# Lecture 19: NN Regularization

### CS109A Introduction to Data Science Pavlos Protopapas and Kevin Rader



- Norm Penalties
- Early Stopping
- Data Augmentation
- Sparse Representation
- Bagging
- Dropout



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# Regularization

Regularization is any modification we make to a learning algorithm that is intended to **reduce its generalization** error but not its training error.



Fitting a deep neural network with 5 layers and 100 neurons per layer can lead to a very good prediction on the training set but poor prediction on validations set.





We used to optimize:

J(W; X, y)

Change to ...





- L<sub>2</sub> regularization:
  - Weights decay
  - MAP estimation with Gaussian prior
- L<sub>1</sub> regularization:
  - encourages sparsity
  - MAP estimation with Laplacian prior

 $\Omega(W) = \frac{1}{2} \parallel W \parallel_1$ 



### Norm Penalties

We used to optimize:  $W^{(i+1)} = W^{(i)} - \lambda \frac{\partial J}{\partial W}$ Change to ...  $J_R(W; X, y) = J(W; X, y) + \frac{1}{2} \alpha W^2$ Biases not  $W^{(i+1)} = W^{(i)} - \lambda \frac{\partial J}{\partial W} - \lambda \alpha W$ Biases not penalized

L<sub>2</sub> regularization:

- Decay of weights
- MAP estimation with Gaussian prior
- *L*<sub>1</sub> regularization:
  - encourages sparsity
  - MAP estimation with Laplacian prior

 $\Omega(W) = \frac{1}{2} \parallel W \parallel_2^2$ 

$$\Omega(W) = \frac{1}{2} \parallel W \parallel_1$$



### Norm Penalties



$$\Omega(W) = \frac{1}{2} \parallel W \parallel_2^2$$

$$\Omega(W) = \frac{1}{2} \parallel W \parallel_1$$

 $\min_{\Omega(W)\leq K}J(W;X,y)$ 

Useful if K is known in advance

Optimization:

- Construct Lagrangian and apply gradient descent
- Projected gradient descent



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Early stopping: terminate while validation set performance is better





# Early Stopping





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# Data Augmentation





flip-Ir



crop-and-pan



flip-ud



elastic









### Data Augmentation





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 $J(\theta; X, y)$ 







 $J_R(W; X, y) = J(\theta; X, y) + \alpha \Omega(W)$ 





CS109A, PROTOPAPAS, RAD Weights in output layer



 $J(\theta; X, y)$ 

$$[4.34] = [3.2 \ 2 \ 1] \begin{bmatrix} 2 \\ -2.2 \\ 1.3 \end{bmatrix} \xrightarrow{h_{31}, h_{32}, h_{33}}$$





 $J_R(W; X, y) = J(\theta; X, y) + \alpha \Omega(h)$ 





CS109A, PROTOPAPAS, RADER

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Original dataset First ensemble member First resampled dataset 8 Second resampled dataset Second ensemble member 8



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#### Random perturbation of network weights

- Gaussian noise: Equivalent to minimizing loss with regularization term
- Encourages smooth function: small perturbation in weights leads to small changes in output
- Injecting noise in output labels
  - Better convergence: prevents pursuit of hard probabilities



Train all sub-networks obtained by removing nonoutput units from base network





For each new example/mini-batch:

- Randomly sample a binary mask  $\mu$  independently, where  $\mu_i$  indicates if input/hidden node *i* is included
- Multiply output of node *i* with  $\mu_i$ , and perform gradient update

Typically, an input node is **included** with **prob=0.8**, hidden node with **prob=0.5**.



During prediction time use all units, but scale weights with probability of inclusion





## Adversarial Examples



### **Adversarial Examples**



Panda 57% confidence noise

Gibbon 99.3% confidence

Training on adversarial examples is mostly intended to improve security, but can sometimes provide generic regularization.



### Recap

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