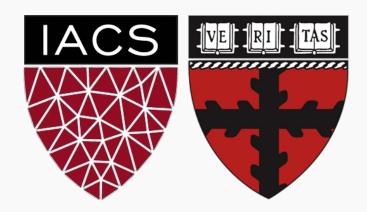
Lecture 10: Recurrent Neural Networks

CS109B Data Science 2 Pavlos Protopapas and Mark Glickman



Sequence Modeling: Handwritten Text Translation

Winter is here. Go to the store and buy some snow shovels.

Winter is here. Go to the store and buy some snow shovels.

- Input : Image
- Output: Text

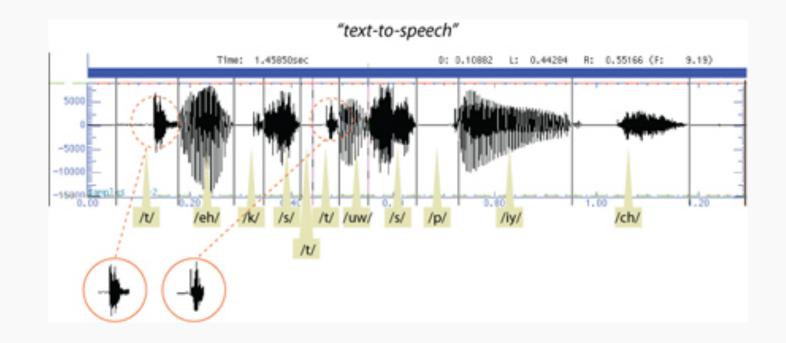
https://towardsdatascience.com/build-a-handwritten-text-recognition-system-using-tensorflow-



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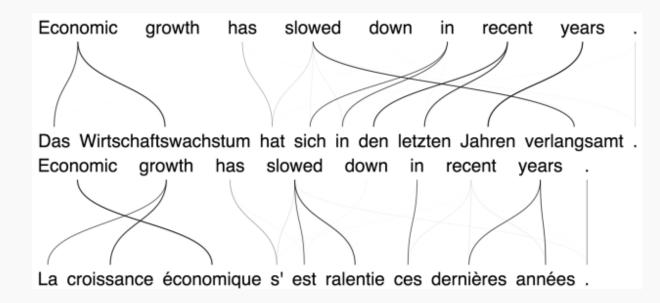
Sequence Modeling: Text-to-Speech



- Input : Audio
- Output: Text



Sequence Modeling: Machine Translation



- Input : Text
- Output: Translated Text



https://github.com/robbiebarrat/rapping-neural-network



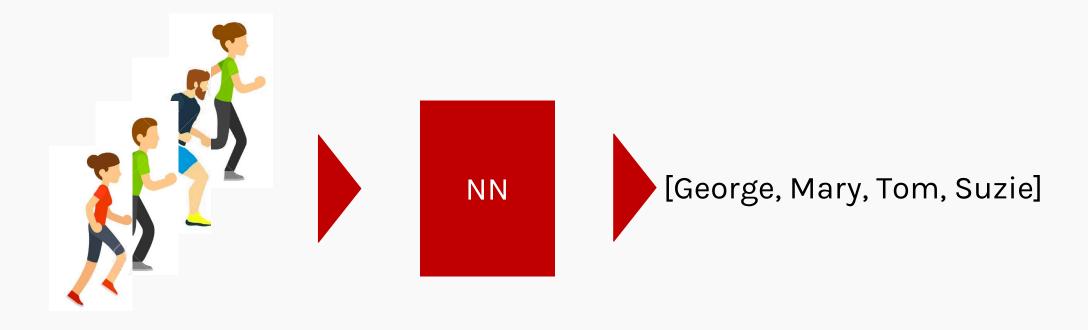
Why RNNs Main Concept of RNNs More Details of RNNs RNN training Gated RNN



Why RNNs Main Concept of RNNs More Details of RNNs RNN training Gated RNN



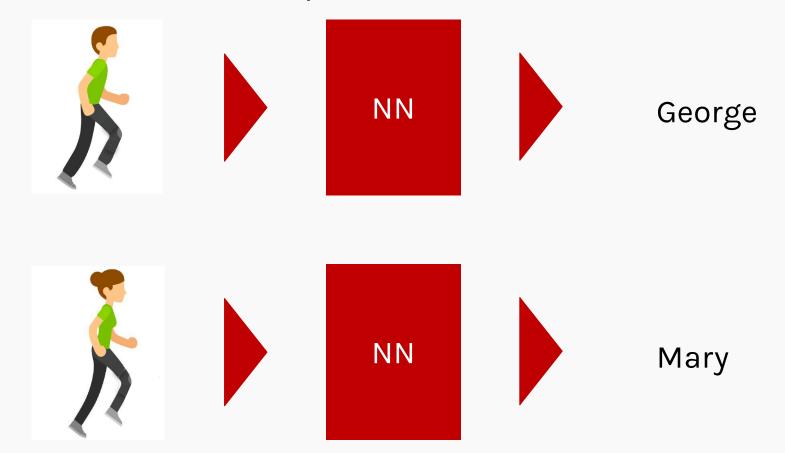
Training: Present to the NN examples and learn from them.





What can my NN do?

Prediction: Given an example



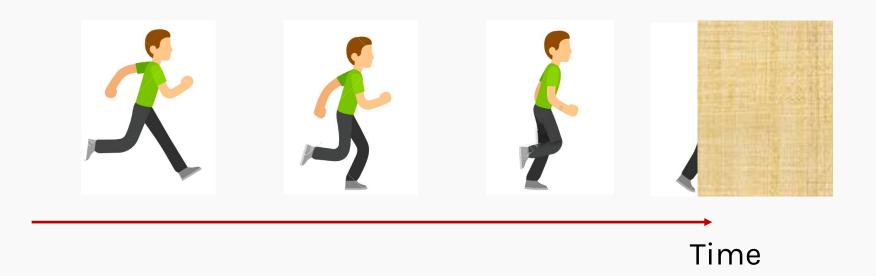


What my NN can NOT do?



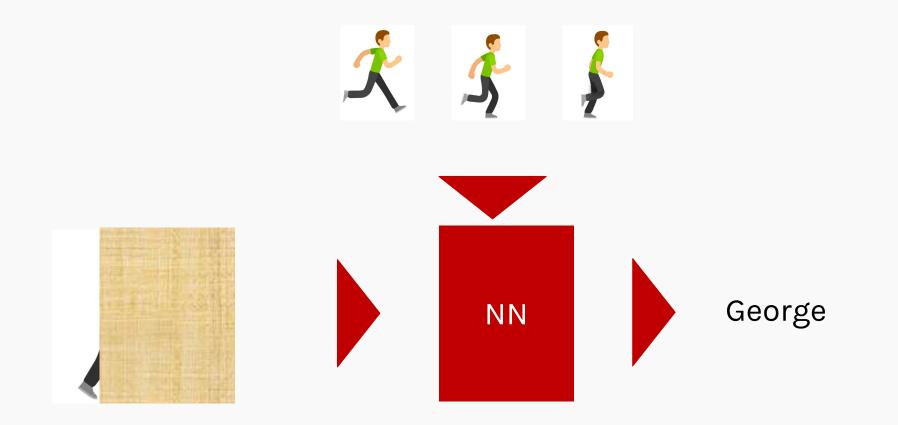


Learn from previous examples

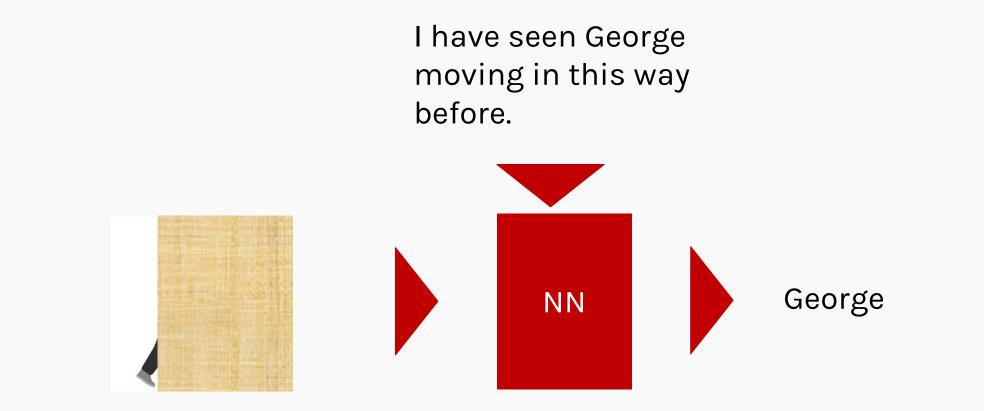




Recurrent Neural Network (RNN)







RNNs recognize the data's sequential characteristics and use patterns to predict the next likely scenario.

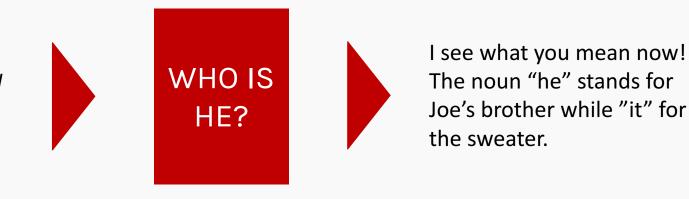




Our model requires context - or contextual information - to understand the subject (he) and the direct object (it) in the sentence.



Hellen: Nice sweater Joe.
Joe: Thanks, Hellen. It used to belong to my brother and he told me I could have it.

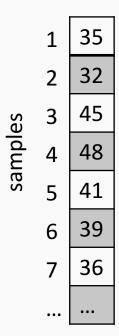


After providing sequential information, the model understood the subject (Joe's brother) and the direct object (sweater) in the sentence .



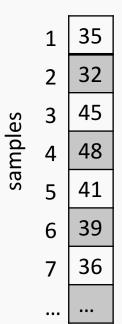
- We want a machine learning model to understand sequences, not isolated samples.
- Can MLP do this?
- Assume we have a sequence of temperature measurements and we want to take 3 sequential measurements and predict the next one

features

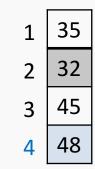




- We want a machine learning model to understand sequences, not isolated samples.
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- Assume we have a sequence of temperature measurements and we want to take 3 sequential measurements and predict the next one

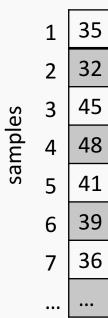


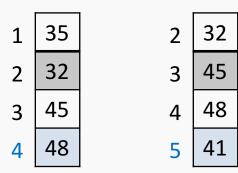






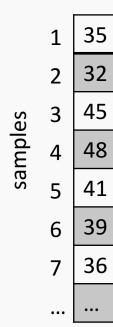
- We want a machine learning model to understand sequences, not isolated samples.
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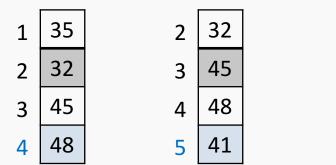




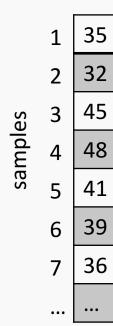


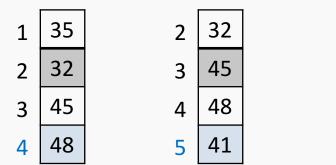
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- Can MLP do this?
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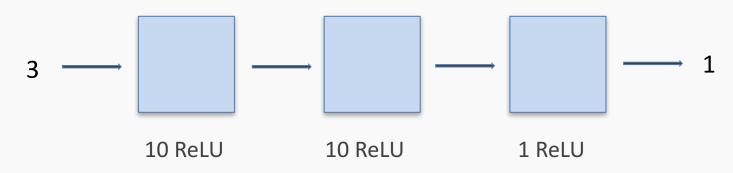
- We want a machine learning model to understand sequences, not isolated samples.
- Can MLP do this?
- Assume we have a sequence of temperature measurements and we want to take 3 sequential measurements and predict the next one



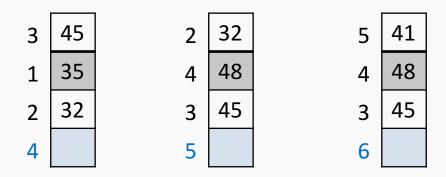


This is called **overlapping windowed** dataset, since we're windowing observations to create new.

We can easily do using a MLS:



But re-arranging the order of the inputs like:





- 1. MLPs/CNNs require fixed input and output size
- 2. MLPs/CNNs can't classify inputs in multiple places



What follows after: 'I got in the car and'?

drove away

What follows after: 'In car the and I'?

Not obvious it should be 'drove away'

The order of words matters. This is true for most sequential data.

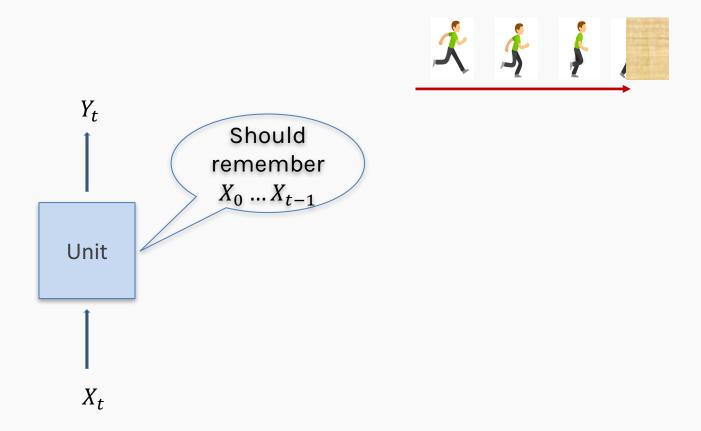
A fully connected network will not distinguish the order and therefore missing some information.



Why RNNs **Main Concept of RNNs** More Details of RNNs RNN training Gated RNN

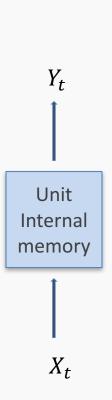


Somehow the computational unit should remember what it has seen before.





Somehow the computational unit should remember what it has seen before.





Somehow the computational unit should remember what it has seen before. We'll call the information the unit's **state**.







In neural networks, once training is over, the weights do not change. This means that the network is done learning and done changing.

Then, we feed in values, and it simply applies the operations that make up the network, using the values it has learned.

But the RNN units are able to remember new information after training has completed.

That is, they're able to keep changing after training is over.



Question: How can we do this? How can build a unit that remembers the past?

The memory or **state** can be written to a file but in RNNs, we keep it inside the recurrent unit.

In an array or in a vector!

Work with an example:

Anna Sofia said her shoes are too ugly. Her here means Anna Sofia.

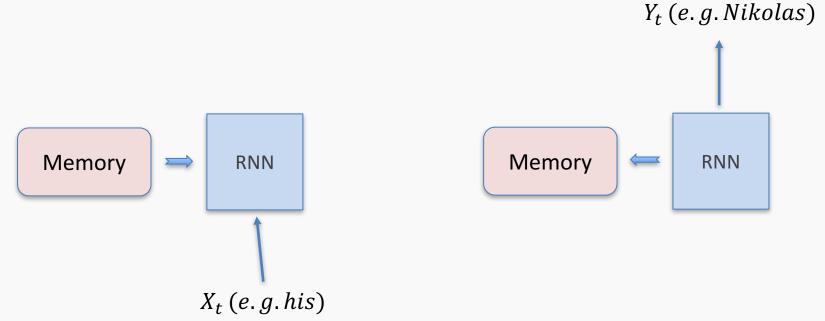
Nikolas put his keys on the table. His here means Nikolas



Question: How can we do this? How can build a unit that remembers the past?

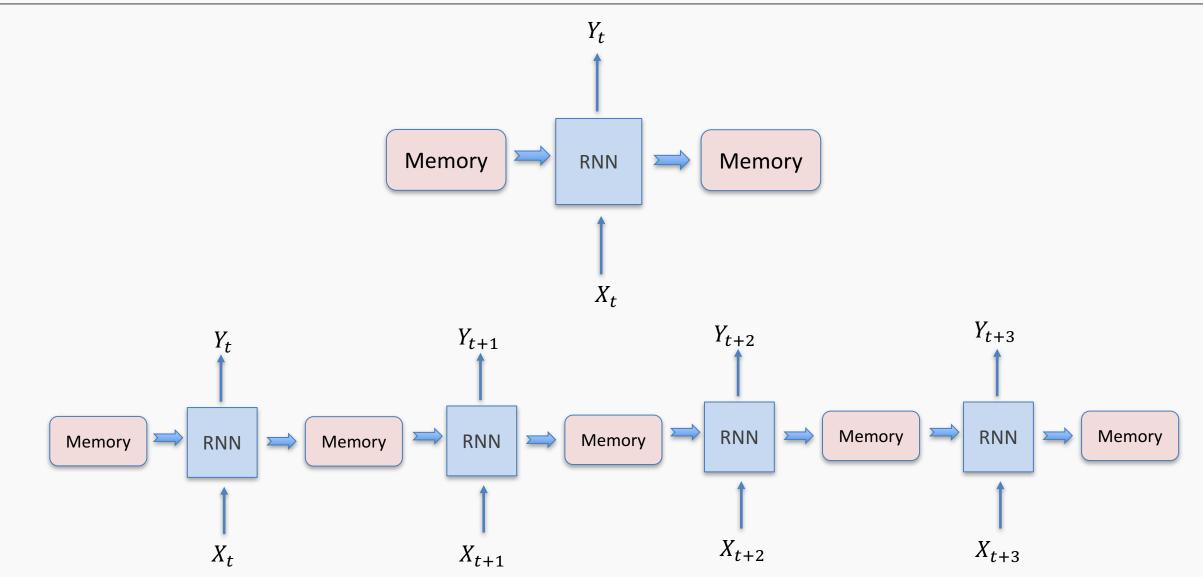
The memory or **state** can be written to a file but in RNNs, we keep it inside the recurrent unit.

In an array or in a vector!





Building an RNN





Why RNNs Main Concept of RNNs **More Details of RNNs** RNN training

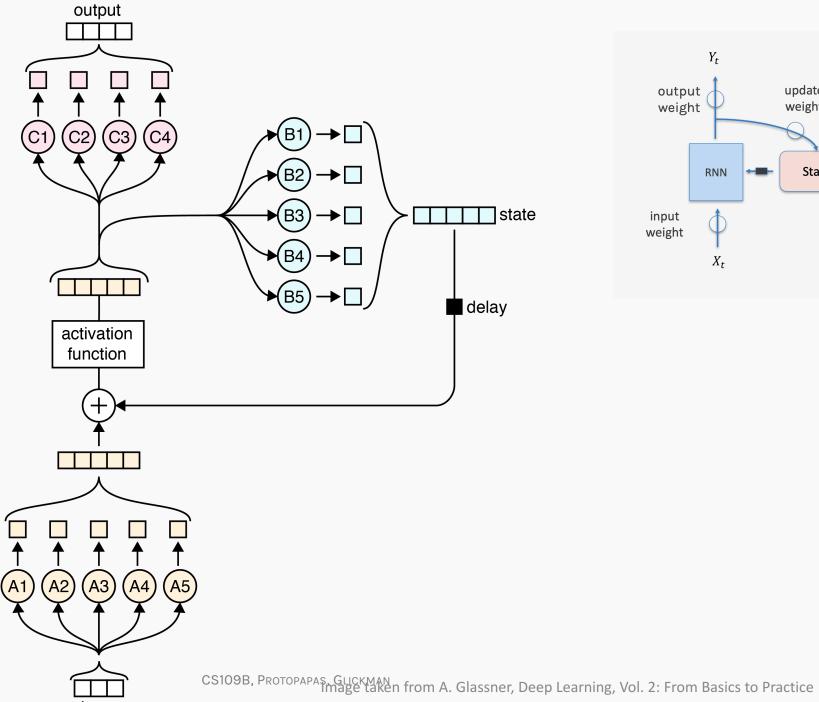
Gated RNN



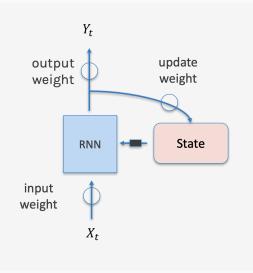
Structure of an RNN cell

Memory X_{t+3} Y_t Y_t update output weight weight State RNN State RNN ← input weight X_t X_t





input





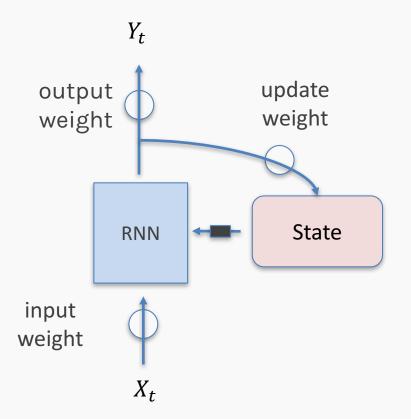
Why RNNs Main Concept of RNNs More Details of RNNs **RNN training** Gated RNN



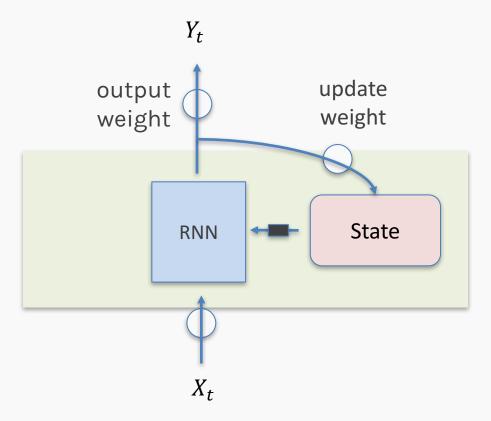
Backprop Through Time

- For each input, unfold network for the sequence length T
- Back-propagation: apply forward and backward pass on unfolded network
- Memory cost: O(T)

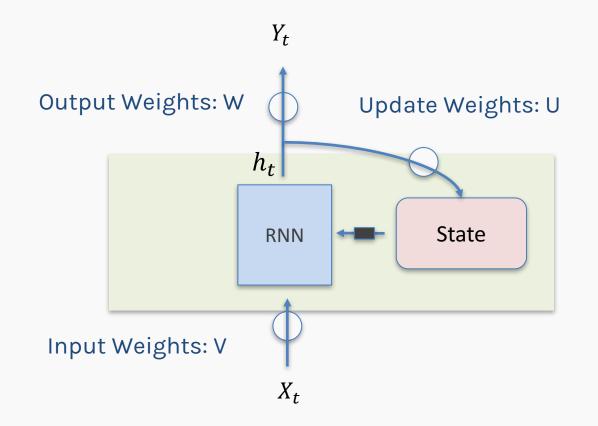




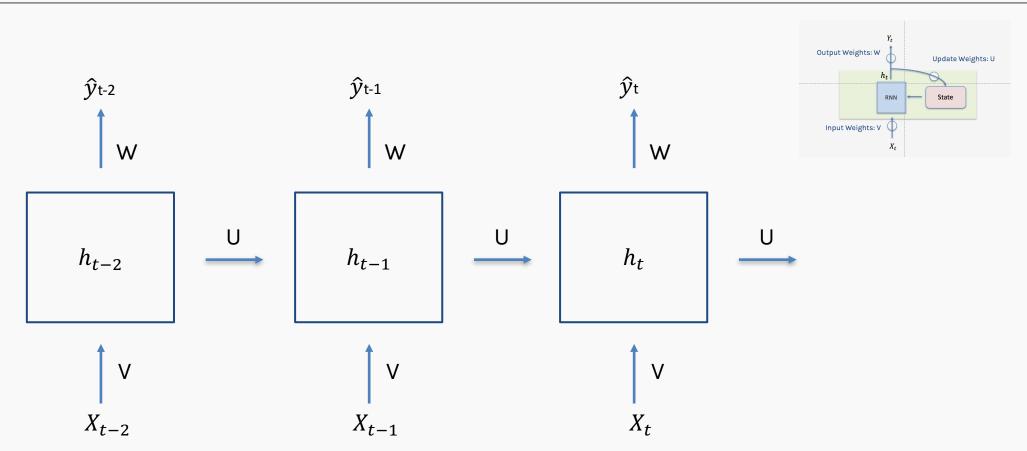








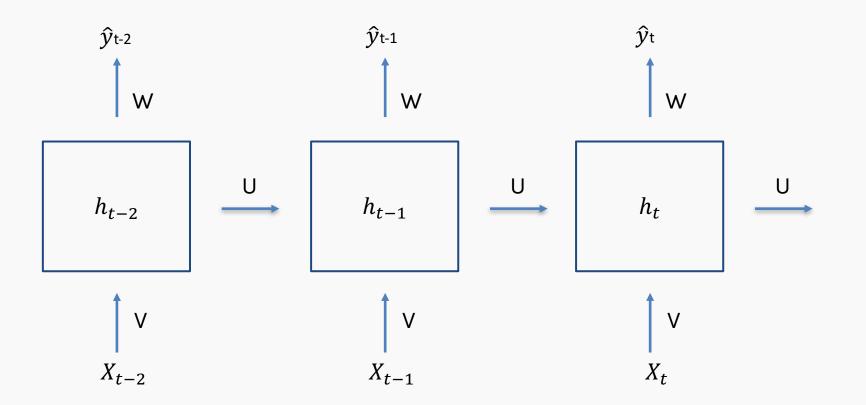




You have two activation functions g_h which serves as the activation for the hidden state and g_y which is the activation of the output. In the example shown before g_y was the identity.



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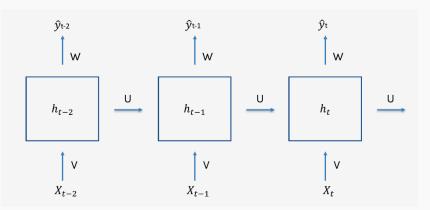


 $\hat{y}_t = g_y(Wh_t + b)$

$$L = \sum_{t} L_t \qquad \qquad L_t = L_t(\hat{y}_t)$$

$$\frac{dL}{dW} = \sum_{t} \frac{dL_t}{dW} = \sum_{t} \frac{\partial L_t}{\partial \hat{y}_t} \frac{\partial \hat{y}_t}{\partial W}$$

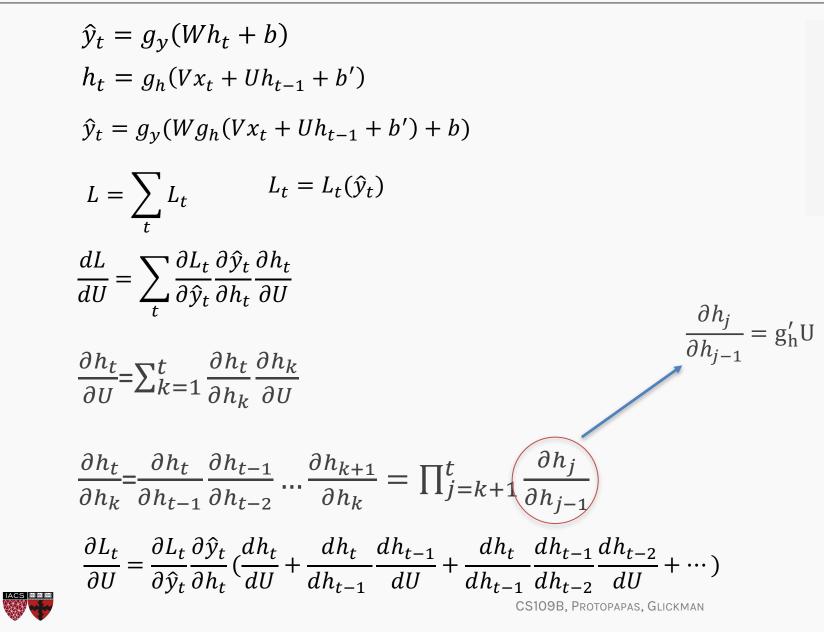
 $\frac{\partial \hat{y}_t}{\partial W} = g_y' h_t$

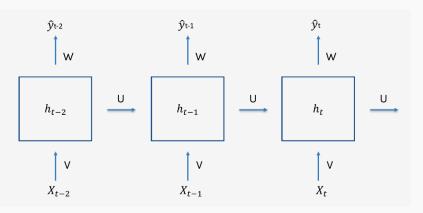








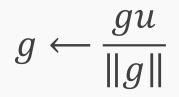




Gradient Clipping

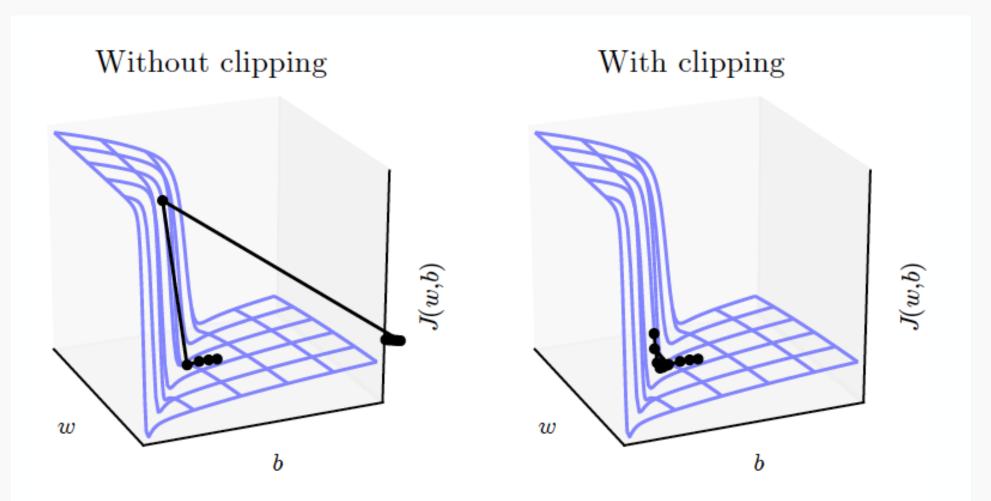
Prevents exploding gradients Clip the norm of gradient before update. For some derivative *g*, and some threshold *u*

 $\text{if } \|g\| > u$





Gradient Clipping





Why RNNs Main Concept of RNNs More Details of RNNs RNN training Gated RNN



Unfolded networks can be very deep

Long-term interactions are given exponentially smaller weights than small-term interactions

Gradients tend to either vanish or explode

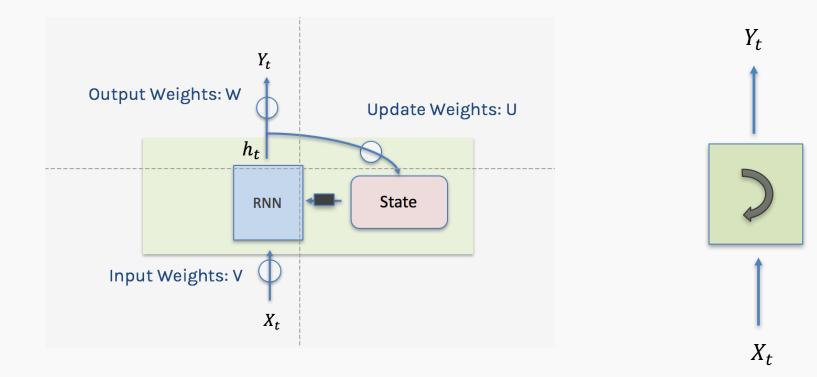


Handles long-term dependencies

- Leaky units where weight on self-loop α is context-dependent
- Allow network to decide whether to accumulate or forget past info

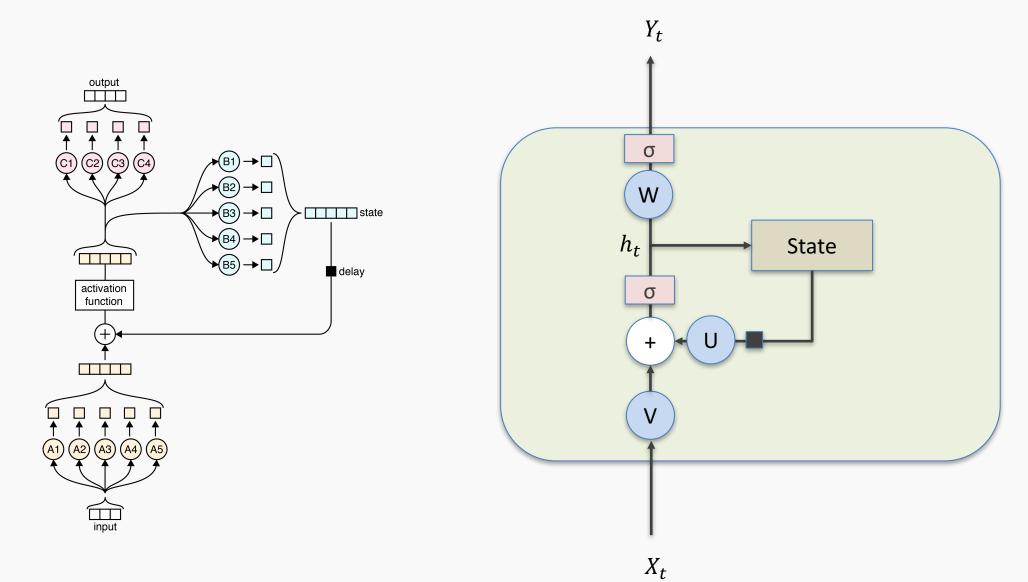


Using conventional and convenient notation



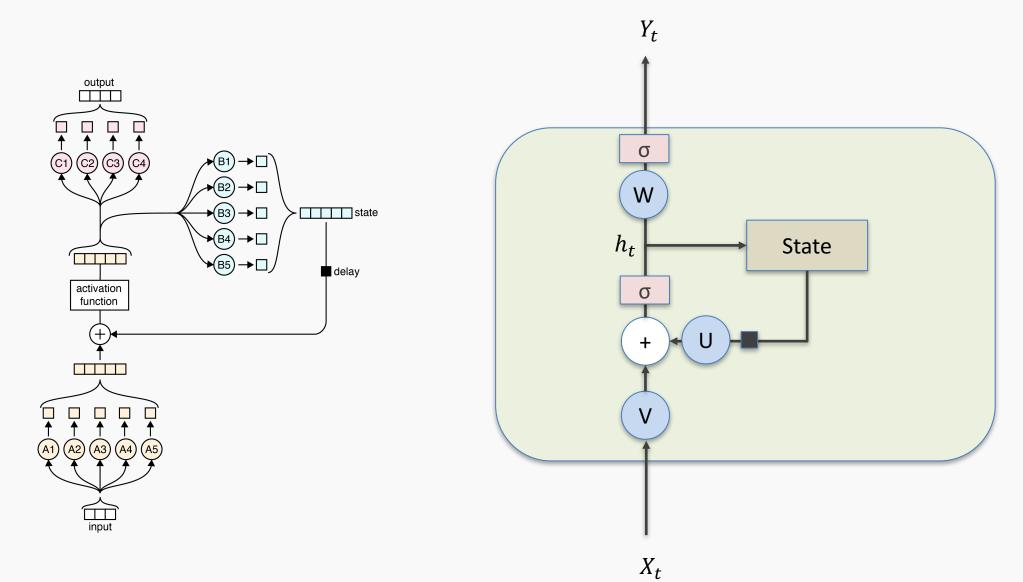


Simple RNN again



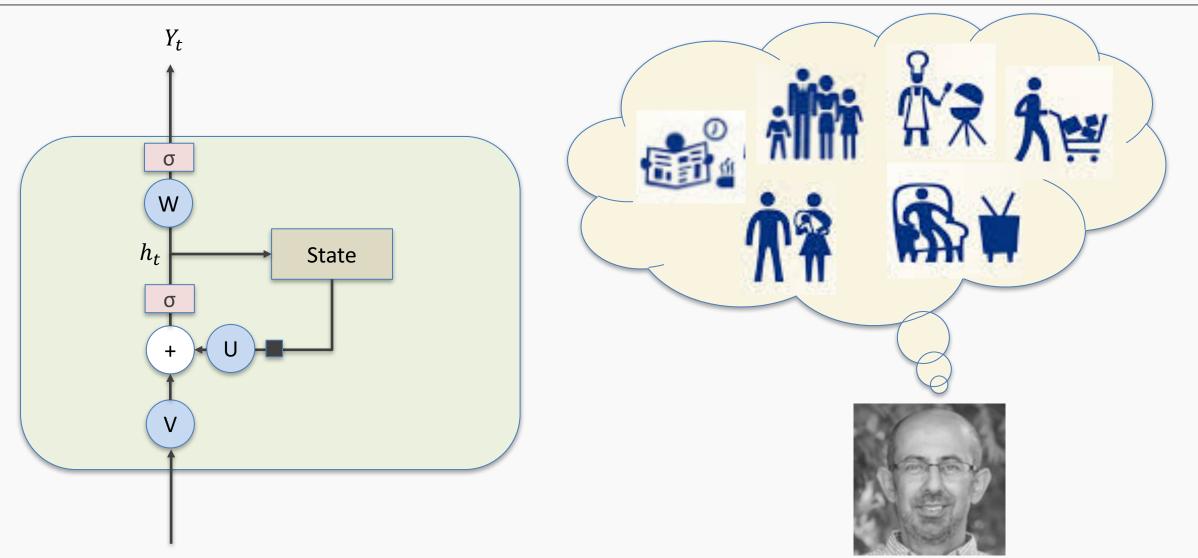


Simple RNN again





Simple RNN again: Memories

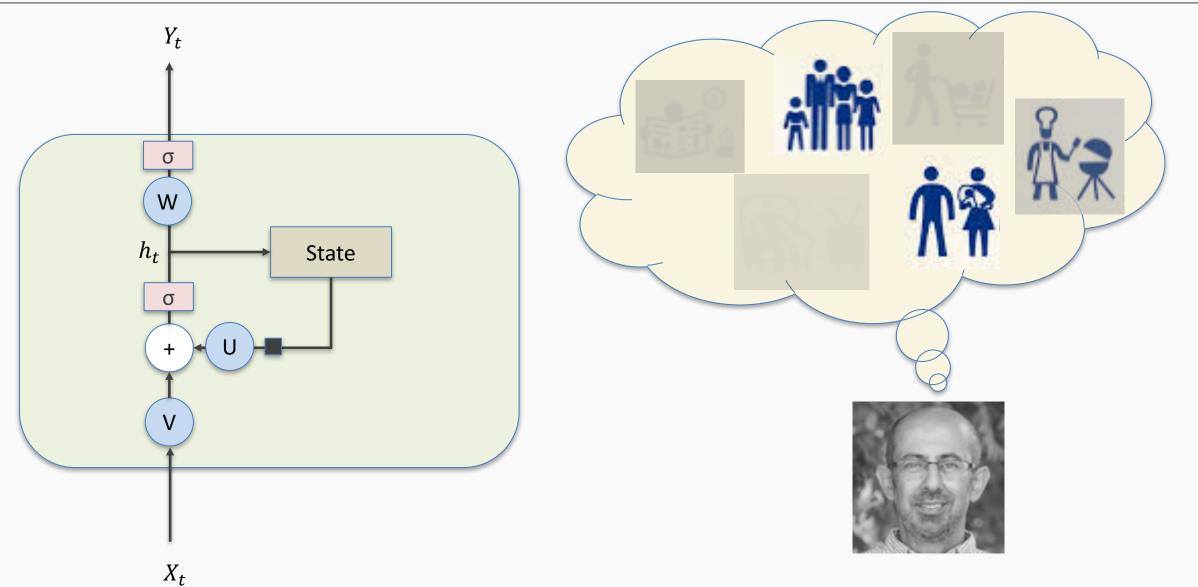




 X_t



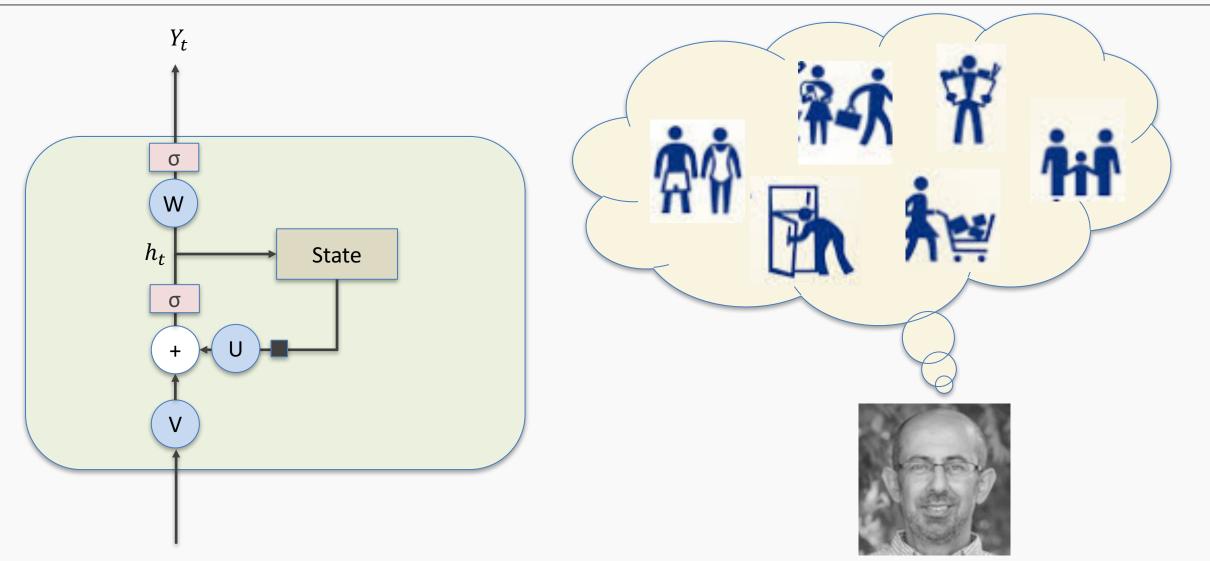
Simple RNN again: Memories - Forgetting





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Simple RNN again: New Events

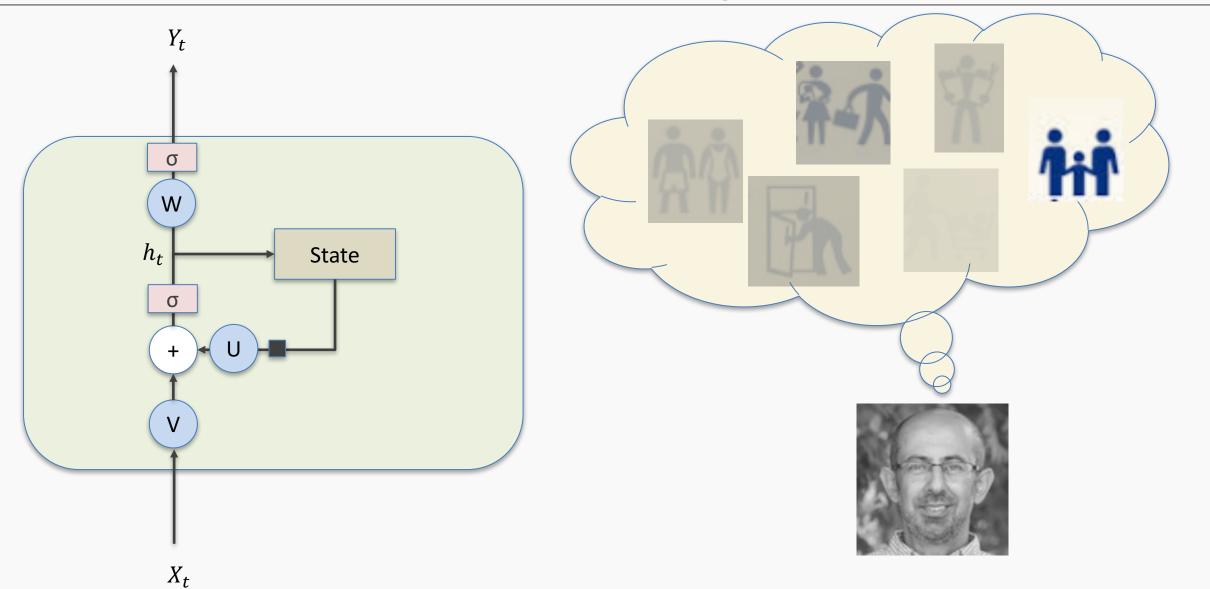




 X_t

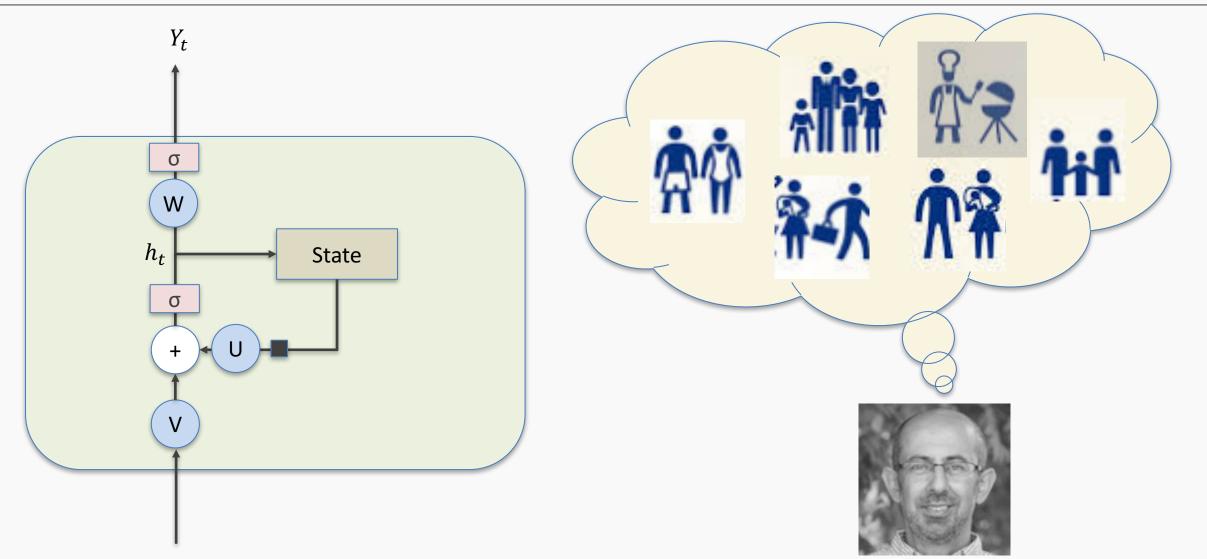
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Simple RNN again: New Events Weighted





Simple RNN again: Updated memories





 X_t

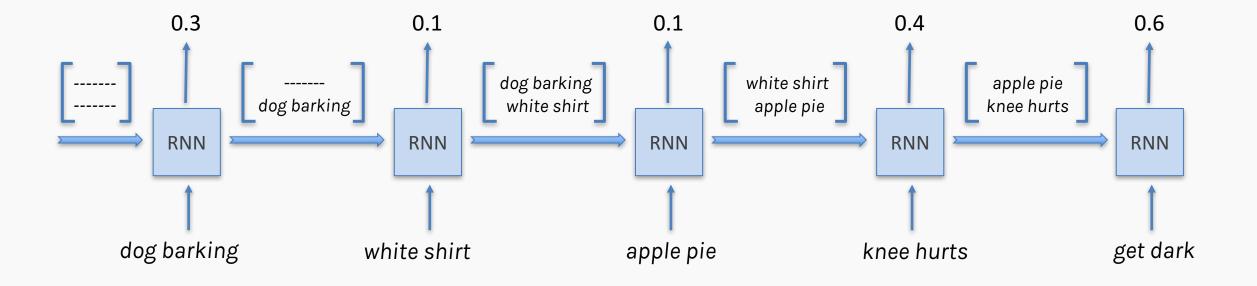
- [Chen17b] Qiming Chen, Ren Wu, "CNN Is All You Need", arXiv 1712.09662, 2017. <u>https://arxiv.org/abs/1712.09662</u>
- [Chu17] Hang Chu, Raquel Urtasun, Sanja Fidler, "Song From PI: A Musically Plausible Network for Pop Music Generation", arXiv preprint, 2017. <u>https://arxiv.org/abs/1611.03477</u>
- [Johnson17] Daniel Johnson, "Composing Music with Recurrent Neural Networks", Heahedria, 2017. <u>http://www.hexahedria.com/2015/08/03/ composing-music-with-</u> <u>recurrent-neural-networks/</u>
- [Deutsch16b] Max Deutsch, "Silicon Valley: A New Episode Written by AI", Deep Writing blog post, 2017. <u>https://medium.com/deep-writing/ silicon-valley-a-new-episode-written-by-ai-a8f832645bc2</u>
- [Fan16] Bo Fan, Lijuan Wang, Frank K. Soong, Lei Xie "Photo-Real Talking Head with Deep Bidirectional LSTM", Multimedia Tools and Applications, 75(9), 2016. <u>https://www.microsoft.com/en-us/research/wp-</u> <u>content/uploads/2015/04/icassp2015_fanbo_1009.pdf</u>



Continue on Wednesday

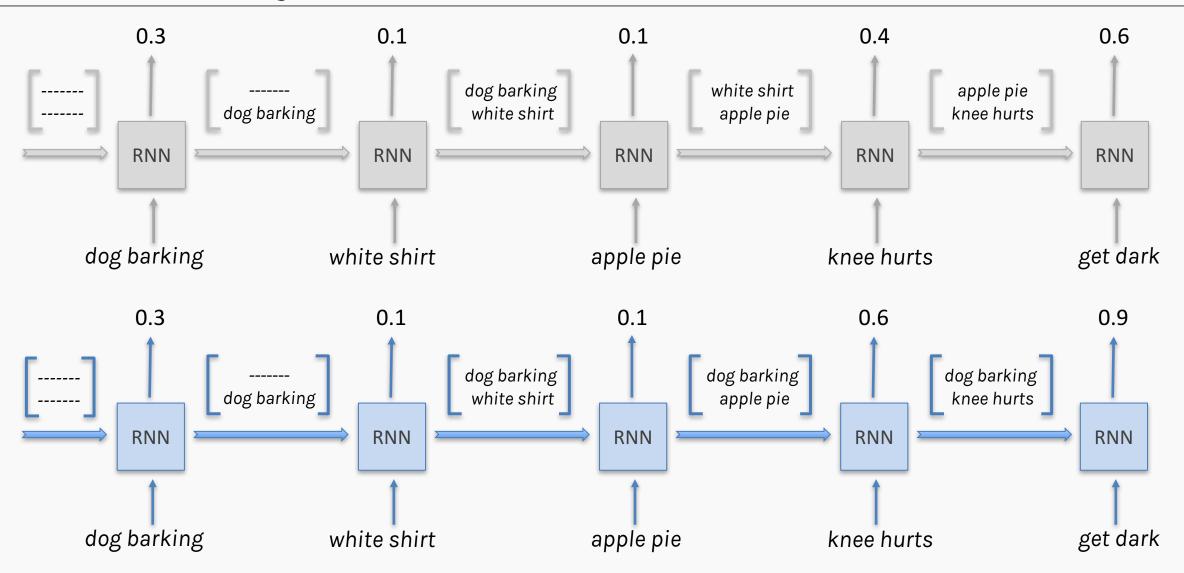


Is it raining? We build an RNN to the probability if it is raining:



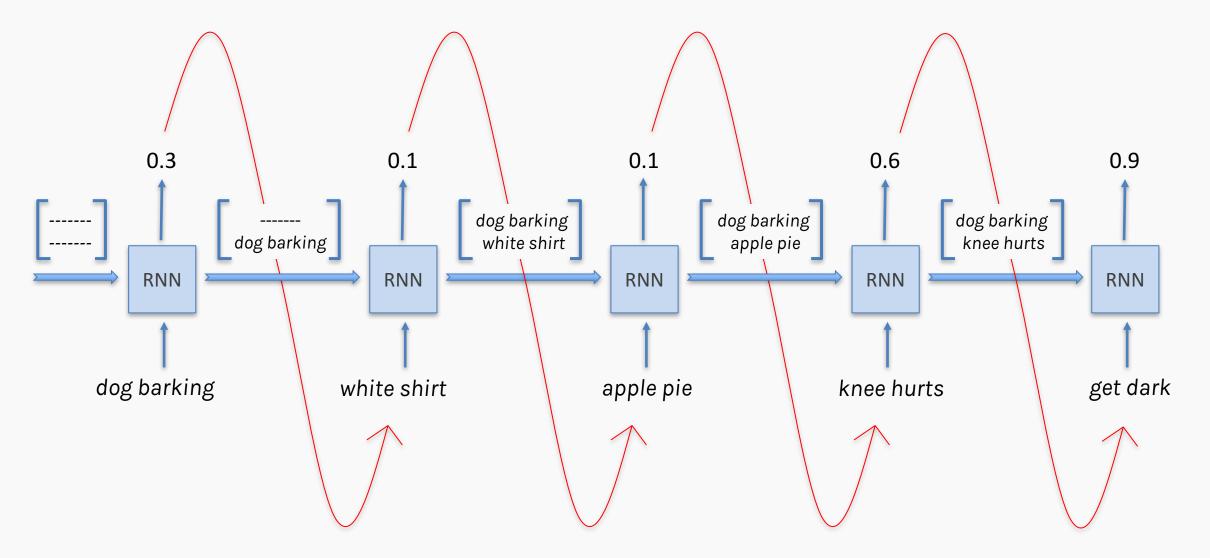


RNN + Memory



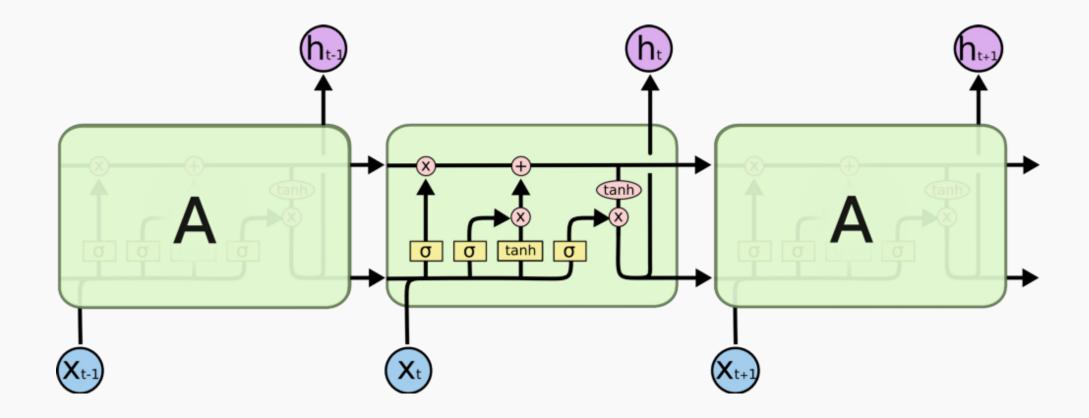


RNN + Memory + Output



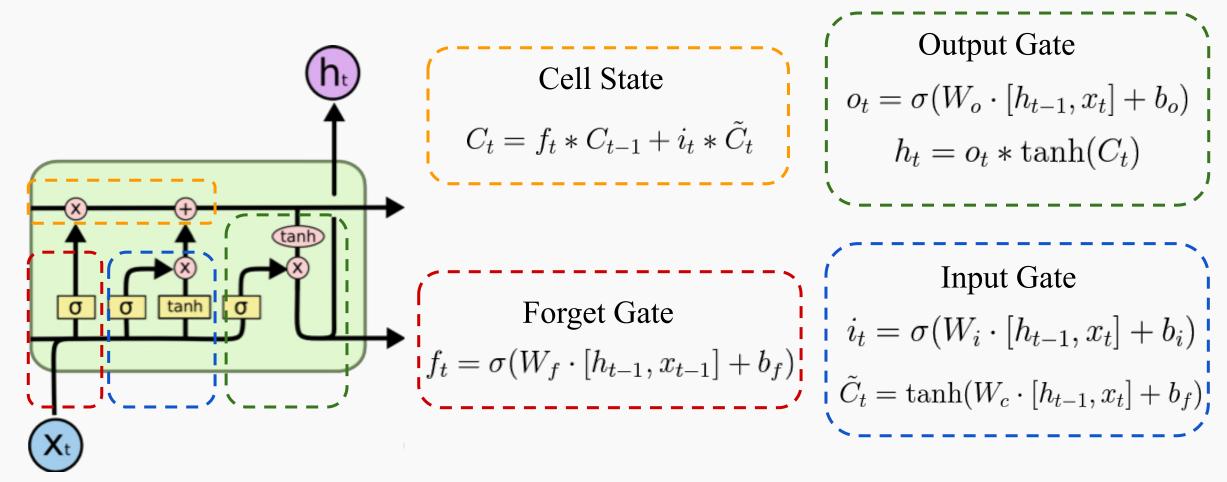


LSTM: Long short term memory



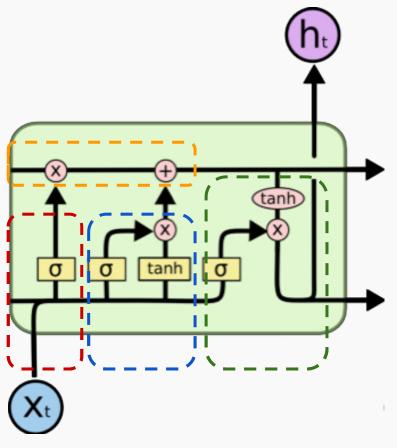


Before to really understand LSTM lets see the big picture ...





Before to really understand LSTM lets see the big picture ...



- LSTM are recurrent neural network with a cell and a hidden state, boths of these are updated in each step and can be thought as memories.
- 2. Cell states work as a long term memory and the updates depends on the relation between the hidden state in t -1 and the input.
- 3. The hidden state of the next step is a transformation of the cell state and the output (which is the section that is in general used to calculate our loss, ie information that we want in a short memory).



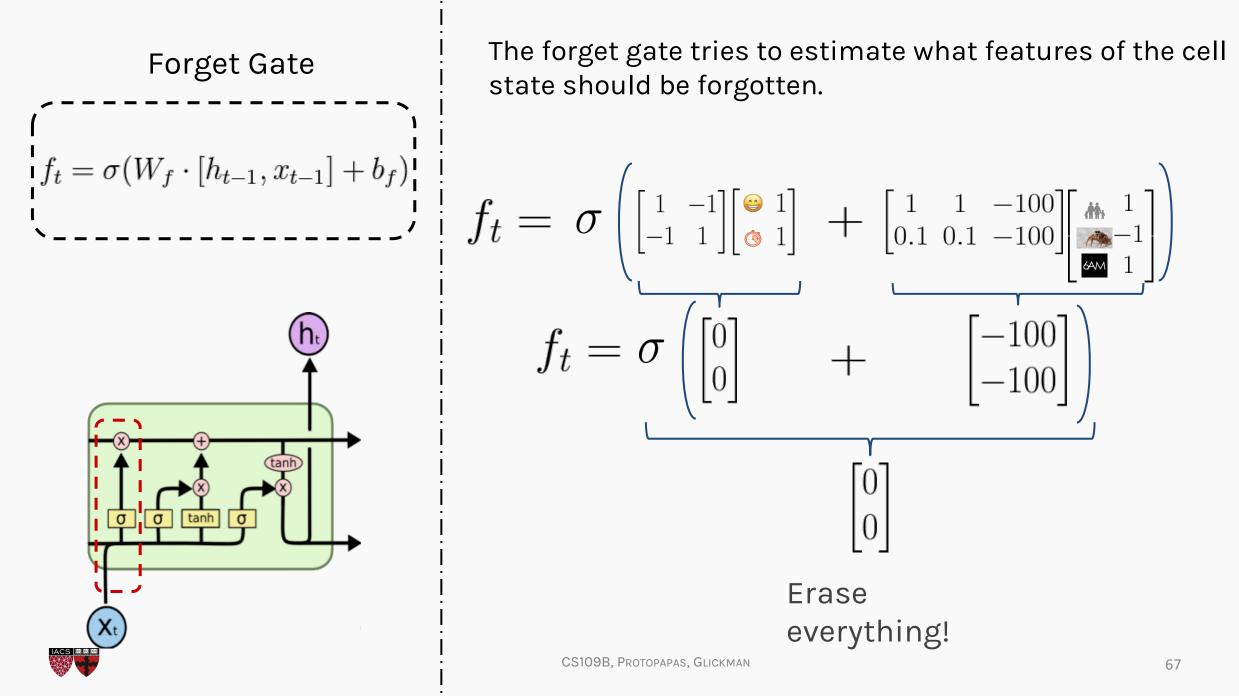
Let's think about my cell state

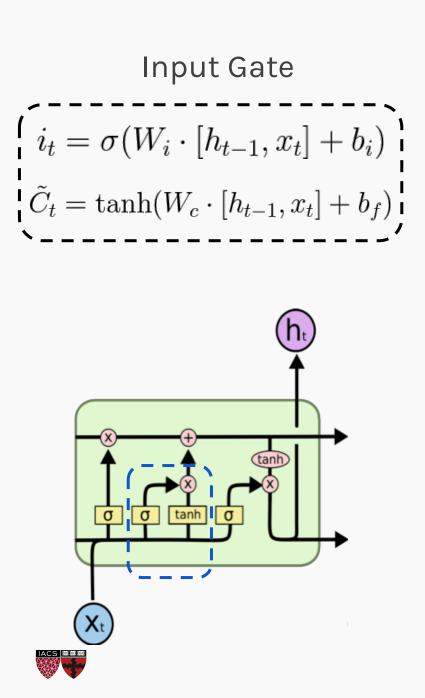
 $x_t =$

Let's predict if i will help you in the homework in time t



 $\begin{array}{c|c} & & 1 \\ \hline & & -1 \\ \hline & & -1 \\ \hline & & 1 \end{array} \end{array} \begin{array}{c} h_{t-1} = \begin{bmatrix} @ & 1 \\ @ & 1 \\ \hline & & 1 \end{bmatrix} \end{array} \begin{array}{c} C_{t-1} = \begin{bmatrix} @ & 0.7 \\ @ & 0.3 \\ \hline & & 0.3 \end{array}$



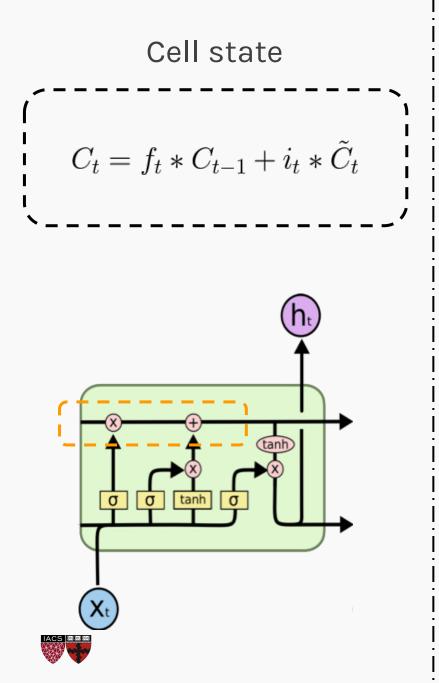


The input gate layer works in a similar way that the forget layer, the input gate layer estimate the degree of confidence of \tilde{C}_t and \tilde{C}_t is a new estimation of the cell state.

Let's say that my input gate estimation is:

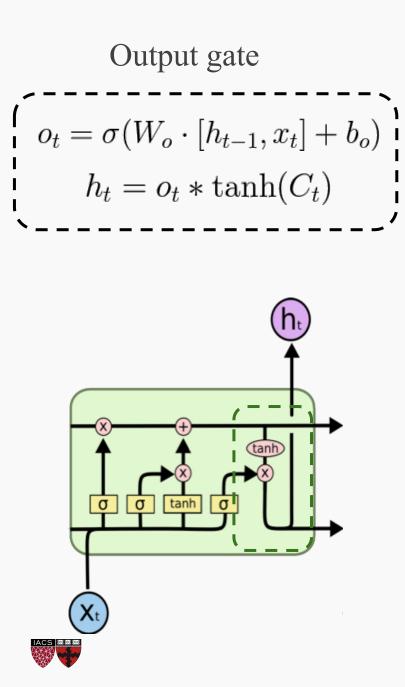
$$i_t = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

$$\tilde{C}_{t} = \tanh\left(\begin{bmatrix}1 & 0\\0 & 1\end{bmatrix}\begin{bmatrix} @ & 1\\ @ & 1\end{bmatrix} + \begin{bmatrix}10 & 1 & -1\\ -1 & 1 & 10\end{bmatrix}\begin{bmatrix} & 1\\ & & -1\\ & & & 1\end{bmatrix}\right)$$
$$\tilde{C}_{t} = \tanh\left(\begin{bmatrix}1\\1\end{bmatrix} + \begin{bmatrix}10\\10\end{bmatrix}\right)$$
$$\begin{bmatrix}@ & 1\end{bmatrix}$$



After the calculation of forget gate and input gate we can update our cell state.

$$C_{t} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \ast \begin{bmatrix} \textcircled{\begin{subarray}{c} 0.7 \\ \textcircled{\begin{subarray}{c} 0.3 \end{bmatrix}} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} \ast \begin{bmatrix} \textcircled{\begin{subarray}{c} 1 \\ \textcircled{\begin{subarray}{c} 1 \end{bmatrix}} \end{bmatrix}$$
$$C_{t} = \begin{bmatrix} \textcircled{\begin{subarray}{c} 1 \\ \textcircled{\begin{subarray}{c} 1 \end{bmatrix}} \end{bmatrix}$$



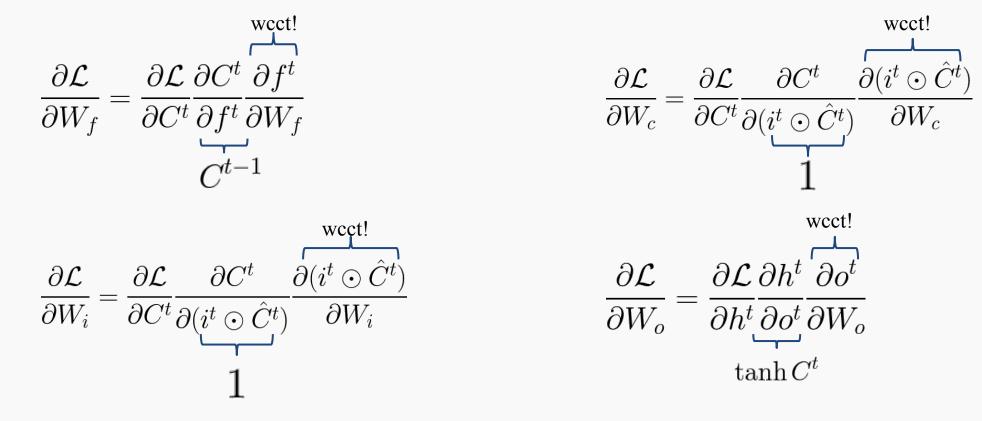
- The output gate layer is calculated using the information of the input x in time t and hidden state of the last step.
- It is important to notice that hidden state used in the next step is obtained using the output gate layer which is usually the function that we optimize.

$$o_{t} = \sigma \left(\begin{bmatrix} 1 & 1 \end{bmatrix} \begin{bmatrix} \bullet & 1 \\ \bullet & 1 \end{bmatrix} + \begin{bmatrix} 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} \bullet & 1 \\ \bullet & -1 \\ \bullet & 1 \end{bmatrix} \right)$$
$$o_{t} \approx 0.9$$
$$h_{t} \approx 0.9 * \begin{bmatrix} \bullet & 1 \\ \bullet & 1 \\ \bullet & 1 \end{bmatrix} = \begin{bmatrix} \bullet & 0.9 \\ \bullet & 0.9 \end{bmatrix}$$

wcct! = we can calculate this!

To optimize my parameters i basically need to do: Let's calculate all the derivatives in some time t!

$$W = W - \eta \frac{\partial \mathcal{L}}{\partial W}$$



So... every derivative is wrt the cell state or the hidden state

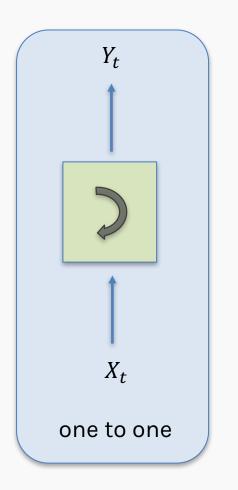
Let's calculate the cell state and the hidden state

$$\frac{\partial \mathcal{L}}{\partial h^{t-1}} = \frac{\partial \mathcal{L}}{\partial C^t} \left(\frac{\partial C^t}{\partial f^t} \frac{\partial f^t}{\partial h^t} + \frac{\partial C^t}{\partial (i^t \odot \hat{C}^t)} \frac{\partial (i^t \odot \hat{C}^t)}{\partial h^t} \right) + \frac{\partial \mathcal{L}}{\partial h^t} \frac{\partial h^t}{\partial o^t} \frac{\partial o^t}{\partial h^{t-1}}$$

$$\begin{aligned} \frac{\partial \mathcal{L}}{\partial C^{t}} &= \frac{\partial \mathcal{L}}{\frac{\partial (f^{t+1} \odot C^{t} + i^{t+1} \odot \hat{C}^{t})}{Q(f^{t+1} \odot C^{t} + i^{t+1} \odot \hat{C}^{t})}} \underbrace{\frac{\partial (f^{t+1} \odot C^{t} + i^{t+1} \odot \hat{C}^{t})}{QC^{t}}}_{\left(\frac{\partial \mathcal{L}}{\partial C^{t+1}} + \frac{\partial \mathcal{L}}{\partial h^{t+1}} \frac{\partial h^{t+1}}{QC^{t+1}}\right) \odot f^{t+1}} \end{aligned}$$

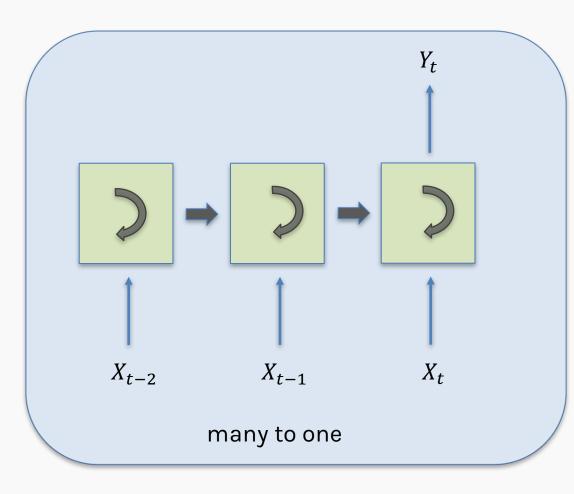


RNN Structures



- The one to one structure is useless.
- It takes a single input and it produces a single output.
- Not useful because the RNN cell is making little use of its unique ability to remember things about its input sequence

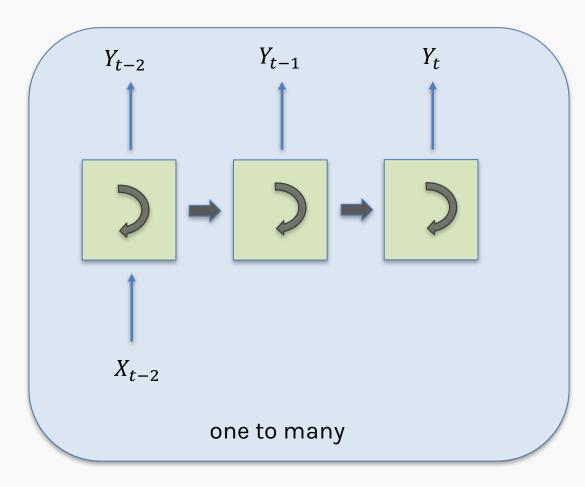




The many to one structure reads in a sequence and gives us back a single value. Example: Sentiment analysis, where the network is given a piece of text and then reports on some quality inherent in the writing. A common example is to look at a movie review and determine if it was positive or negative.



RNN Structures (cont)

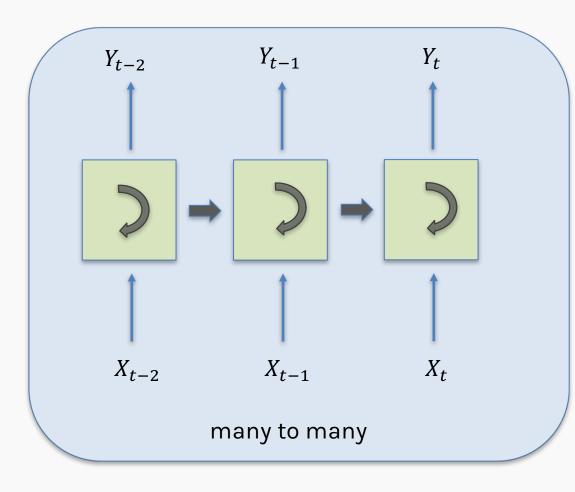


The **one to many** takes in a single piece of data and produces a sequence.

For example we give it the starting note for a song, and the network produces the rest of the melody for us.

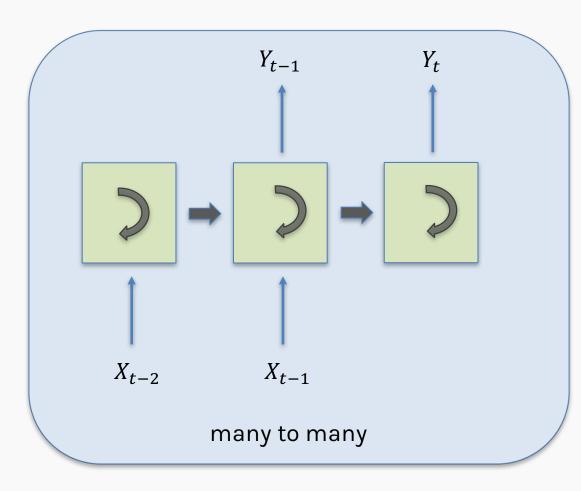


RNN Structures (cont)



The **many to many** structures are in some ways the most interesting. used for machine translation. Example: Predict if it will rain given some inputs.





This form of **many to many** can be used for machine translation.

For example, the English sentence: **"The black dog jumped over the cat"** In Italian as: "Il cane nero saltò sopra il gatto" In the Italia, the adjective "nero" (black) follows the noun "cane" (dog), so we need to have some kind of buffer so we can produce the words in their proper English.



LSTM and RNN are designed to analyze sequence of values.

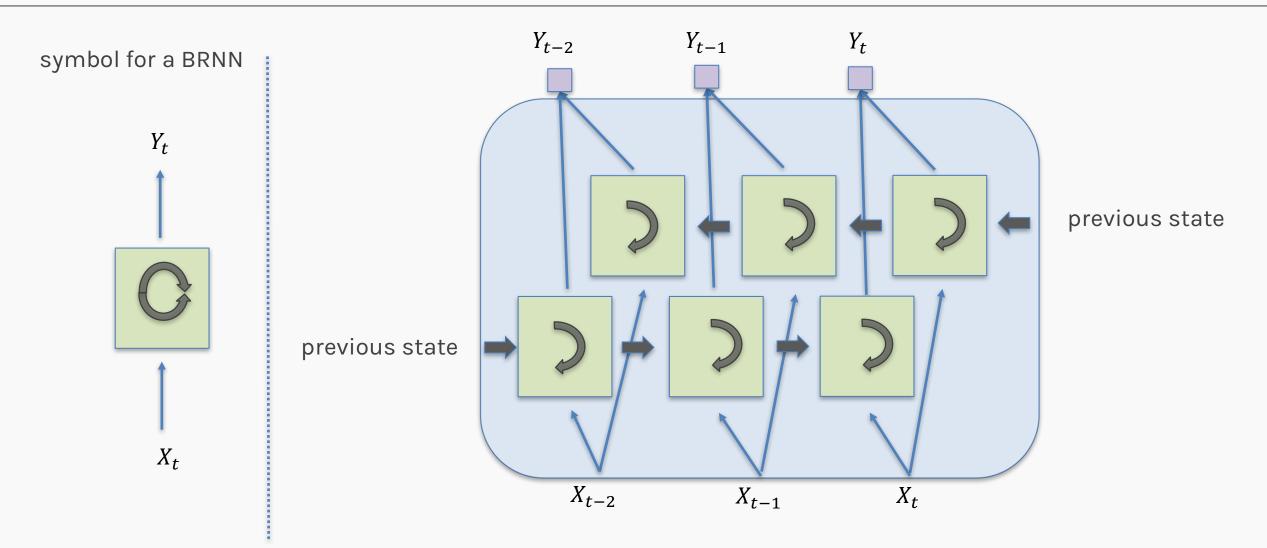
For example: Patrick said he needs a vacation. he here means Patrick and we know this because Patrick was before the word he.

However consider the following sentence: He needs to work more, Pavlos said about Patrick.

Bidirectional RNN or BRNN or bidirectional LSTM or BLSTM when using LSTM units.



Bidirectional (cond)



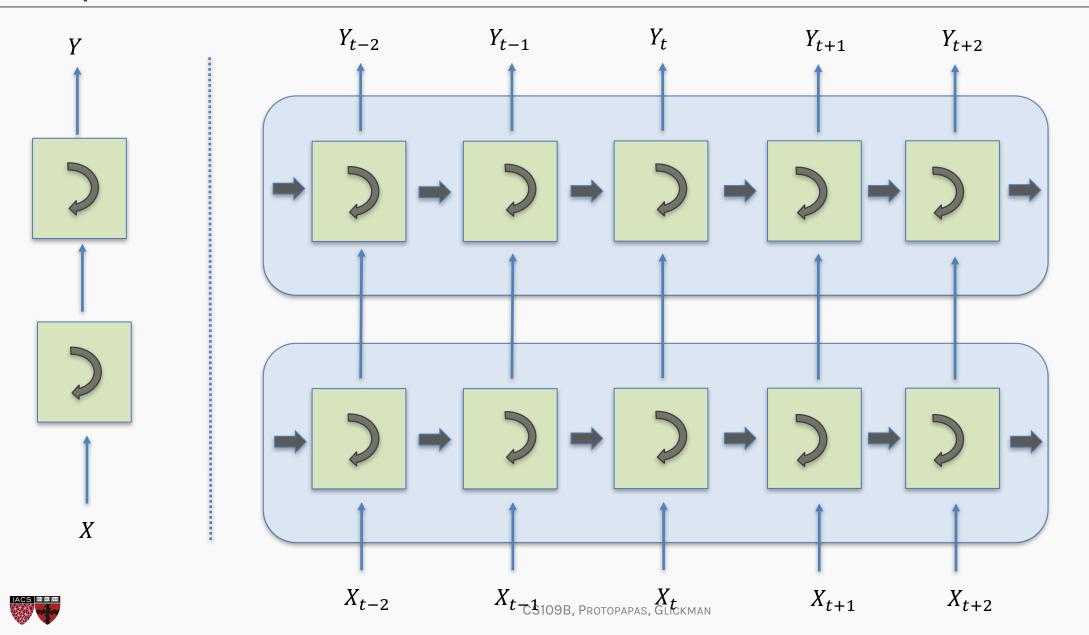


LSTM units can be arranged in layers, so that each the output of each unit is the input to the other units. This is called **a deep RNN**, where the adjective "deep" refers to these multiple layers.

- Each layer feeds the LSTM on the next layer
- First time step of a feature is fed to the first LSTM, which processes that data and produces an output (and a new state for itself).
- That output is fed to the next LSTM, which does the same thing, and the next, and so on.
- Then the second time step arrives at the first LSTM, and the process repeats.

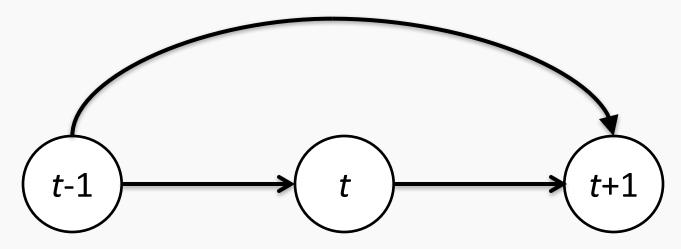


Deep RNN



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Add additional connections between units *d* time steps apart Creating paths through time where gradients neither vanish or explode



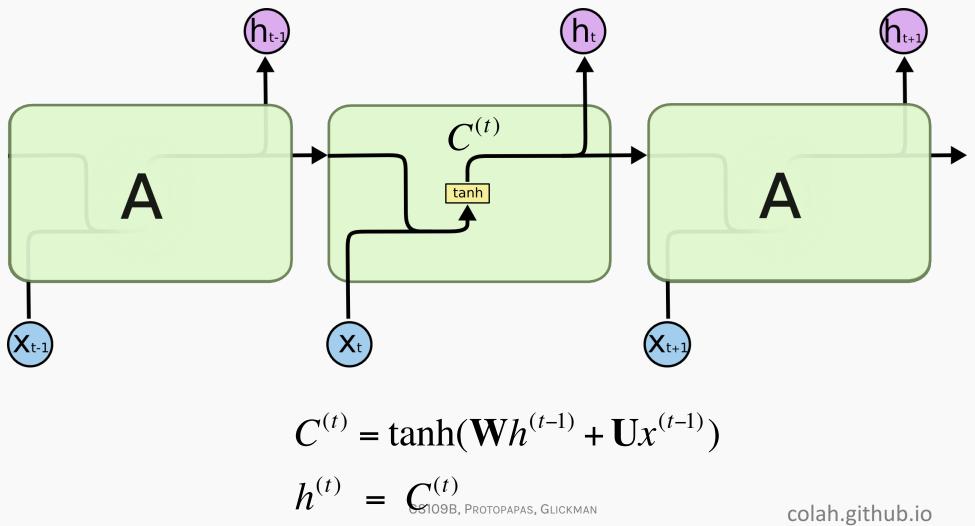


Linear self-connections

Maintain cell state: running average of past hidden activations



Standard RNN



Leaky Unit

