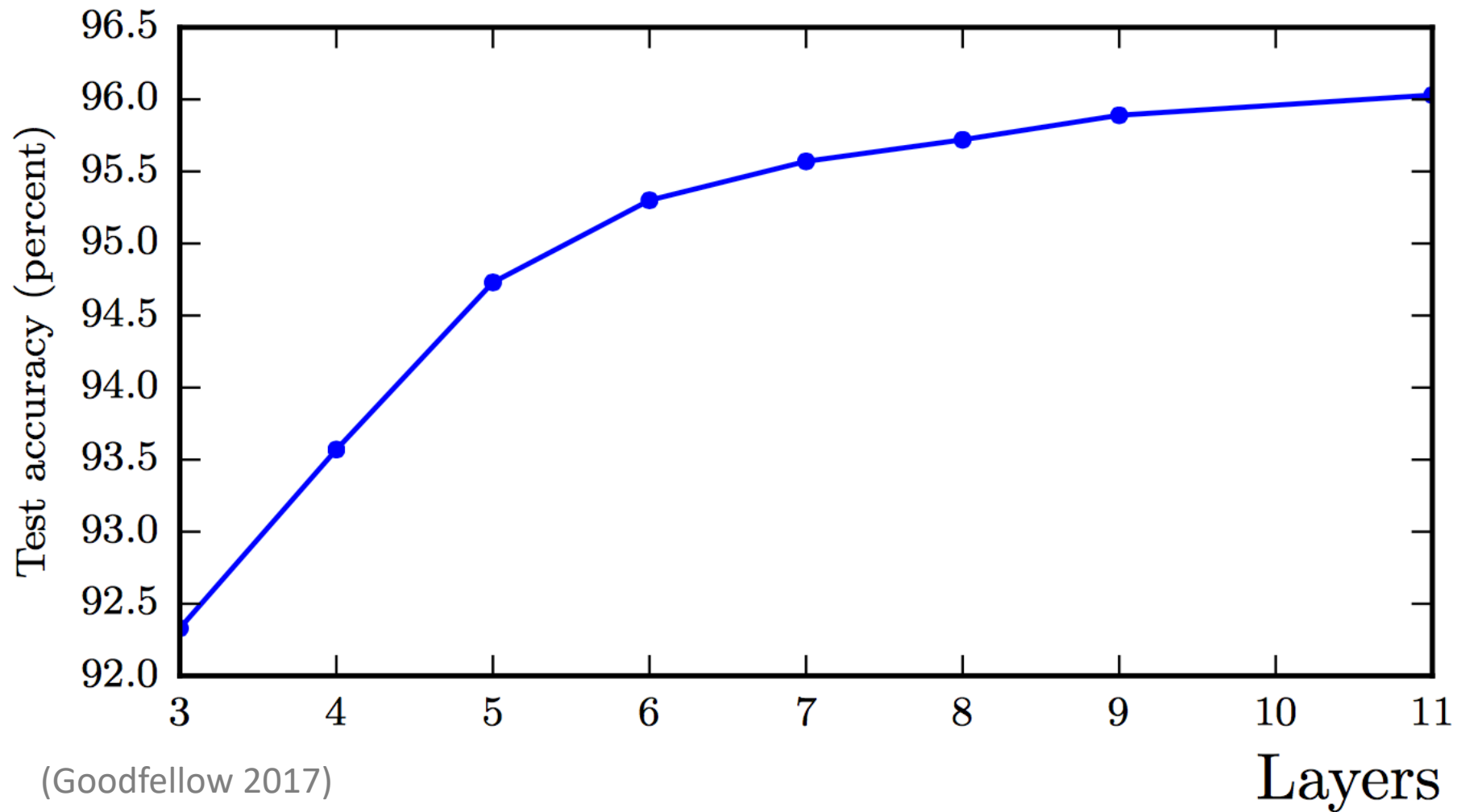
Neural networks can **learn useful representations** for the problem. This is another reason why they can be so powerful!



Depth = Repeated Compositions

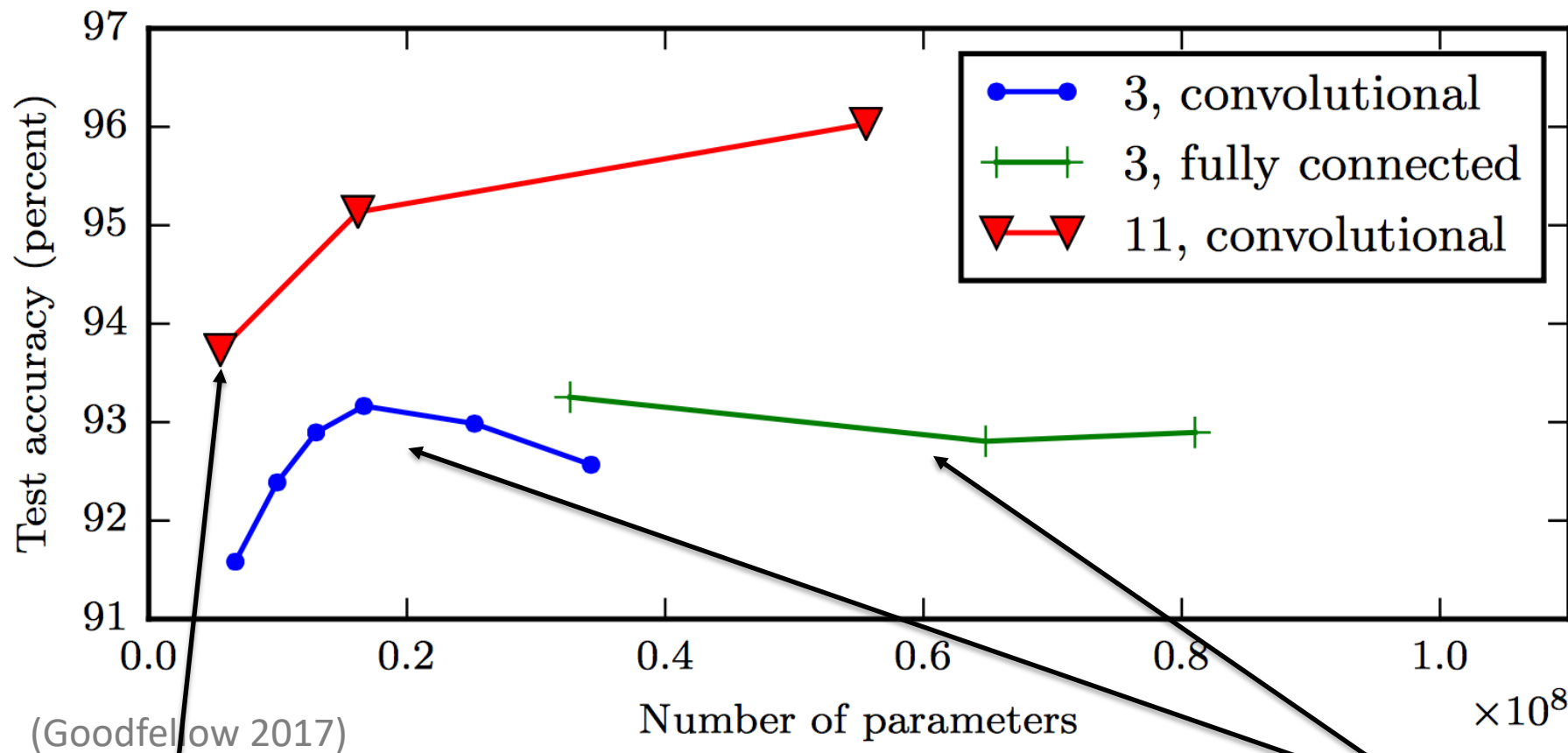


Better Generalization with Depth



Shallow Nets Overfit More

Depth helps, and it's not just because of more parameters

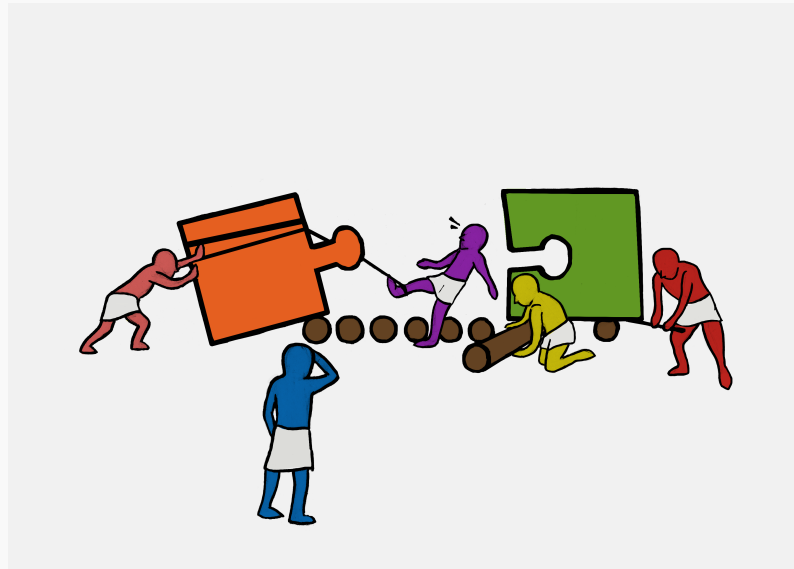


Don't worry about this word "convolutional". It's just a special type of neural network, often used for images.

(Goodfellow 2017)

The **11-layer net** generalizes better on the test set when controlling for number of parameters.

The 3-layer nets perform worse on the test set, even with similar number of total parameters.



Classifier using Keras on Iris data